Analysis of backscattering using the ADV:

The sonar equation can be written for the case of the ADV as:

$$EL = C_2 \cdot counts = C_1 - 2R\alpha_p^*[conc] + 10\log_{10}(C_3b_p^*[conc] + b_{background})$$

Where we read *counts* of the machine,  $C_j$  are constants, star quantities denote mass specific attenuation and backscattering and  $b_{background}$  is the backscattering in the blank reference material, *[conc]* is the concentration of beads.

We can obtain  $C_1$  by running the instrument without obtaining any backscattering, e.g. into a large room far from boundaries. In this case we measure ~61counts ([conc]=0).

$$\rightarrow C_1 = C_2 \cdot 61$$

Before we put our sample in water we measure the background which is nonzero due to bubble or dirt in the water:

$$\Rightarrow b_{background} = 10^{\{(C_2 \cdot counts - C_1)/10\}}.$$

We can rewrite the sonar equation in terms of 3 unknowns  $(x_i)$ :

counts = 
$$61 - 2Rx_1[conc] + \frac{1}{x_2} 10\log_{10}(x_3[conc] + b_{background}).$$

It is apparent that we cannot obtain the specific backscattering coefficient but within a constant,  $C_3$ , unless we perform prior to our measurements a calibration using beads on known acoustical properties.

When performing a least squares fit of the last equation it is readily apparent that  $b_{background}$  has negligible influence on the  $x_j$ .