## SMS-204: Integrative marine sciences.

## Assignment \#1

Knowledge base: Linking mass, volume and density. Skills: uncertainties, propagation of uncertainties, graphing data, regression, adding error bars to graphs. Computing basic statistical estimators with a spreadsheet.
The assignment can be done by a group. However, each student hands-in individual
homework that is NOT IDENTICAL to other group members. In the case of IDENTICAL homework the grade will be split among the students. A rubric addressinglevel of expertise in treatment of data is provided on the class's web site.

Submit the homework electronically to: sms204.umaine @ gmail.com by next Monday at $12: 10 \mathrm{pm}$. Late homework will suffer an automatic 10 pt penalty for the first week and afterwards will get a grade of zero. Name your homework: lastname_intial_HW\#.doc or .pdf (e.g. Smith_N_HW1.doc for the first homework).

1. A. Compute the volume and densities and their uncertainties for all the rods your group measured. Divide the rods into two groups with similar densities (5pts).

The uncertainty in the scale may be estimated as half the smallest unit reported by the scale. Since the scale measured to 0.01 grams, the uncertainty may be estimated as $+/-0.005 \mathrm{gram}$. If the scale seemed more variable, it may be more honest to report the uncertainty as 0.01 grams.

Because the smallest mark on the ruler was 1 mm , the uncertainty due to the ruler is $+/-0.5 \mathrm{~mm}=+/-0.05 \mathrm{~cm}$.

The uncertainties in volume are based on those for diameter $(D)$ and length $(L)$ :
Below I will assume the uncertainty in the diameter and length to be based on the ruler ( $\mathrm{dL}=0.05 \mathrm{~cm}$ ).

Volume $($ cylinder $)=\pi$ width $^{2} \times$ length $/ 4=\pi D^{2} \times \mathrm{L} / 4$
Using the formula for propagation of errors provided to you in the lab, we can calculate the uncertainty in the volume of a cylinder:
$\rightarrow$ dVolume $=$ Volume $\sqrt{\left(\frac{d L}{L}\right)^{2}+\left(\frac{d D}{D}\right)^{2}+\left(\frac{d D}{D}\right)^{2}}$

Since the mass of each cylinder was different the uncertainty of mass will be different for each cylinder.

For example, for the 2.5 cm long rod, with diameter of 1.3 cm that weighed 3.65 gr :
Uncertainty in volume $=3.32 \sqrt{\left(\frac{0.005}{2.5}\right)^{2}+2\left(\frac{0.005}{1.3}\right)^{2}}=0.19$ cubic cm

Uncertainties in density are computed from those of a ratio:

$$
\begin{aligned}
& \frac{\text { Sdensity }}{}=\text { density } \sqrt{\left(\frac{\text { SVolume }}{\text { Volume }}\right)^{2}+\left(\frac{\text { dmass }}{\text { mass }}\right)^{2}} \\
& \frac{\text { ddensity }}{}=1.13 \sqrt{\left(\frac{0.19}{3.32}\right)^{2}+\left(\frac{0.005}{3.65}\right)^{2}}=0.06 \mathrm{grams}
\end{aligned}
$$

| Rod \# | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Mass (g) | 3.65 | 5.57 | 5.11 | 7.13 | 6.57 | 8.89 | 10.98 | 14.30 |
| Length <br> $(\mathrm{cm})$ | 2.5 | 3.0 | 3.5 | 4.0 | 4.5 | 5.0 | 7.5 | 8.0 |
| Diameter <br> $(\mathrm{cm})$ | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 | 1.3 |
| Dlength <br> $(\mathrm{cm})$ | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 |
| Dmass <br> $(\mathrm{g})$ | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 |
| Volume <br> $\left(\mathrm{cm}^{3}\right)$ | 3.32 | 3.98 | 4.65 | 5.31 | 5.97 | 6.64 | 9.95 | 10.62 |
| Dvolume <br> $\left(\mathrm{cm}^{3}\right)$ | 0.19 | 0.23 | 0.26 | 0.30 | 0.33 | 0.37 | 0.55 | 0.58 |
| Density <br> $\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ | 1.10 | 1.35 | 1.10 | 1.34 | 1.10 | 1.34 | 1.10 | 1.35 |
| Ddensity <br> $\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ | 0.06 | 0.08 | 0.06 | 0.07 | 0.06 | 0.07 | 0.06 | 0.07 |

Table 1. Rod measured and derived data. Highlighted data represents a group of rods with different density than those that are not highlighted
The rods you analyzed where of two densities, about $1.13 \mathrm{~g} / \mathrm{cm}^{3}$ and about $1.39 \mathrm{~g} / \mathrm{cm}^{3}$ (however, results close to these will be given credit). Given the above uncertainties we should easily be able to differentiate the two groups of rods. The 2.5, 3.5, 4.5, and 7.5 cm rods have lower densities.
B. Plot the mass as a function of volume for these two groups. Use your experience from previous classes to make a good plot (one that has: labels for each axis which includes units, tick marks on axis and a symbol to denote each datum with no line connecting them and no grid lines) (10pts).


Figure 1. Rod mass as function of volume. Error bars indicate uncertainties in the measurements. The uncertainties in mass are too small to show. The lines are the linear regression fit to the two different groups of rod of similar density.

Note: it may be easier for you to separate the two groups of similar density rods into separate graphs. That is OK.
C. For both groups of rods, obtain the linear regression line between Mass and volume, a (this can be done by right clicking the data points in Excel, see links below). ( 5 pts )

## See Figure 1.

D. Display the equation and the line on the graph. You should get an equation of the type: Mass $=A \times$ Volume $+B$. (5pts)

See Figure 1.
E. Does there seem to be a linear relationship between Volume and Mass? (5pts)

Yes. Mass is linearly correlated with volume and a straight line fits well with the data.
F. What does the slope of the regression line represents ( $A$ in the equation in question 1D) (5pts)? What are its units ( 5 pts )?

The slope represents the density=mass/volume. Units are $[\mathrm{g} / \mathrm{ml}]$ or $\left[\mathrm{g} / \mathrm{cm}^{3}\right]$.
G. What are the units of the intercept ( $B$ in the equation in question 1 D ) ( 5 pts )?

Unit is [g] as the equation is one for mass.
I. Add uncertainties (in the form of error bars, see links below) to your plot (5pts).

## See Figure 1.

J. Explain how the uncertainties were computed (5pts).

Uncertainties in mass were assumed constant based on the rounding of values provided in the table, e.g.+/-0.005g. Uncertainties in volume are based on propagating error associated with measurements of length and width. I assumed we measured width and length with ruler had the same uncertainty (+/-0.05cm) and propagated using:

$$
\frac{\delta \text { Volume }}{\text { Volume }}=\sqrt{\left(\frac{\delta H}{H}\right)^{2}+2\left(\frac{\delta D}{D}\right)^{2}} .
$$

2.A Using an Excel spreadsheet (or another program of your choice) and the data your whole class collected on sinking speeds of different beads, compute for each bead the mean, median, maximum, minimum, $16^{\text {th }}$ percentile, $84^{\text {th }}$ percentile, and the standard deviation of the sinking speed for that bead (10pts, those program have built-in function to compute these, to learn how to use them, for example google 'how to compute percentile with excel' + some tutorial on YouTube will walk you through it).

|  | sinking <br> speed of <br> bead size <br> $1(\mathrm{~cm} / \mathrm{s})$ | sinking <br> speed of <br> bead size <br> (cm/s) | sinking <br> speed of <br> bead size <br> $3(\mathrm{~cm} / \mathrm{s})$ | sinking <br> speed of <br> bead size <br> $4(\mathrm{~cm} / \mathrm{s})$ | sinking <br> speed of <br> bead size 5 <br> $(\mathrm{cm} / \mathrm{s})$ |
| ---: | ---: | ---: | ---: | ---: | :--- |
| 1 | 2.44 | 5.12 | 8.87 | 17.40 | 27.40 |
| 1 | 2.45 | 5.08 | 8.77 | 16.90 | 27.00 |
| 1 | 2.40 | 5.35 | 9.01 | 17.20 | 28.80 |
| 2 | 2.42 | 5.29 | 8.94 | 18.63 | 31.15 |
| 2 | 2.38 | 5.22 | 9.13 | 18.45 | 28.36 |
| 2 | 2.37 | 5.20 | 9.20 | 19.59 | 39.01 |
| 3 | 2.50 | 5.30 | 9.00 | 19.20 | 31.40 |
| 3 | 2.49 | 5.20 | 9.10 | 17.50 | 34.20 |
| 3 | 2.47 | 5.20 | 9.10 | 18.60 | 29.70 |
| 4 | 3.00 | 5.00 | 9.00 | 19.00 | 28.00 |
| 4 | 3.00 | 5.00 | 9.00 | 17.00 | 28.00 |
| 4 | 3.00 | 5.00 | 9.00 | 17.00 | 28.00 |
| 5 | 2.55 | 5.43 | 9.18 | 18.45 | 27.88 |
| 5 | 2.57 | 5.34 | 8.85 | 18.25 | 28.30 |
| 5 | 2.50 | 5.31 | 9.55 | 18.25 | 27.88 |
| 6 | 2.60 | 5.50 | 9.60 | 17.40 | 28.30 |
| 6 | 2.60 | 5.40 | 9.50 | 18.30 | 27.30 |


| 6 | 2.60 | 5.50 | 9.20 | 18.30 | 27.10 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | 2.50 | 5.25 | 8.71 | 18.90 | 26.70 |
| 7 | 2.46 | 5.32 | 8.79 | 17.80 | 29.30 |
| 7 | 2.47 | 5.30 | 9.23 | 18.40 | 26.70 |
| 8 | 2.54 | 5.64 | 8.57 | 18.33 | 30.64 |
| 8 | 2.60 | 5.33 | 9.16 | 14.08 | 27.75 |
| 8 | 2.57 | 5.47 | 9.25 | 19.15 | 25.53 |
| 9 | 2.51 | 5.36 | 9.27 | 18.82 | 28.51 |
| 9 | 2.51 | 5.43 | 9.12 | 18.82 | 28.30 |
| 9 | 2.55 | 5.36 | 8.93 | 18.54 | 29.16 |
| 10 | 2.51 | 5.34 | 9.12 | 16.98 | 29.16 |
| 10 | 2.53 | 5.27 | 9.12 | 19.39 | 28.51 |
| 10 | 2.52 | 5.34 | 9.18 | 18.28 | 26.29 |
| 11 | 2.39 | 5.22 | 9.36 | 19.29 | 32.20 |
| 11 | 2.52 | 5.26 | 9.34 | 18.72 | 25.33 |
| 11 | 2.47 | 5.24 | 9.07 | 17.60 | 28.79 |
| 12 | 2.49 | 5.49 | 9.16 | 17.10 | 26.90 |
| 12 | 2.50 | 5.34 | 9.23 | 17.70 | 26.10 |
| 12 | 2.52 | 5.34 | 8.99 | 17.40 | 27.80 |
| 13 | 2.48 | 5.44 | 9.16 | 19.15 | 27.96 |
| 13 | 2.50 | 5.35 | 9.14 | 18.87 | 29.24 |
| 13 | 2.47 | 5.35 | 9.21 | 18.33 | 28.58 |
| 14 | 2.63 | 5.61 | 9.72 | 19.36 | 29.55 |
| 14 | 2.56 | 5.61 | 9.42 | 19.95 | 30.00 |
| 14 | 2.60 | 5.58 | 9.68 | 19.95 | 30.00 |
| average speed [cm/s] | 2.54 | 5.33 | 9.14 | 18.25 | 28.73 |
| median speed [ $\mathrm{cm} / \mathrm{s}$ ] | 2.51 | 5.34 | 9.14 | 18.36 | 28.30 |
| standard deviation [cm/s] | 0.14 | 0.16 | 0.25 | 1.06 | 2.38 |
| maximum [ $\mathrm{cm} / \mathrm{s}$ ] | 3.00 | 5.64 | 9.72 | 19.95 | 39.01 |
| minimum [cm/s] | 2.37 | 5.00 | 8.57 | 14.08 | 25.33 |
| 16 percentile | 2.46 | 5.20 | 8.94 | 17.31 | 26.96 |
| 84 percentile | 2.60 | 5.48 | 9.35 | 19.17 | 30.00 |
| (84\%-16\%)/2 | 0.07 | 0.14 | 0.21 | 0.93 | 1.52 |

B. How do the median and mean compare? How does the standard deviation compare to ( $84^{\text {th }}$ percentile- $16^{\text {th }}$ percentile) $/ 2$ ? We expect them to be similar for a normal distribution (5pts).
They are similar varying from $\sim 3-8 \%$ of the median values. Hence the underlying statistical distributions of settling velocities are probably not very different from normal.
C. Plot the median sinking speed of the beads ( $y$ or vertical-axis) as function of their cross-sectional area $\left(=\pi \times\right.$ radius $^{2}$ ) ( $x$ or horizontal axis). (10pts)


Figure 2. Settling velocity as function of cross-sectional area for beads.
D. Does there seem to be a relationship between cross-sectional area and median sinking speed (determine a relationship by plotting the regression line and displaying its equation on the plot)? Note: When the bead reaches terminal velocity, a balance exists between the downward pool of gravity and the drag force. We will get back to these data later in the semester when we will analyze the forces acting on bodies immersed in water. (5pts)

There is a monotonic relationship though a concave curve could match data better.
E. Add the uncertainties of the data points to the graph (these are called 'error bars', see links below). Use the statistics from the whole class dataset for uncertainties. What do such uncertainties represent? How do they compare to uncertainties in individual measurements of sinking speed? (5pts)

The uncertainties represent the measurement uncertainties associated with many different students measuring independently the same phenomenon. They are typically much larger than uncertainties based on an individual's measurements.
3. (15pts): What are ALL the curious phenomena related to drag that are demonstrated in the movie "Fluid dynamics of drag, part I" (find the link to on-line movie on class web site. If you have any problem viewing the movie we can set up a computer for you)?
The curious phenomena related to drag that were demonstrated in the movie are:

1. Sometimes an increase in speed can cause a decrease in drag on an object.
2. Through one range of speeds a smooth ball can have more drag than a rough ball, while through another range of speeds the rough ball has less drag.
3. Under certain conditions, streamlining can reduce drag, while in other conditions, streamlining increases drag.

## Resources that may be useful for this homework:

A few links on how to plot a graph with Microsoft Excel (found using Google with 'making graphs with excel 2007' in the subject line)
http://spreadsheets.about.com/od/excelcharts/ss/line_graph.htm
http://www.youtube.com/watch? $\mathrm{v}=8 \mathrm{~B} 8 \mathrm{kFVNzlQ} 8$

How to plot error bars on a graph in excel
http://www.youtube.com/watch?v=90zGaV0KLuk
http://www.youtube.com/watch?v=gmdeYI1DqLs

How to plot a good graph:
http://misterguch.brinkster.net/graph.html
http://chemsite.lsrhs.net/tutorials/good_graphs.pdf

More on how to propagate uncertainties:
http://www.rit.edu/cos/uphysics/uncertainties/Uncertainties.html
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