

The particle size distribution and its optical proxies

Questions:

- What about a particle can we infer from its size?

The particle size distribution and its optical proxies

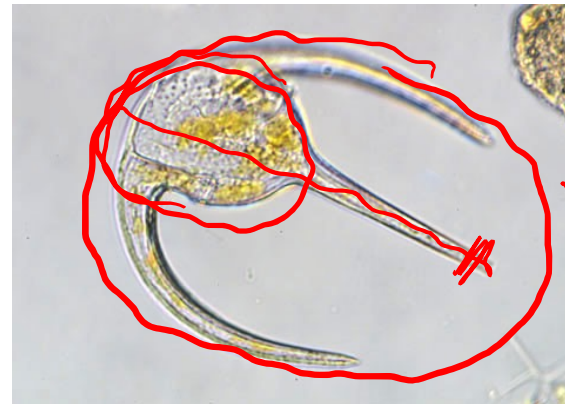
Questions:

- What about a particle can we infer from its size?
- What processes are affected by size?

The particle size distribution and its optical proxies

Questions:

- What about a particle can we infer from its size?
- What processes are affected by size?
- What is the size of:

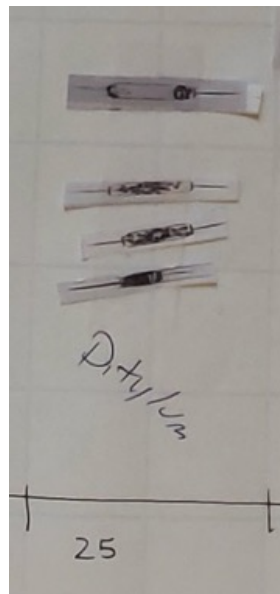
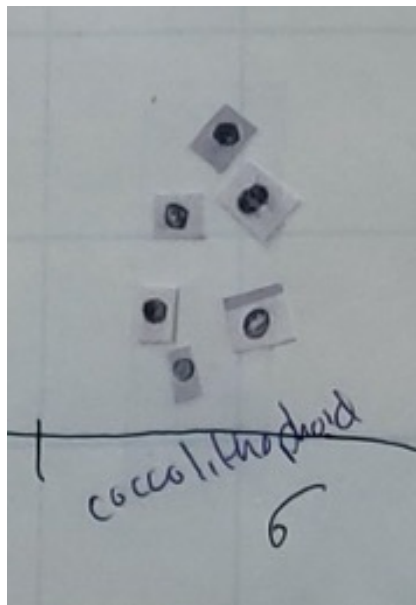
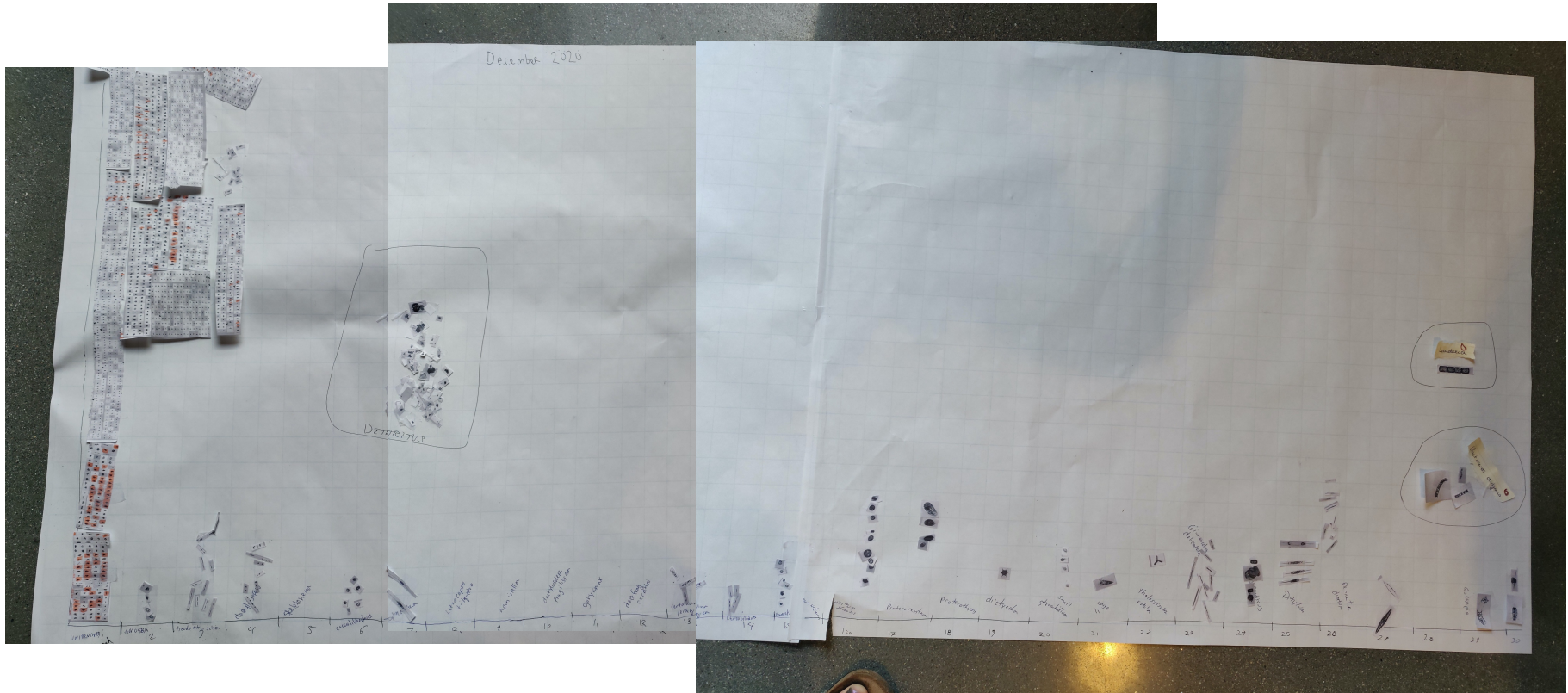


Sphere
↓
ESD

The calculus of size distribution

- How do we characterize the size of particles of varying shape?
- What aspects of size are different observations sensitive to?
- What are the units of the size distribution?
- How do we approximate discrete observations with a continuous distribution?
- How do we compare observations that have different size bins?
- What are the uncertainties in a size distribution?
- How do we convert back and forth between number size distribution and volume or mass?

Manual sorting of IFCB data: December 2020 data (excluding "detritus")



Uncertainty

Counting error $\sim \sqrt{N}$

detection limit - small end (inst.)

large end (sample size)

Size bin choice, units

Regular increment
↓
log spacing

| <i>Category</i> | <i>N</i> | <i>Size (um)</i> |
|-------------------|----------|------------------|
| 1 | 1150 | 10 |
| 6 | 6 | 10 |
| 15 | 5 | 20 |
| 20 | 4 | 20 |
| 3 | 10 | 30 |
| 4 | 7 | 30 |
| 7 | 2 | 30 |
| 13 | 4 | 30 |
| 14 | 4 | 30 |
| 16 | 9 | 30 |
| 19 | 1 | 30 |
| 17 | 4 | 40 |
| 30 | 2 | 40 |
| 23 | 10 | 50 |
| 22 | 1 | 60 |
| 21 | 1 | 70 |
| 24 | 3 | 70 |
| 25 | 4 | 70 |
| C. didymus | 2 | 70 |
| 26 | 8 | 100 |
| 29 | 1 | 120 |
| Lauderia | 1 | 130 |
| 27 | 3 | 140 |

Geometric Mean = $\sqrt{D_1 \cdot D_2}$

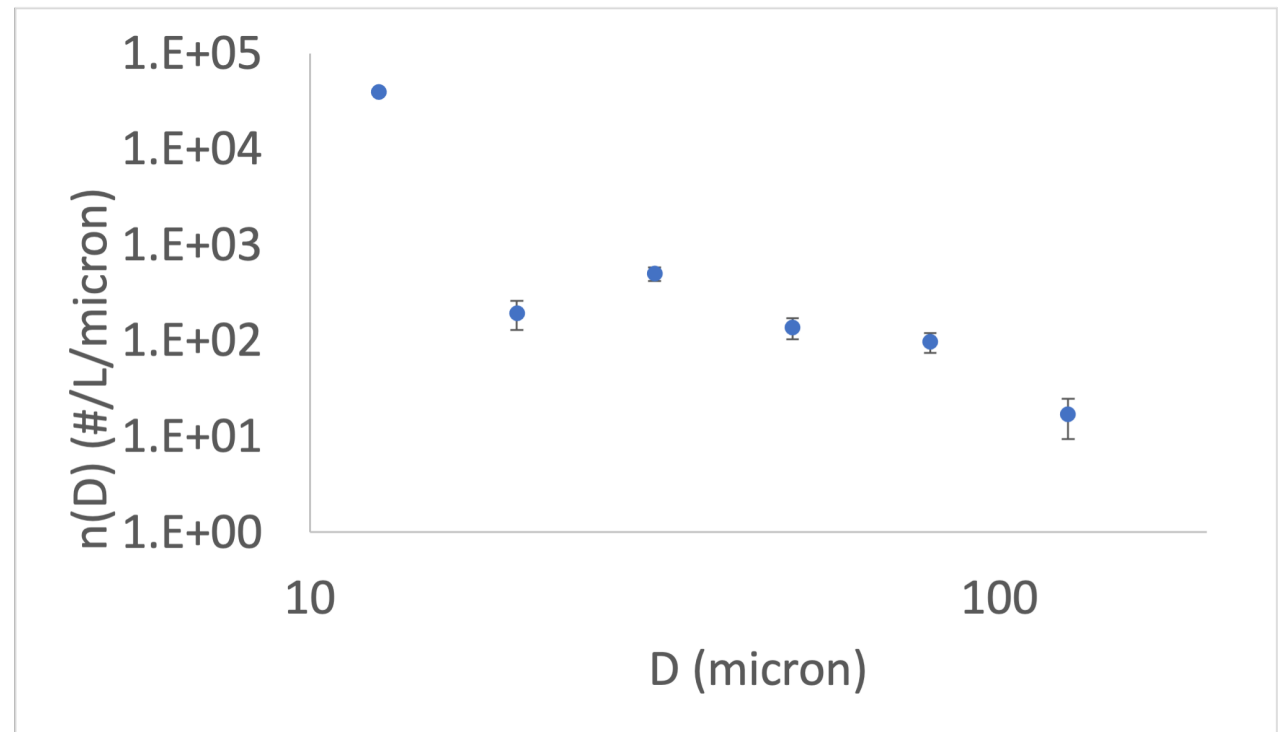
| Category | N | Size (um) | N | Size bin edges | Size bin center | N (between edges) | Nerr | Rel. err | N(D) (#/L) | N(D)err (#/L) |
|------------|------|-----------|------|----------------|-----------------|-------------------|------|----------|------------|---------------|
| 1 | 1150 | 10 | 1150 | 10 | 13 | 1156 | 34 | 3% | 231200 | 6800 |
| 6 | 6 | 10 | 6 | 16 | 20 | 9 | 3 | 33% | 1800 | 600 |
| 15 | 5 | 20 | 5 | 25 | 32 | 37 | 6 | 16% | 7400 | 1217 |
| 20 | 4 | 20 | 4 | 40 | 50 | 16 | 4 | 25% | 3200 | 800 |
| 3 | 10 | 30 | 10 | 63 | 79 | 18 | 4 | 24% | 3600 | 849 |
| 4 | 7 | 30 | 7 | 100 | 126 | 5 | 2 | 45% | 1000 | 447 |
| 7 | 2 | 30 | 2 | 158 | | | | | | |
| 13 | 4 | 30 | 4 | | | | | | | |
| 14 | 4 | 30 | 4 | | | | | | | |
| 16 | 9 | 30 | 9 | | | | | | | |
| 19 | 1 | 30 | 1 | | | | | | | |
| 17 | 4 | 40 | 4 | | | | | | | |
| 30 | 2 | 40 | 2 | | | | | | | |
| 23 | 10 | 50 | 10 | | | | | | | |
| 22 | 1 | 60 | 1 | | | | | | | |
| 21 | 1 | 70 | 1 | | | | | | | |
| 24 | 3 | 70 | 3 | | | | | | | |
| 25 | 4 | 70 | 4 | | | | | | | |
| C. didymus | 2 | 70 | 2 | | | | | | | |
| 26 | 8 | 100 | 8 | | | | | | | |
| 29 | 1 | 120 | 1 | | | | | | | |
| Lauderia | 1 | 130 | 1 | | | | | | | |
| 27 | 3 | 140 | 3 | | | | | | | |

What if we want to compare these discrete data to another measurement? Or model a continuous distribution?

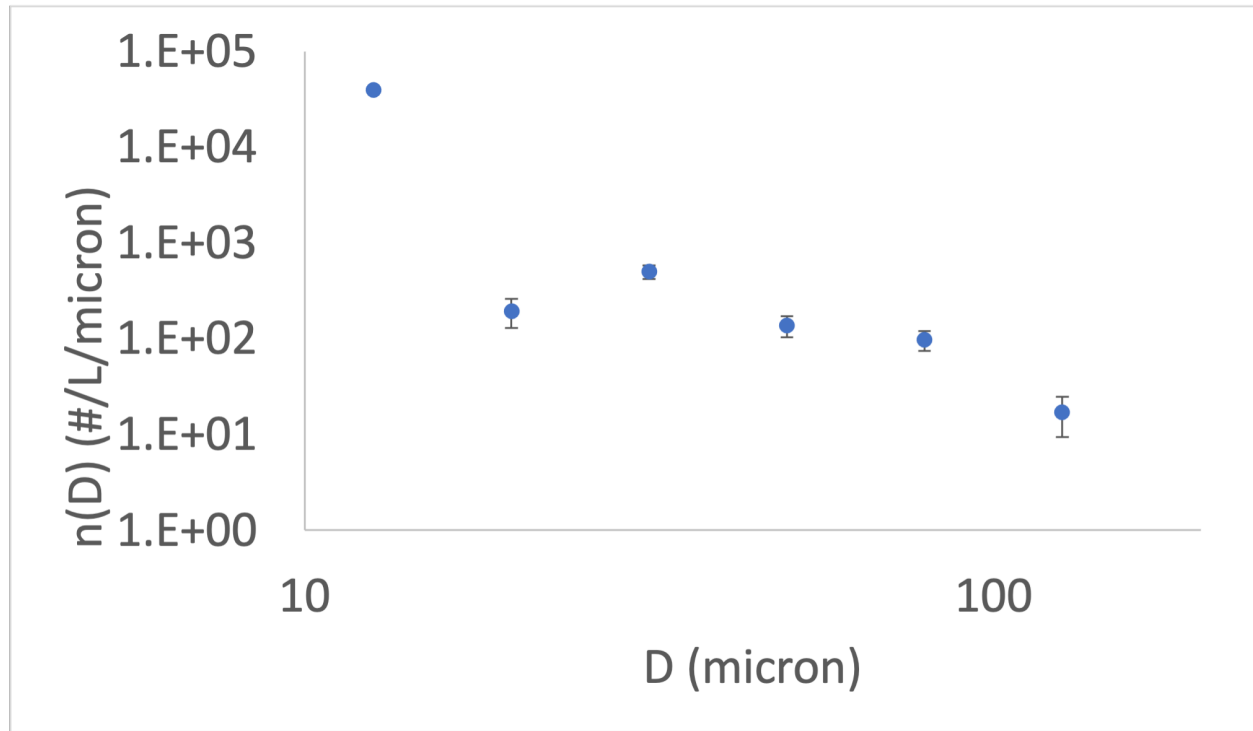
What if we want to compare these discrete data to another measurement? Or model a continuous distribution? --> differential number size distribution

$$\frac{N(\#/L)}{\Delta D (\mu m)} \approx n(D) \left[\#/L/\mu m \right]$$

differential number size distribution



How do we go from a differential number size distribution to a volume size distribution?



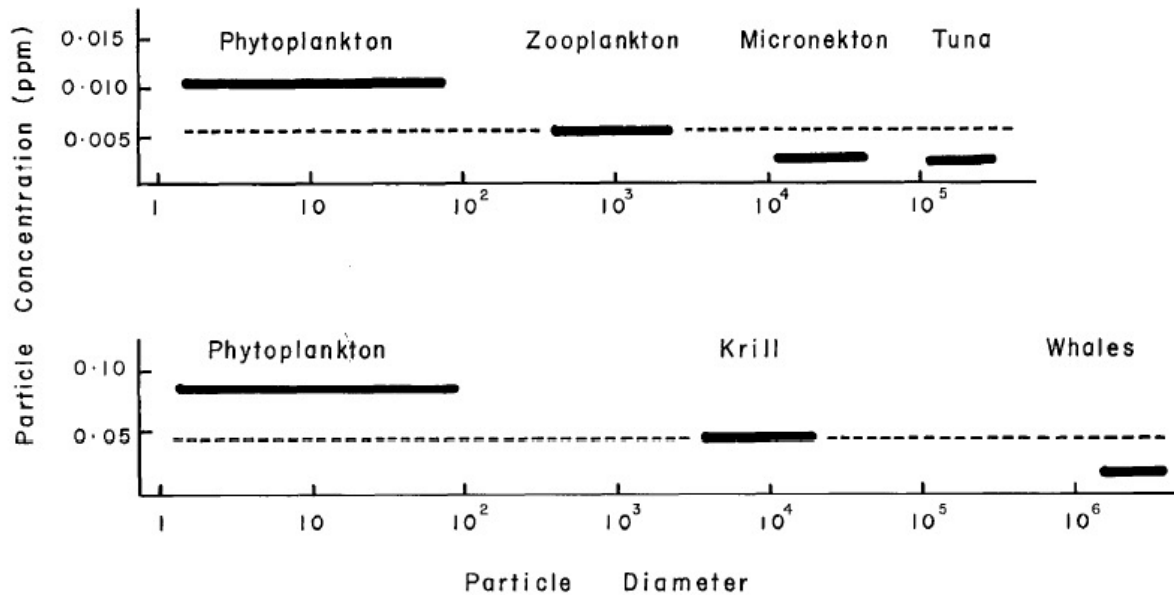
LISST



$$\frac{\mu\text{L}}{\text{L}} \text{ or ppm}$$

$$\frac{\# \text{ particles}}{\text{L} \cdot \mu\text{m}} \times \frac{V_{\text{part}} (\mu\text{L})}{\text{particle}} \times \Delta D (\mu\text{m}) = \frac{\mu\text{L}}{\text{L}}$$

Size distributions in the ocean



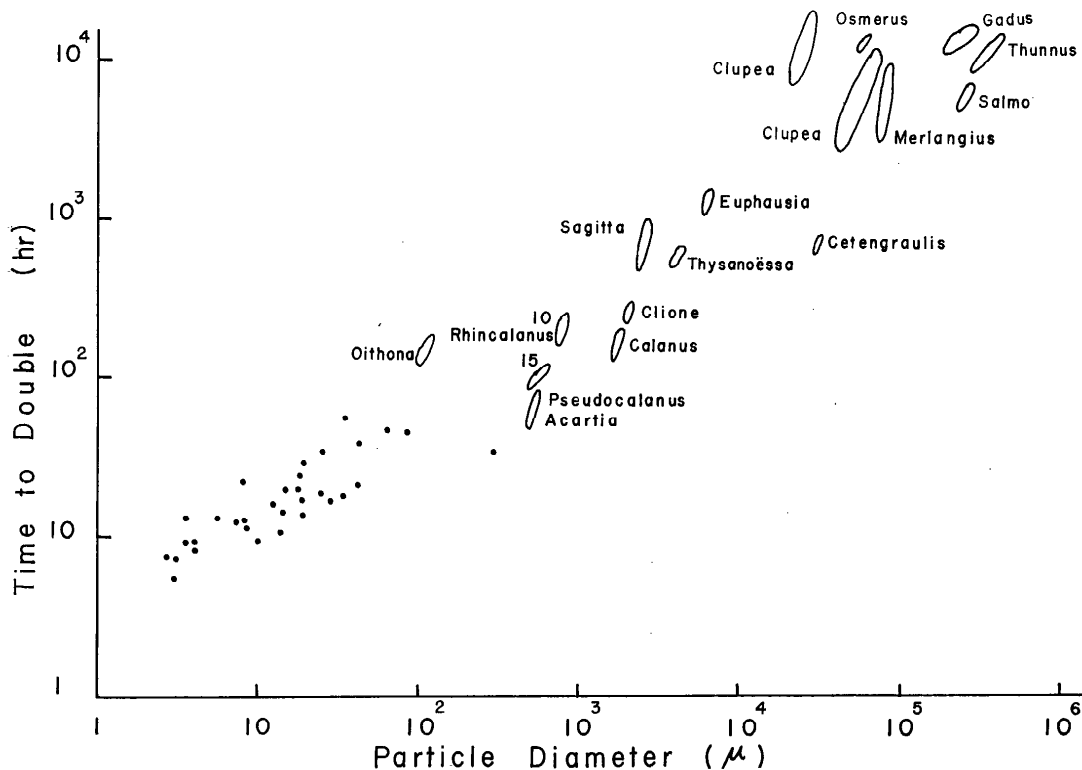
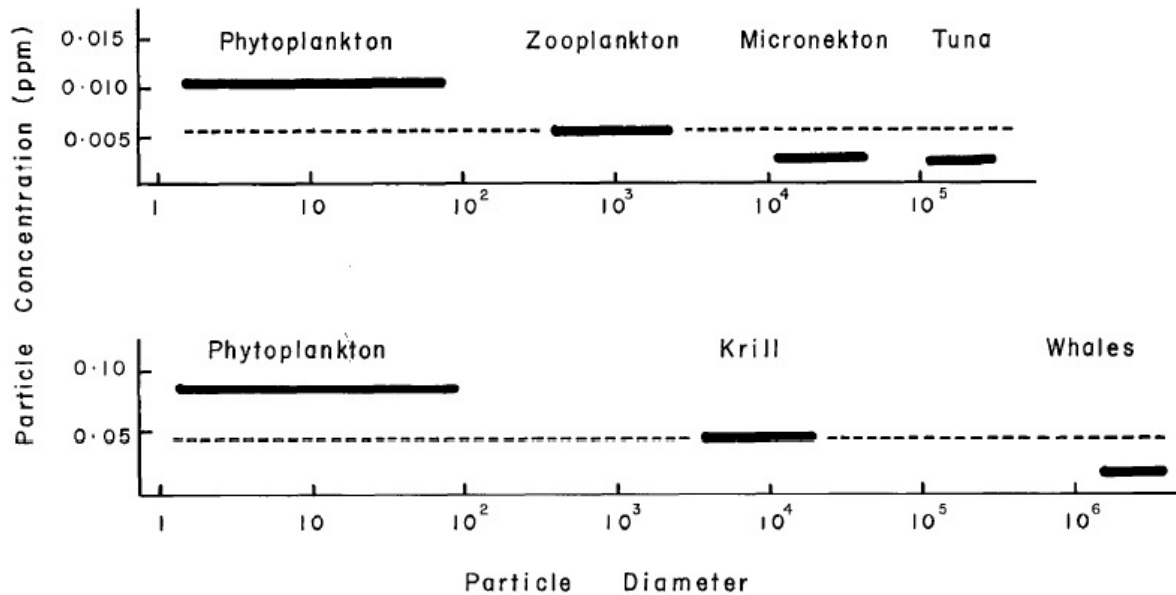
Sheldon et al., 1972:

- To first order, there are roughly equal amounts of material in particles of all sizes ranging logarithmically “**from 1 μ to about 10⁶ μ , i.e. from bacteria to whales**”
- Consistent with $n(D) \sim D^{-4}$

Dunge

Size distributions in the ocean

PARTICLES IN THE OCEAN



Sheldon et al., 1972:

- To first order, there are roughly equal amounts of material in particles of all sizes ranging logarithmically “from 1 μ to about 10⁶ μ, i.e. from bacteria to whales”
- Consistent with $n(D) \sim D^{-4}$
- Has important ecological implications: growth rates must be inversely related to particle size, if this canonical value holds everywhere

A few common models used to approximate PSDs

Power-law size distribution:

$$f(D) = \begin{cases} 0, & \text{if } D < D_{\min} \text{ or } D > D_{\max}; \\ n_0 \left[\frac{D}{D_0} \right]^{-\xi}, & \text{if } D_{\min} \leq D \leq D_{\max} \end{cases} \quad [\# \text{ m}^{-3} \mu\text{m}^{-1}],$$

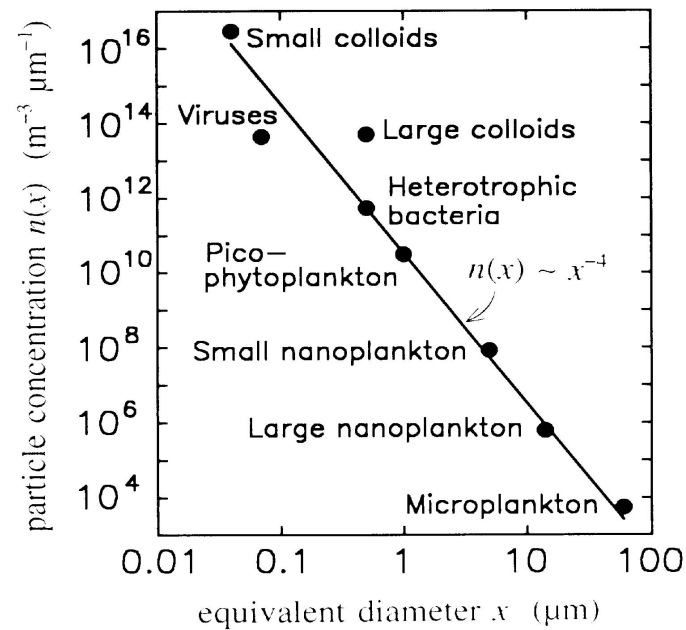


Fig. 3.2. Number size distribution typical of biological particles in the open ocean. [figure courtesy of D. Stramski]

A few common models used to approximate PSDs

Gamma:

$$n(r) = \begin{cases} 0 & r < 0 \\ Cr^{\mu}e^{-br} & r \geq 0; \mu > -1; b > 0, \end{cases}$$

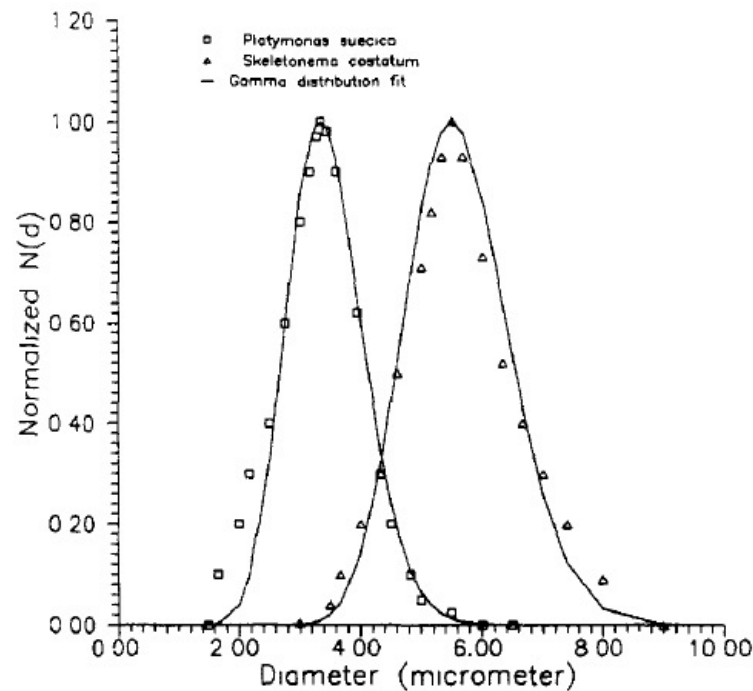
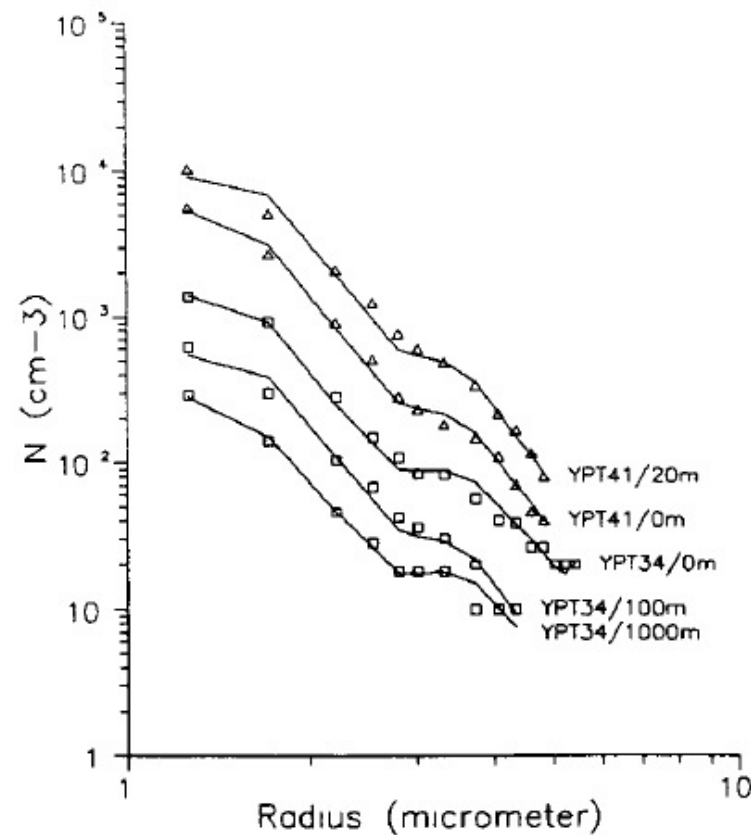


Fig 1 Normalized size distribution of phytoplankton species *Platymonas suecica* and *Skeletonema costatum* (BRICAUD and MOREL, 1986) and corresponding gamma distributions fit. Parameters of the respective distributions are $\mu = 20, b = 5.71$ and $\mu = 40, b = 7.279$

A few common models used to approximate PSDs

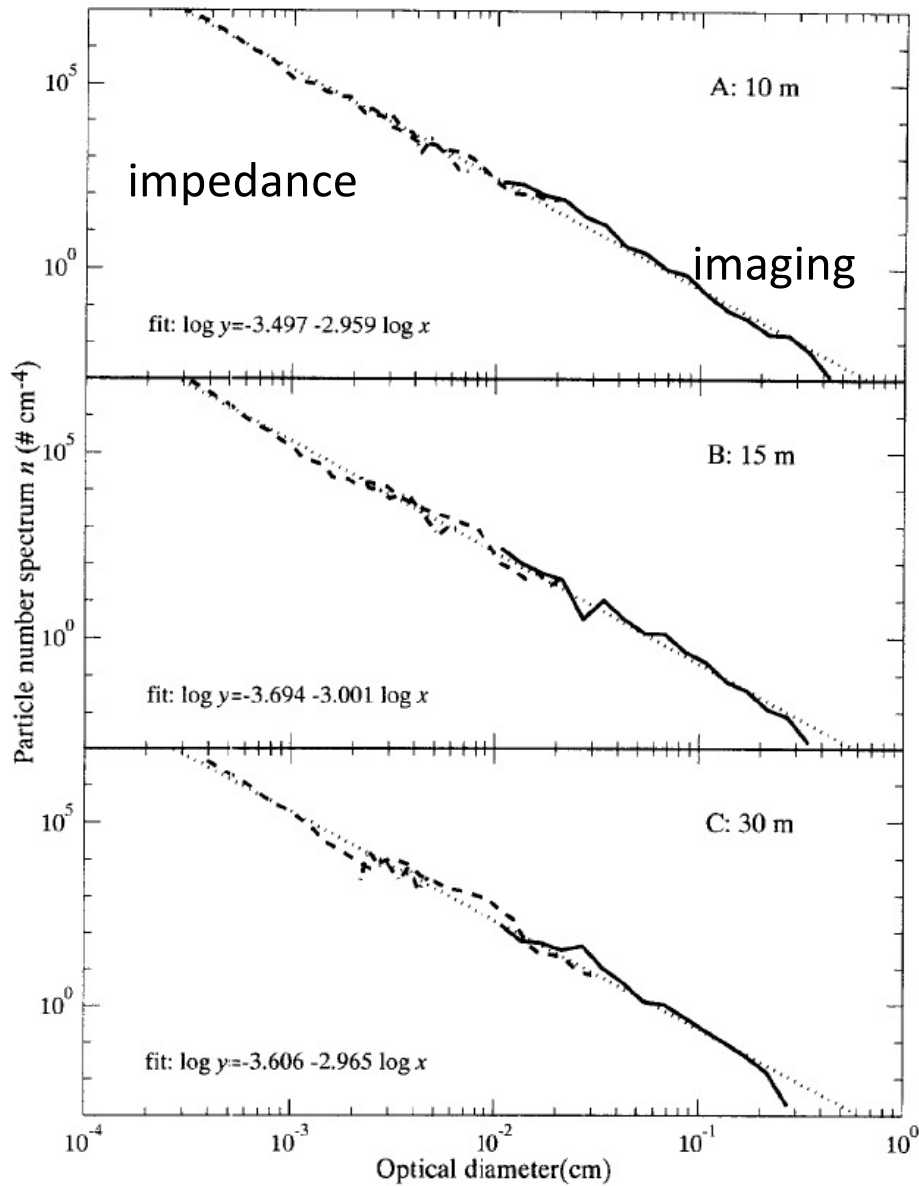
Risovic (1993):

$$f(D) = \begin{cases} 0, & \text{if } D < D_{\min} \text{ or } D > D_{\max}; \\ n_S \left[\frac{D}{D_0} \right]^{\mu_S} \exp(-\tau_S D^{\nu_S}) + n_L \left[\frac{D}{D_0} \right]^{\mu_L} \exp(-\tau_L D^{\nu_L}), & \text{if } D_{\min} \leq D \leq D_{\max} \end{cases} \quad [\# \text{ m}^{-3} \mu\text{m}] \quad (28)$$

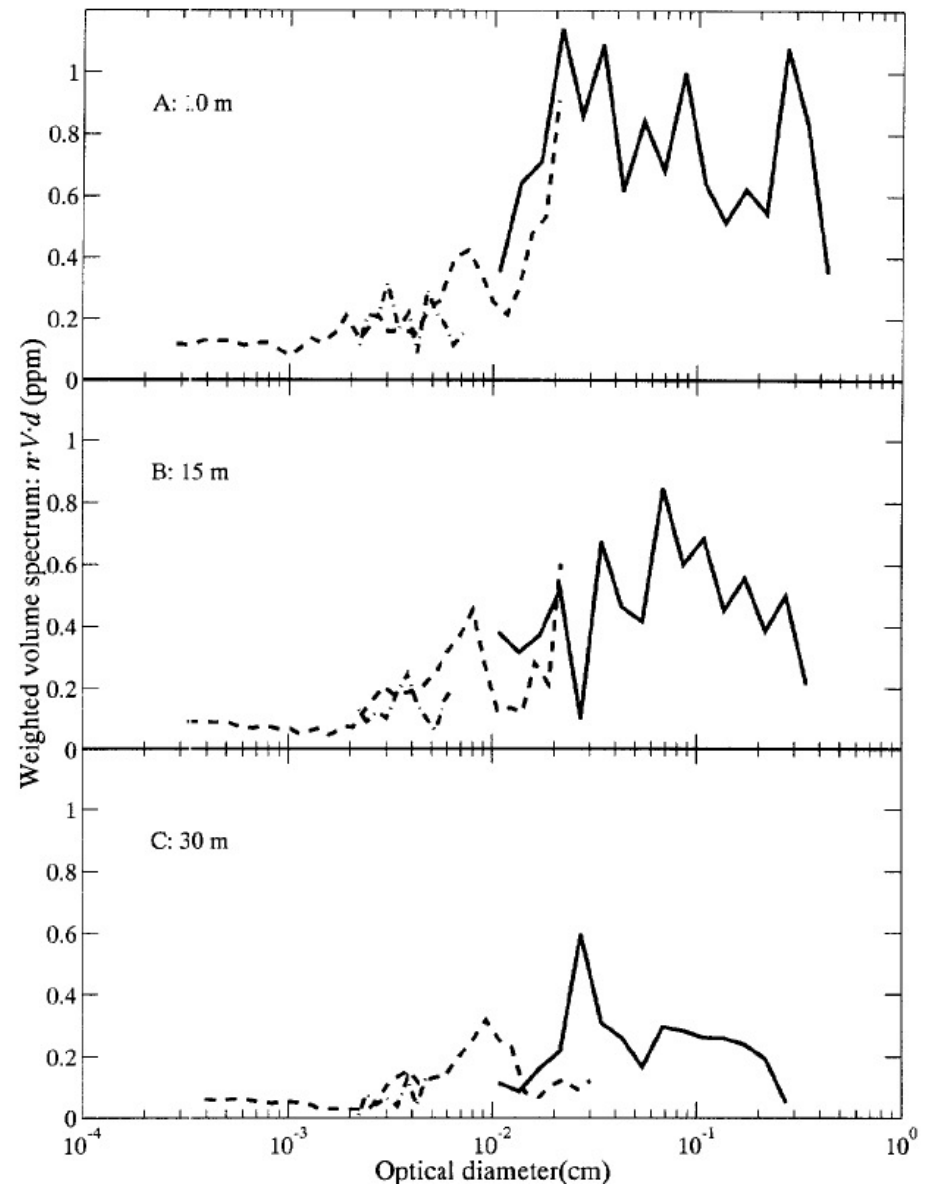


Example of size distribution

Number distribution



Volume distribution (accounting for packing)



Different sizing methods are most 'sensitive' to different sizes.

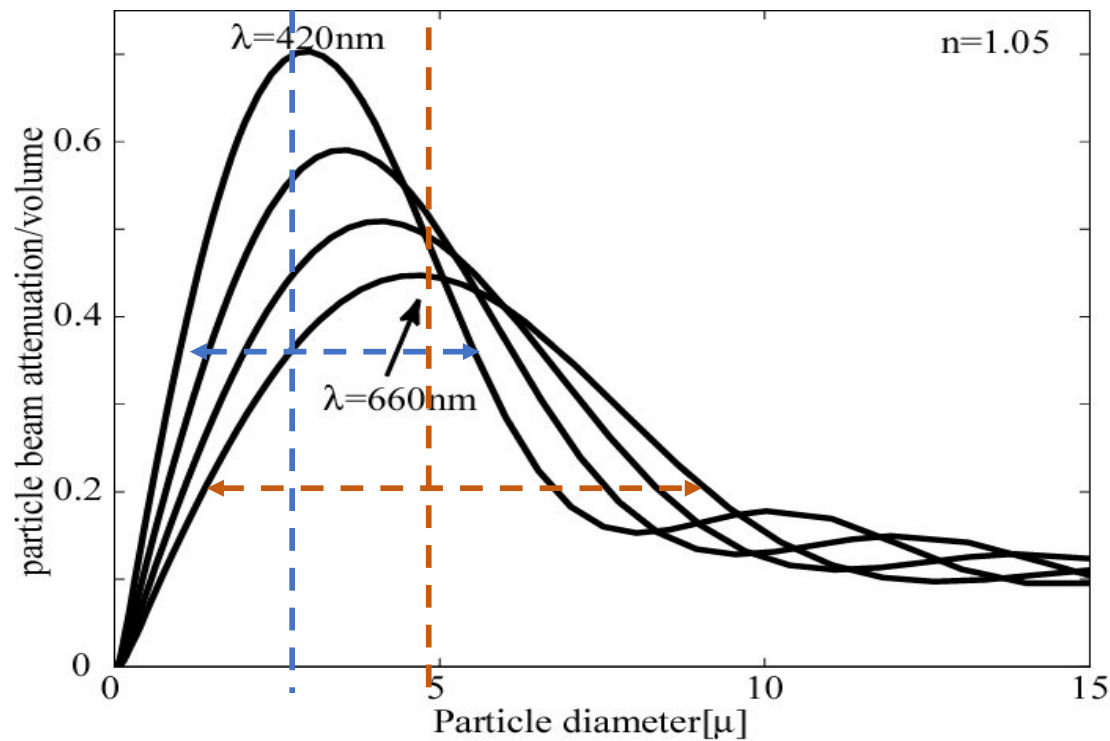
In general, a physical measurement associated with waves (sound, EM) will be most affected by 'inhomogeneities' in the environment which have sizes similar to the wavelength (resonance).

In addition, issues of resolution (e.g. pixel size of a camera) may limit the smallest resolvable size.

Hence, if we want to sense particles of a certain size we need to choose a tool that will be sensitive to that size range.

All methods have problems at both ends due to sensitivity to small particles and rarity of large particles.

$C_{\text{ext}}/\text{volume}$ is sensitive to the wavelength of measurement:



The particle size where the maximum occurs, and the width of the peak, changes between blue to red wavelengths. *Spectral* c_p contains size information!

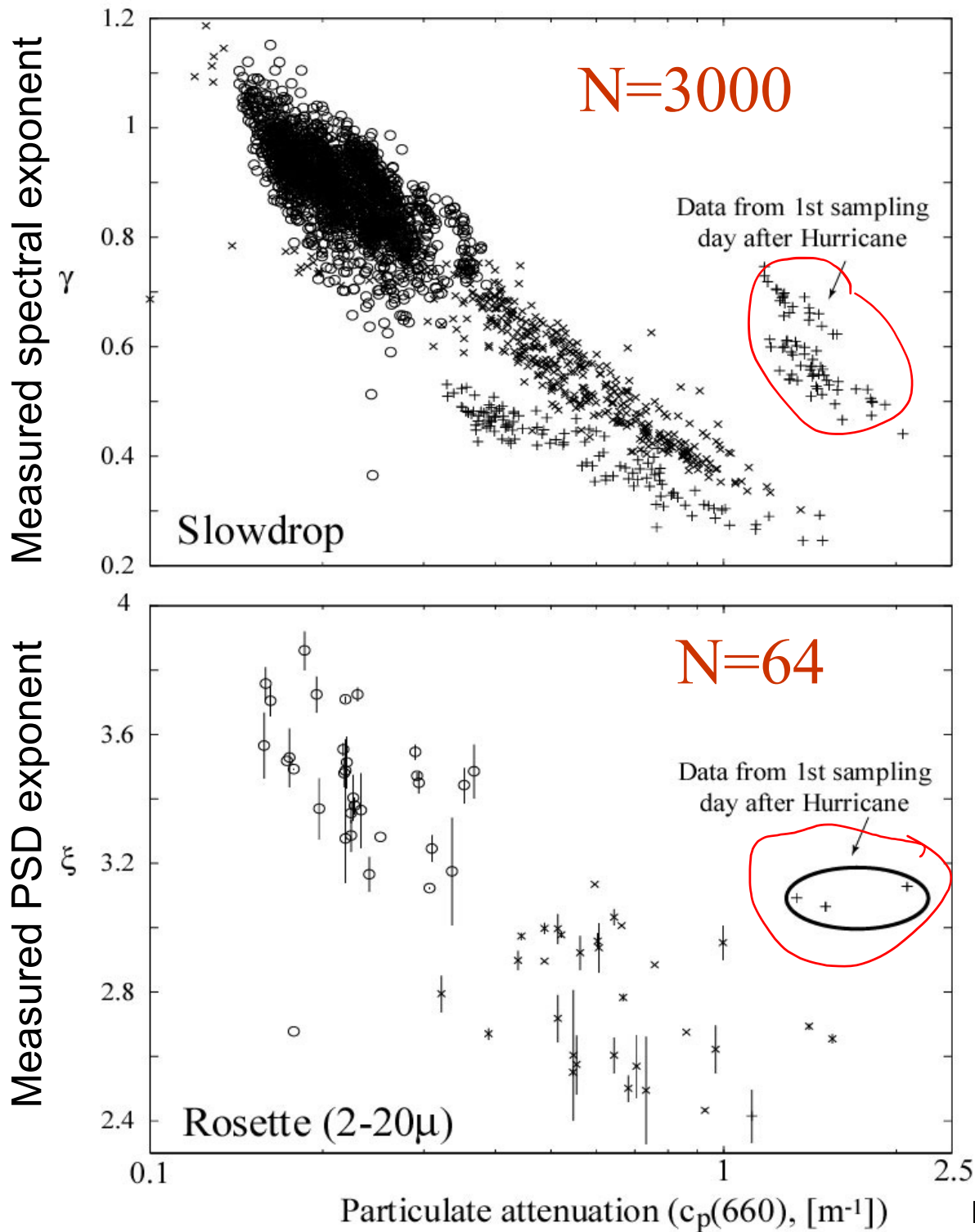
Beam-c and PSD relationship predicted from Mie theory:

Volz (1954): For non-absorbing particles of the same n and a power-law distribution from $D_{\min}=0$ to $D_{\max}=\infty$,

$$N(D) = N_0 (D/D_0)^{-\xi} \quad \leftarrow$$

$$c_p(\lambda) = c_p(\lambda_0) \left(\frac{\lambda}{\lambda_0} \right)^{-\gamma}, \quad \xi = \gamma + 3$$

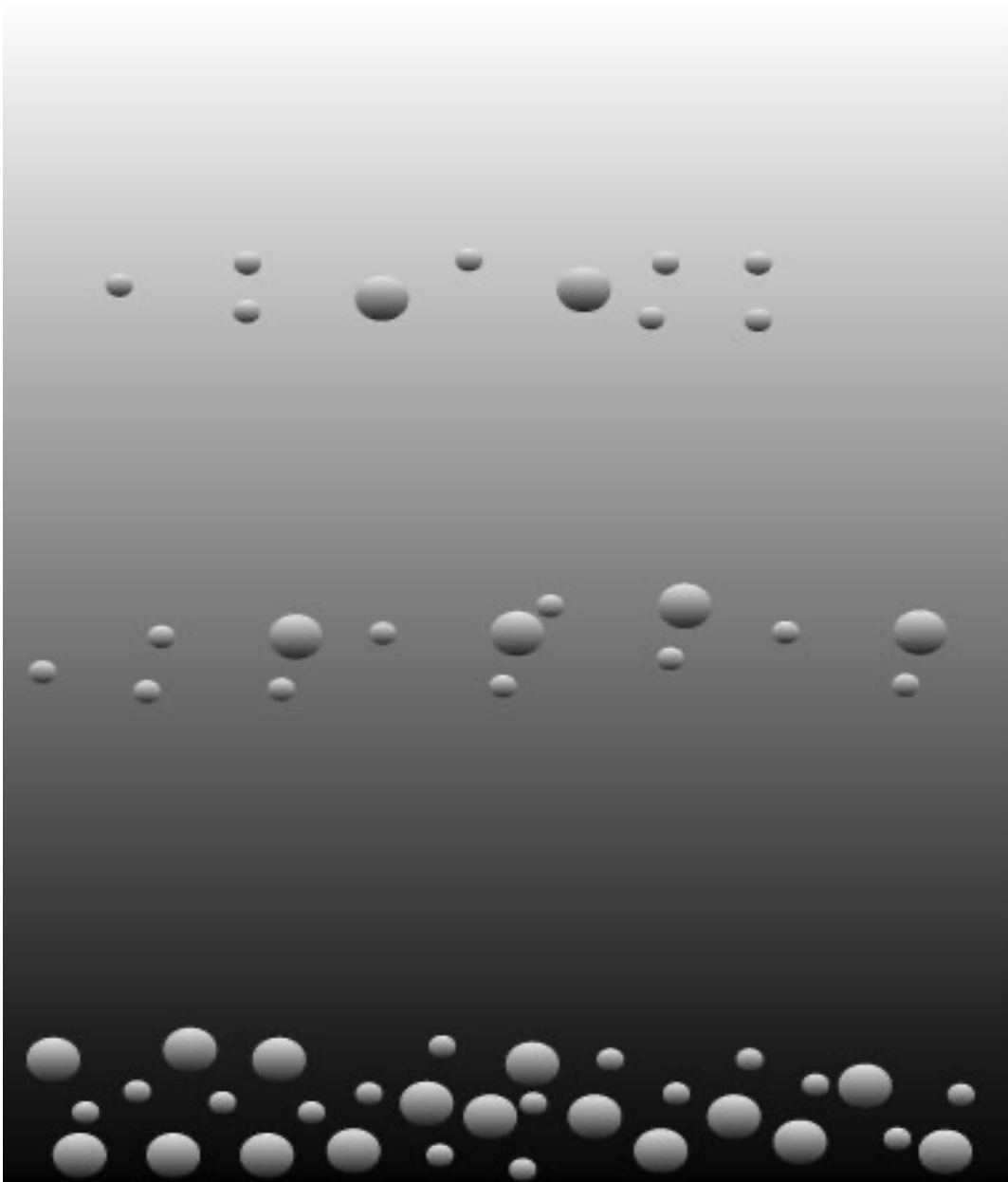
→ expect a relation between attenuation spectrum and PSD.



$\leftarrow c_p(\lambda)$

\leftarrow Coulter counter

Example: particle distribution in the bottom boundary layer



Particle's attenuation increase



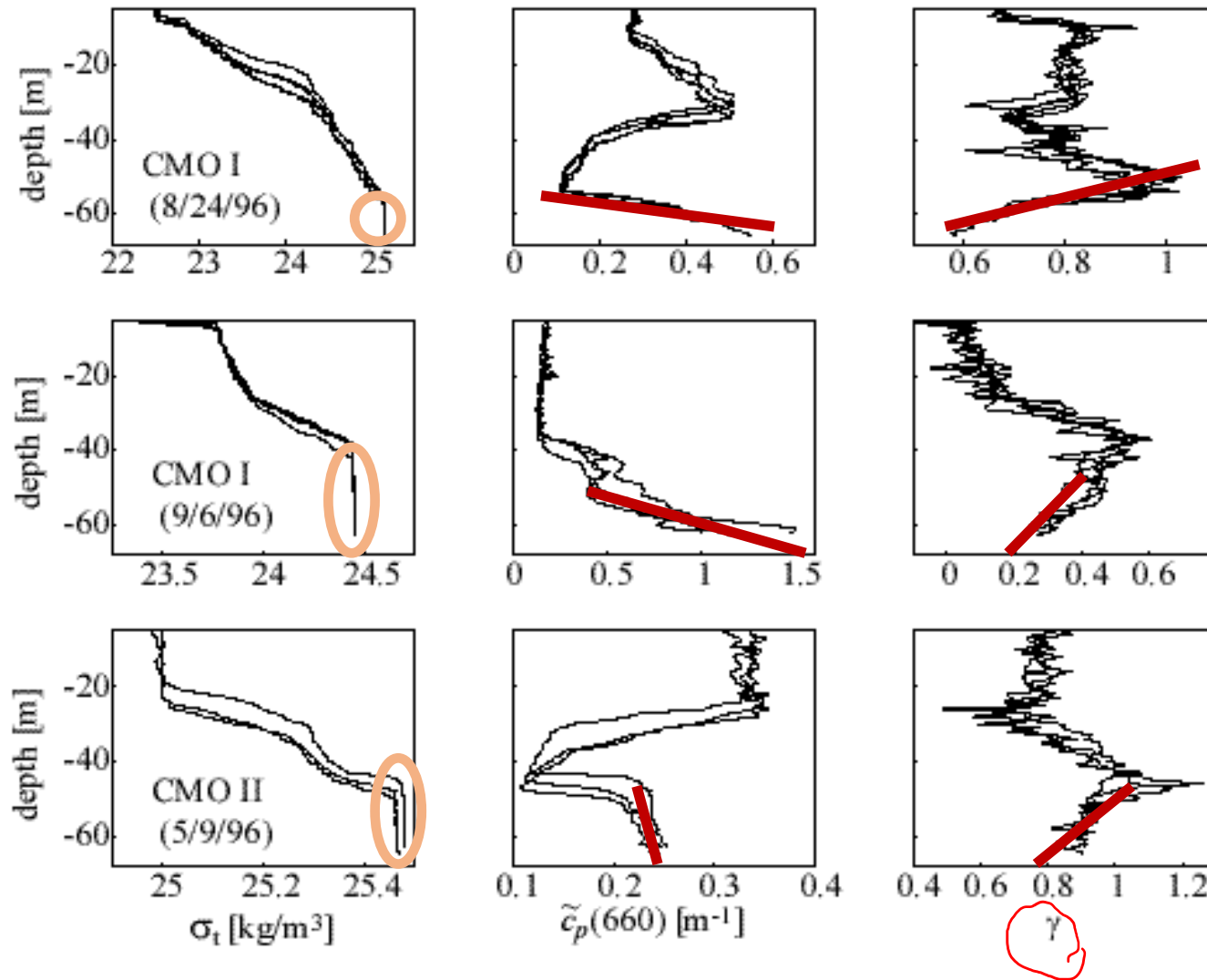
Particle's PSD flattens



Expect:
particle
concentration
and PSD to
change with depth

Why?
Settling is size
dependent

Observations: bottom boundary layer

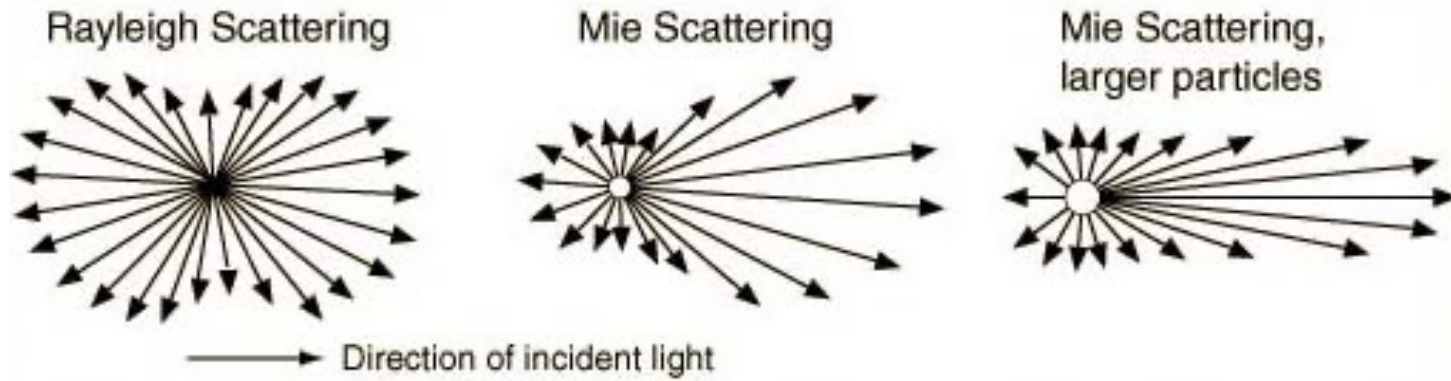


← right after hurricane

← flatter δ

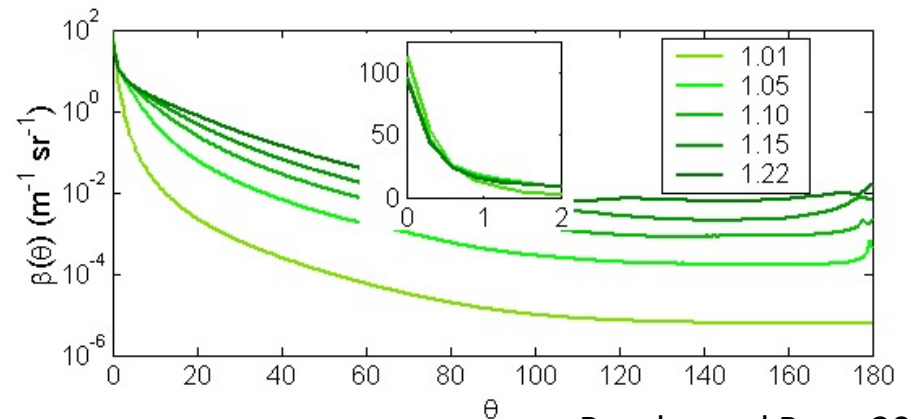
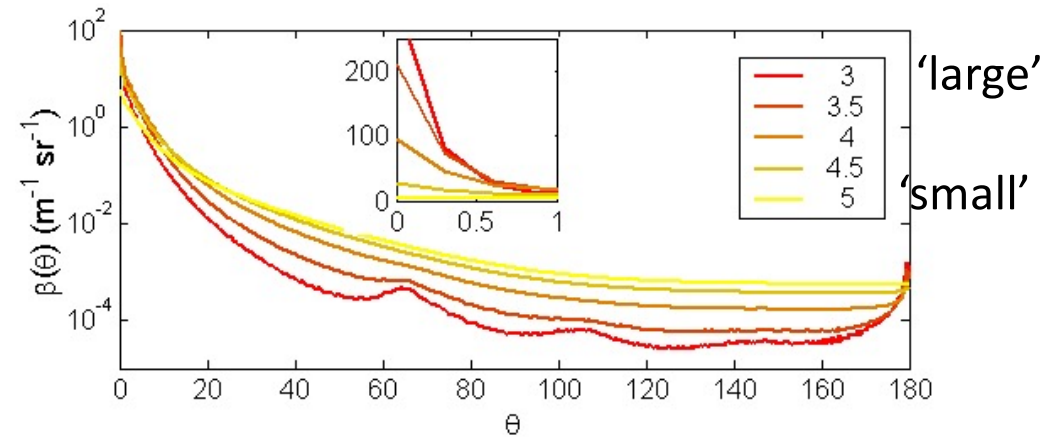
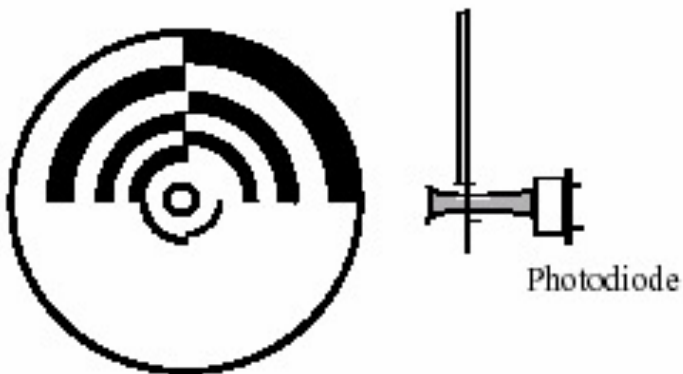
Boss et al., 2001

Angular dependence of scattering on size



- Near forward scattering: Strong dependence on size, less on n .

LISST detector:



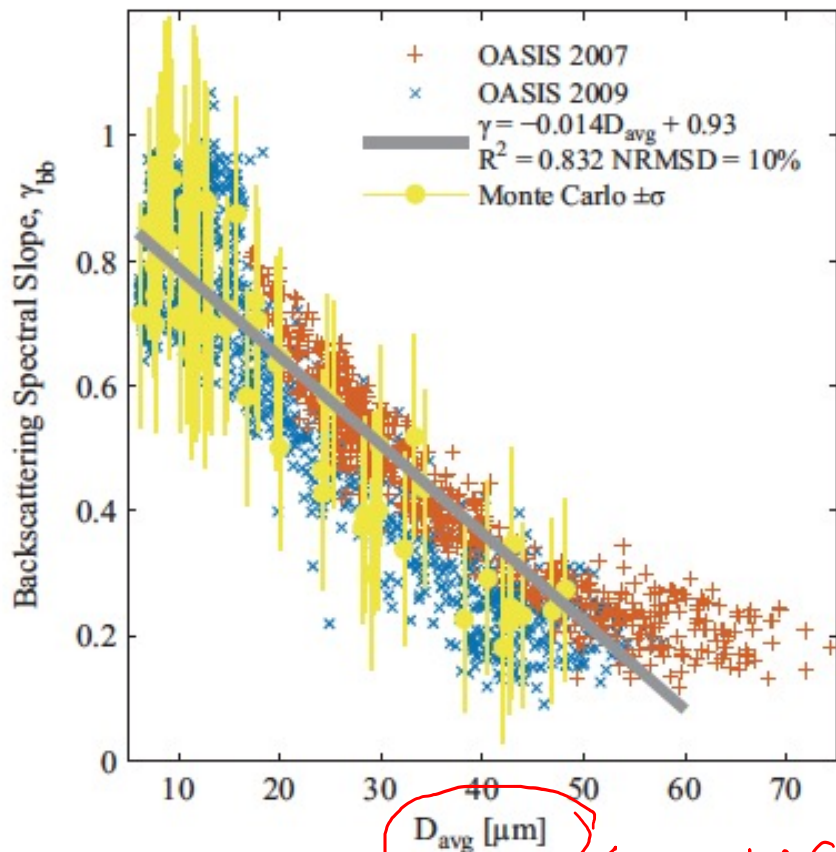
Roesler and Boss, 2008

Closure: LISST vs. IOP spectral slopes

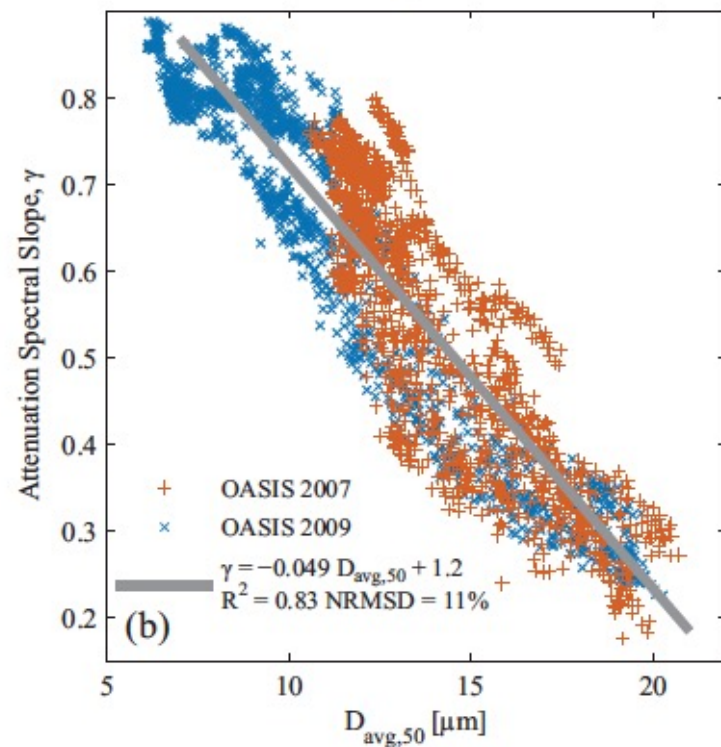
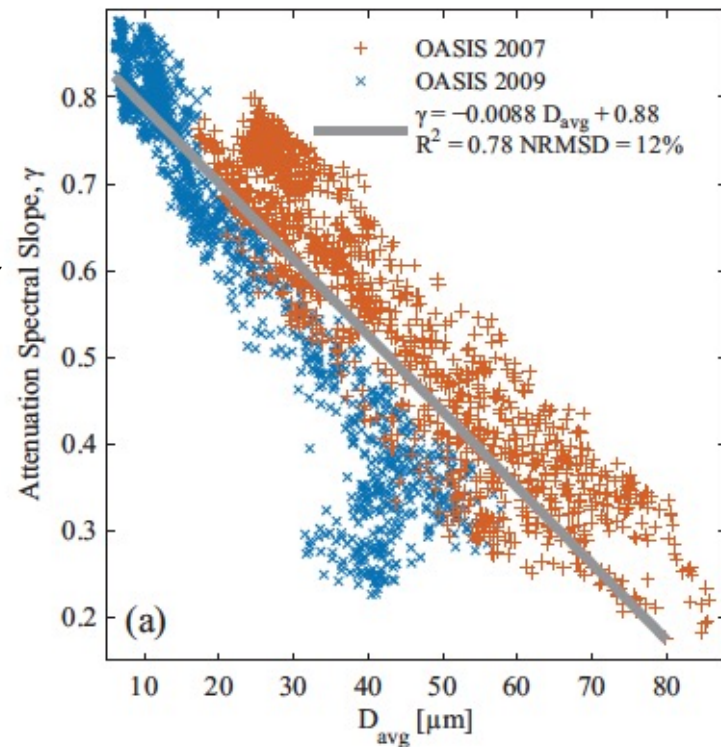
Field data from shelf bottom boundary layer (MVCO)

$$c_p(\lambda) = c_p(\lambda_0) \left(\frac{\lambda}{\lambda_0} \right)^{-\gamma}$$

$$b_{bp}(\lambda) = b_{bp}(\lambda_0) \left(\frac{\lambda}{\lambda_0} \right)^{-\gamma_{bb}}$$



D_{avg} [μm] ← LISST



Is $b_{bp}(\lambda) = b_{bp}(\lambda_0) \left(\frac{\lambda}{\lambda_0}\right)^{-\gamma_{bb}}$ a reasonable model for particles in the surface ocean?

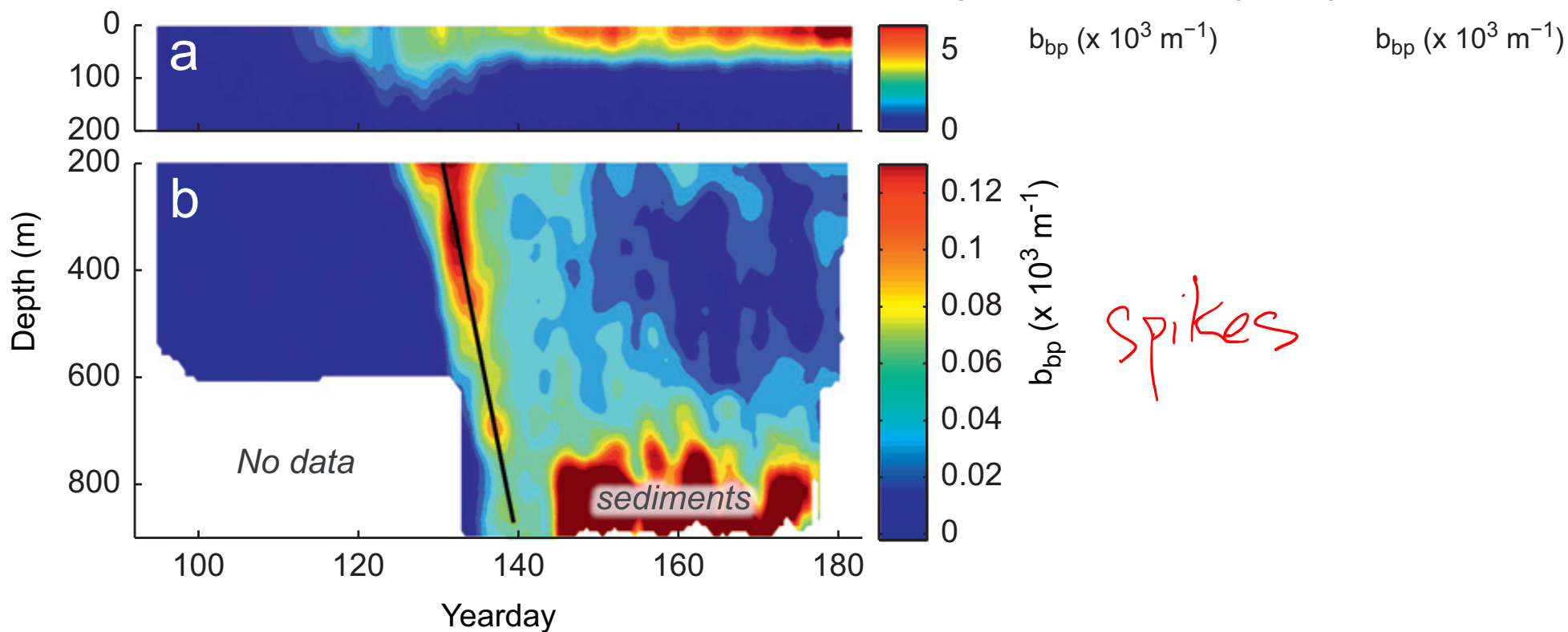
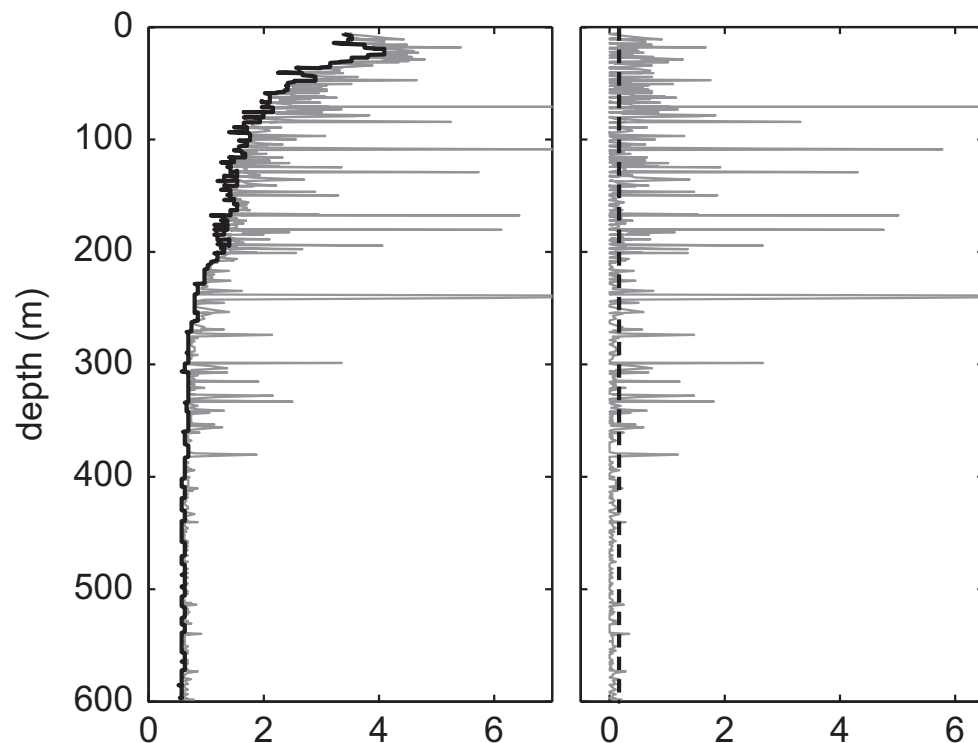
This model serves as the default model in most inversion algorithms.

It is the basis of many PFT inversion models.

However, it has not been validated...

IOP fluctuations = proxy for
particle size?
(Briggs et al., 2011)

Filter to separate “spikes” from “baseline



IOP fluctuation size proxy (Briggs et al., 2013)

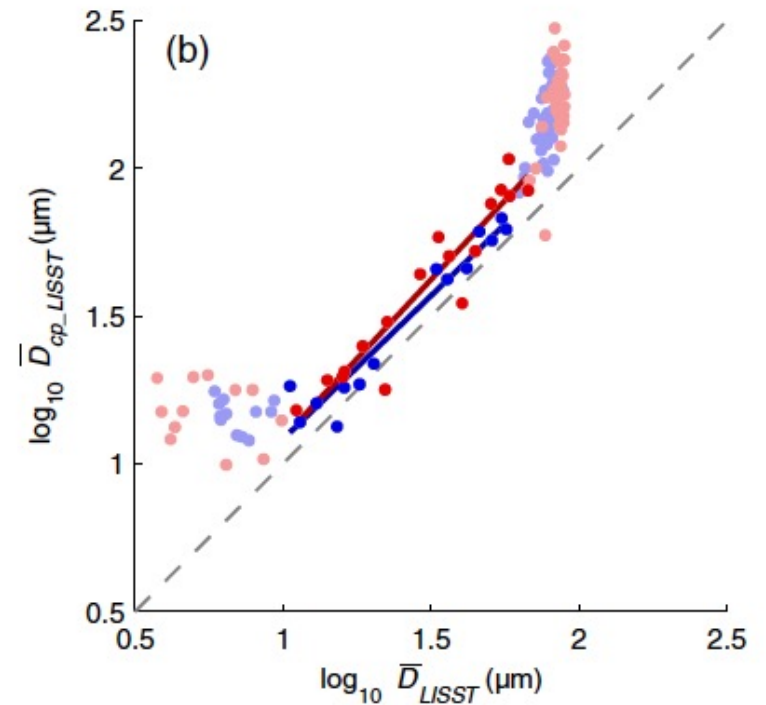
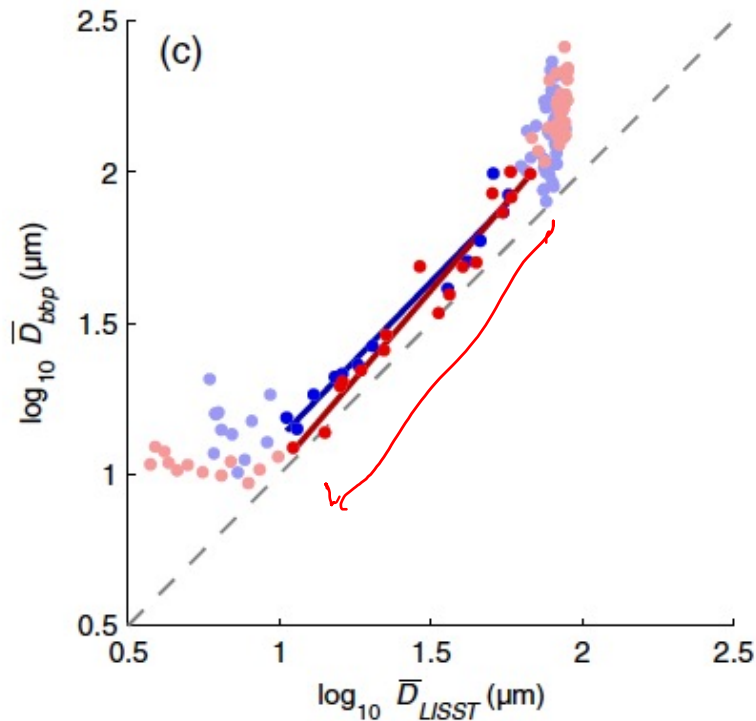
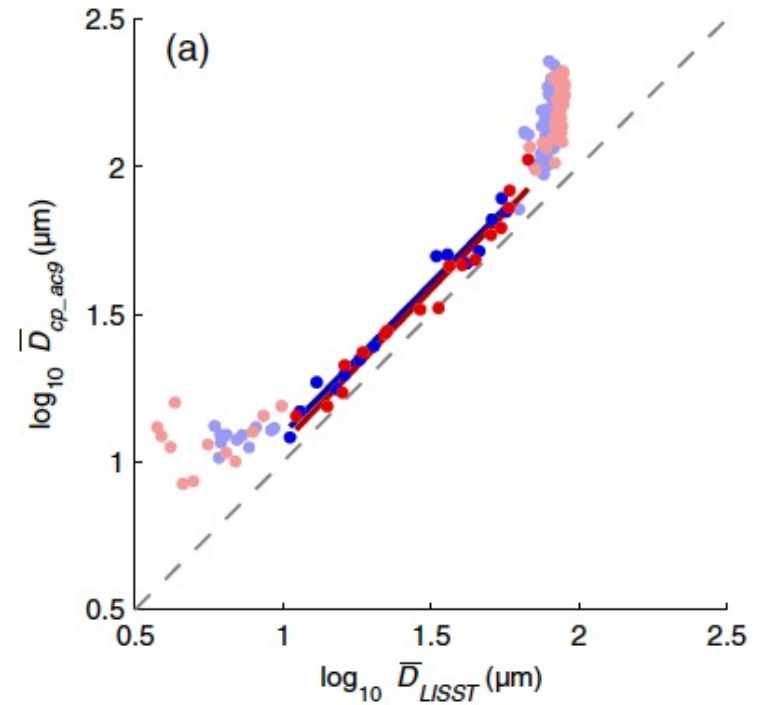
Closure: LISST vs. fluctuations during lab aggregation experiments

V: Sample volume

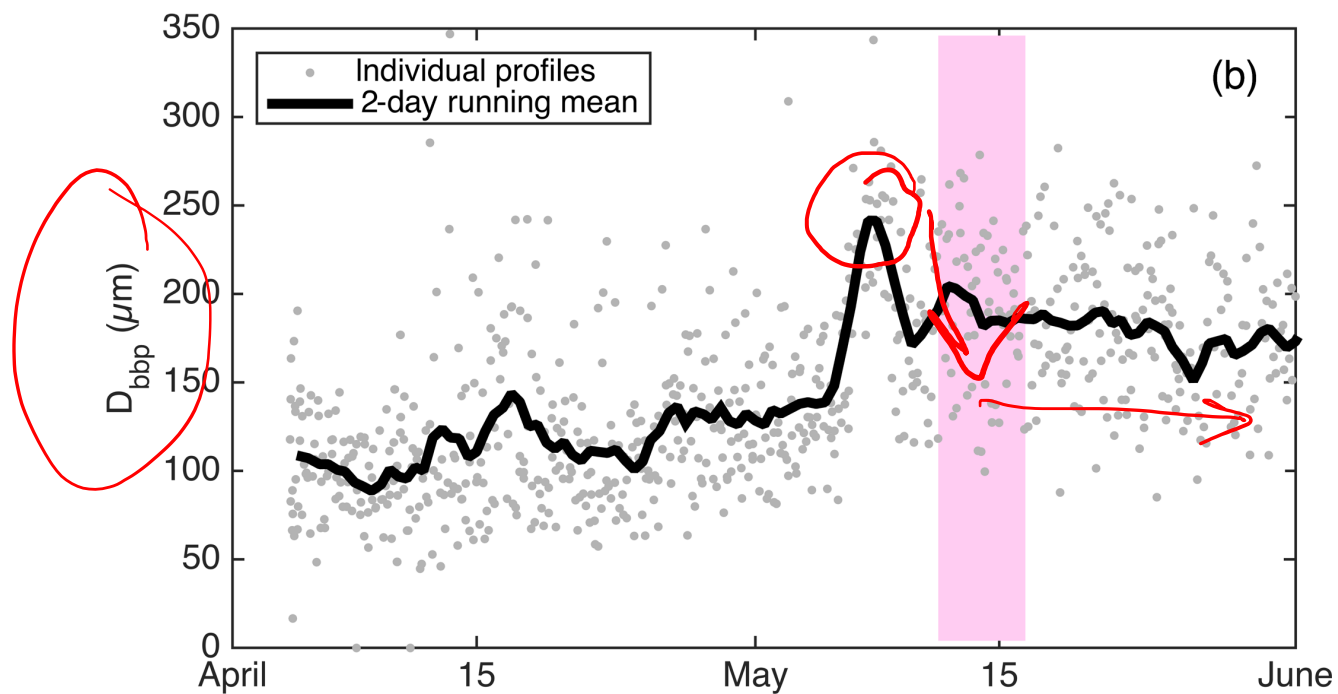
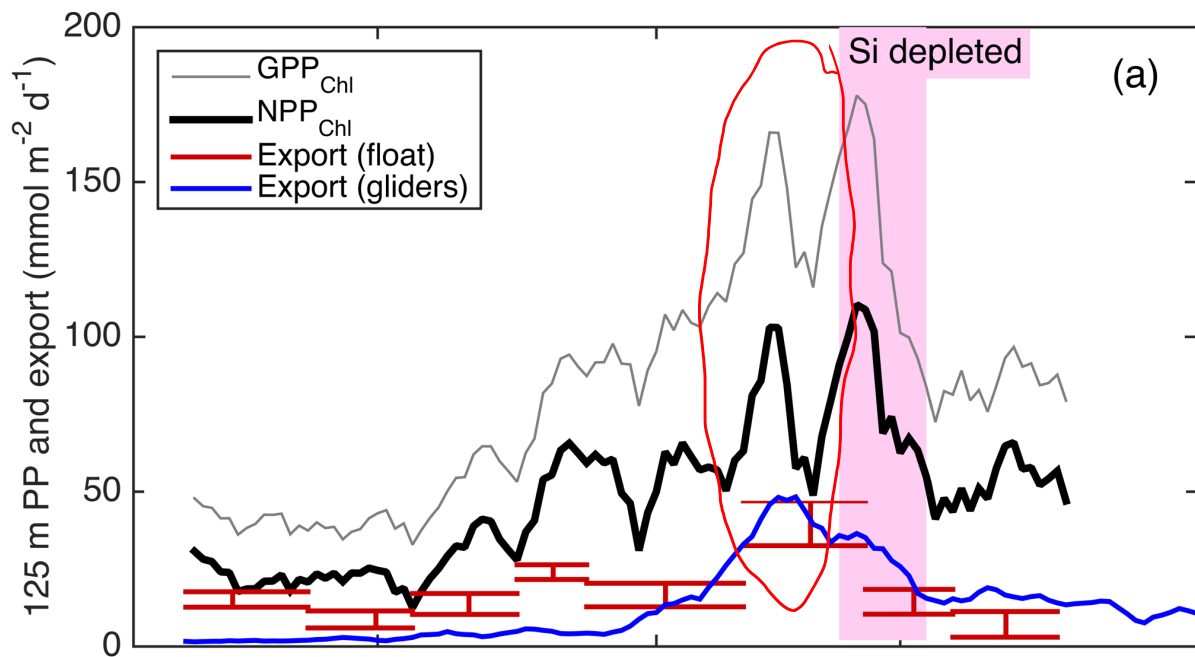
$$\bar{A}_{cp} = \frac{\text{Var}[c_p(t)] V}{E[c_p(t)] Q_c} \frac{1}{\alpha(\tau)}$$

$$\bar{D} = 2\sqrt{\bar{A}\pi^{-1}}$$

α : ratio of residence time to sample integration time



IOP fluctuation size proxy applied to NAB'08 measurements (Briggs et al 2018)



Summary

- Size matters, but it needs to be defined. Given that it varies over orders of magnitude using the diameter of an equivalent sphere may be a reasonable first-order approximation.
- All data looks great on a log-log plot.
- Simple calculus but details are important.
- Optical techniques are useful to constrain size.