

# Phytoplankton community composition derived from optics and remote sensing: Approaches, challenges, and next steps

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Ocean Optics Summer Course – 5 July 2023, Bowdoin College, ME

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Slide content inspired by and with info from Jeremy Werdell (NASA), Julia Uitz (LOV), Patrick Gray (UMaine), & many colleagues and papers (see references at the end)

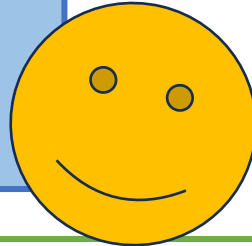
# Week 4 roadmap

Monday: Monte Carlo techniques  
(lecture/interactive demonstration)

Tuesday: Calibrating bb sensors

Wednesday: Remote sensing of  
zooplankton

Wednesday: Phytoplankton  
community and particle size  
inversion from remote sensing



Mon: Arduino lab

Tuesday late afternoon discussion:  
Scientific ethics and being part of a  
community

Wednesday after dinner discussion:  
Career panel with instructors

All week: continue working on  
projects

Friday: Final presentations of projects

# Who am I?



Overarching research goal: How are phytoplankton communities distributed in space and time? At various scales, what changes are occurring in these communities and their distributions?

- use optical measurements to estimate parameters related to phytoplankton
- application to remote sensing data for broad scale ocean ecosystem studies

# What comes to mind when you hear "Phytoplankton Community Composition"?

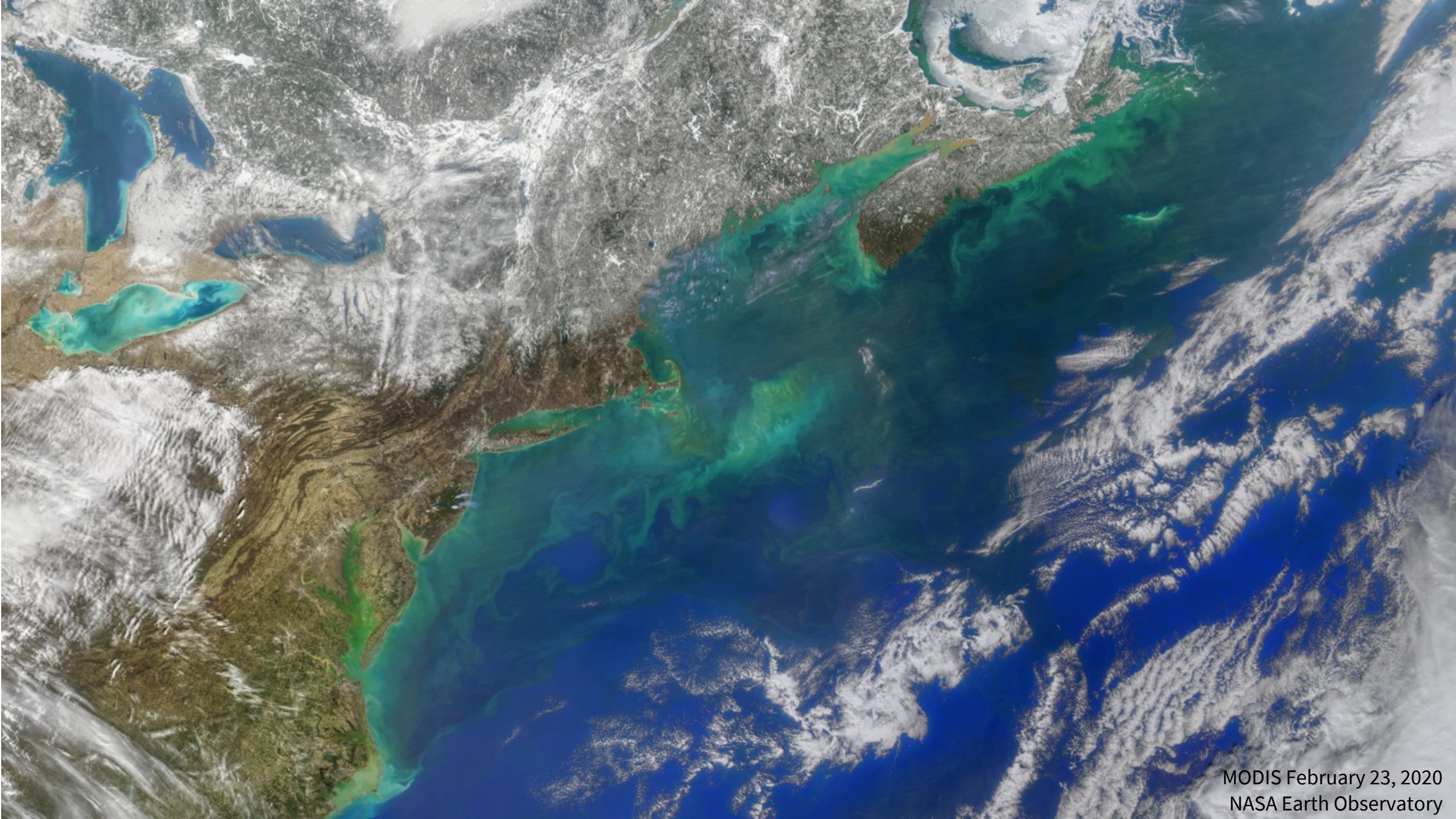




# What comes to mind when you hear "Phytoplankton Community Composition"?

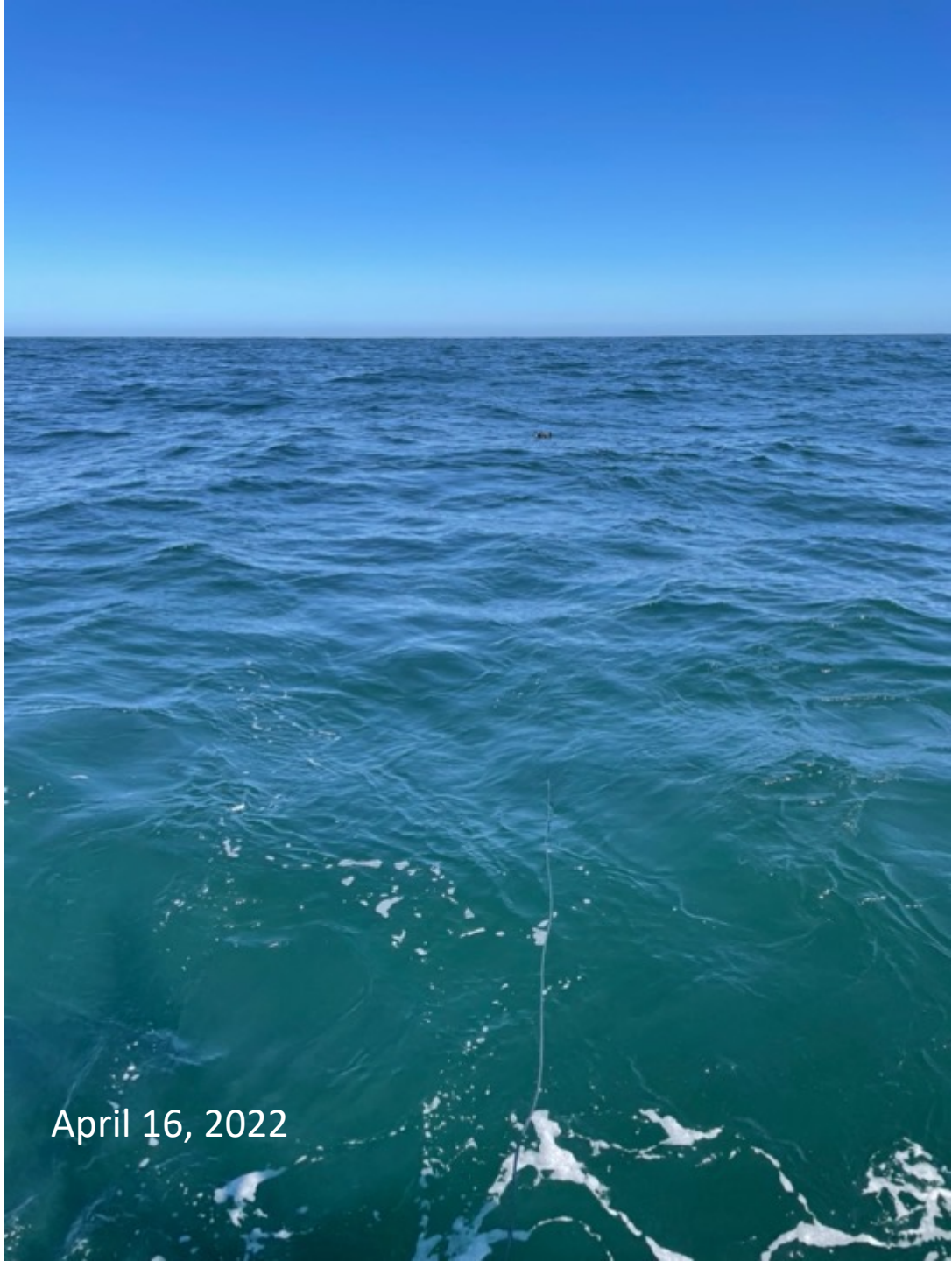




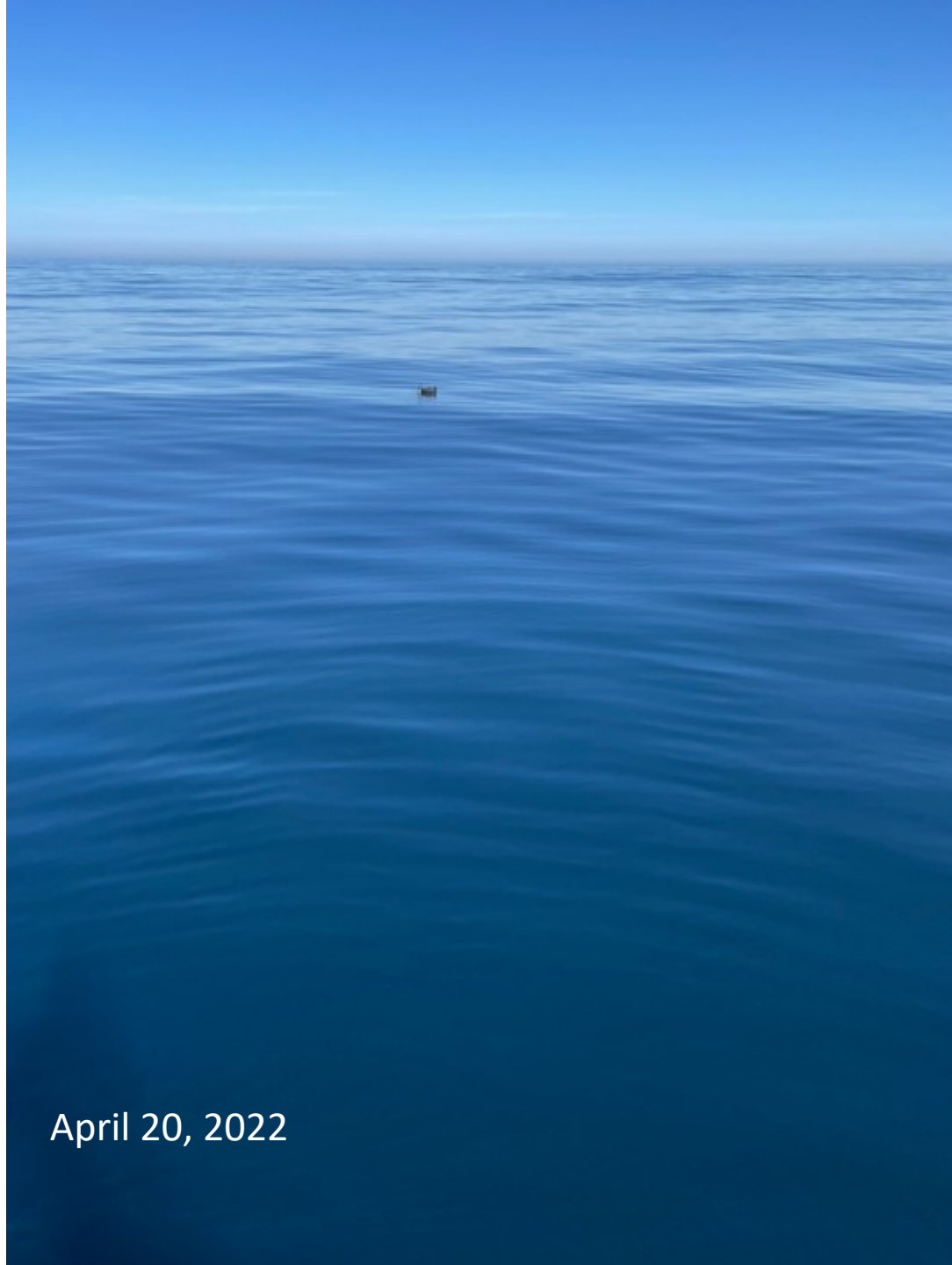


MODIS February 23, 2020  
NASA Earth Observatory





April 16, 2022



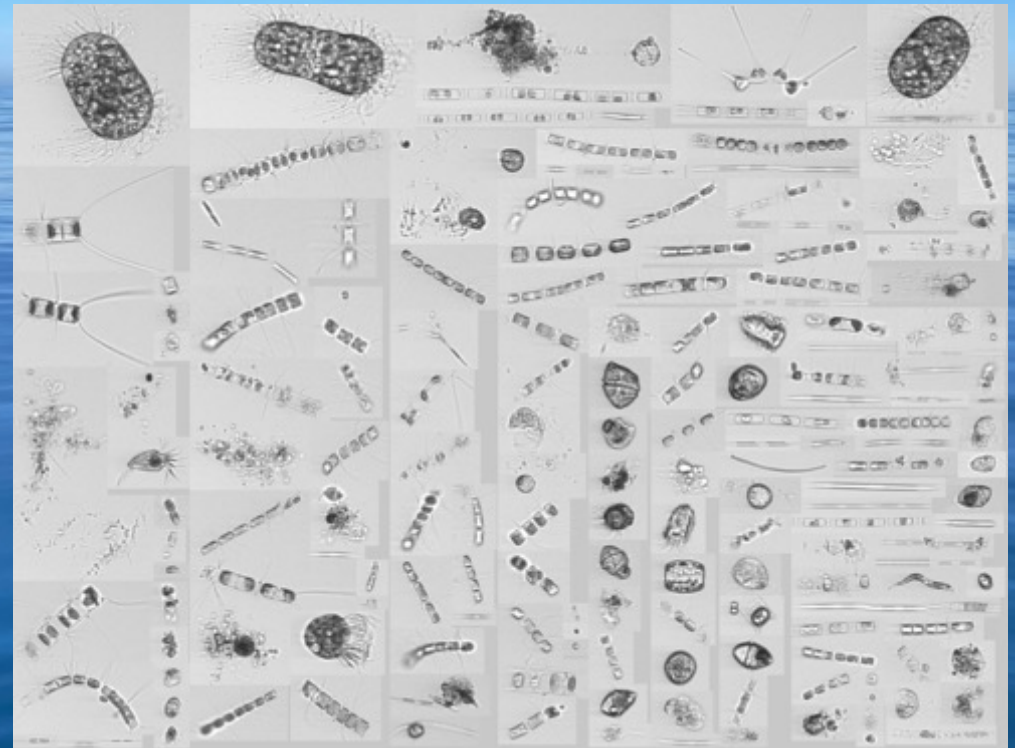
April 20, 2022

~3,000 ROIs/ml



April 16, 2022

~500 ROIs/ml



April 20, 2022



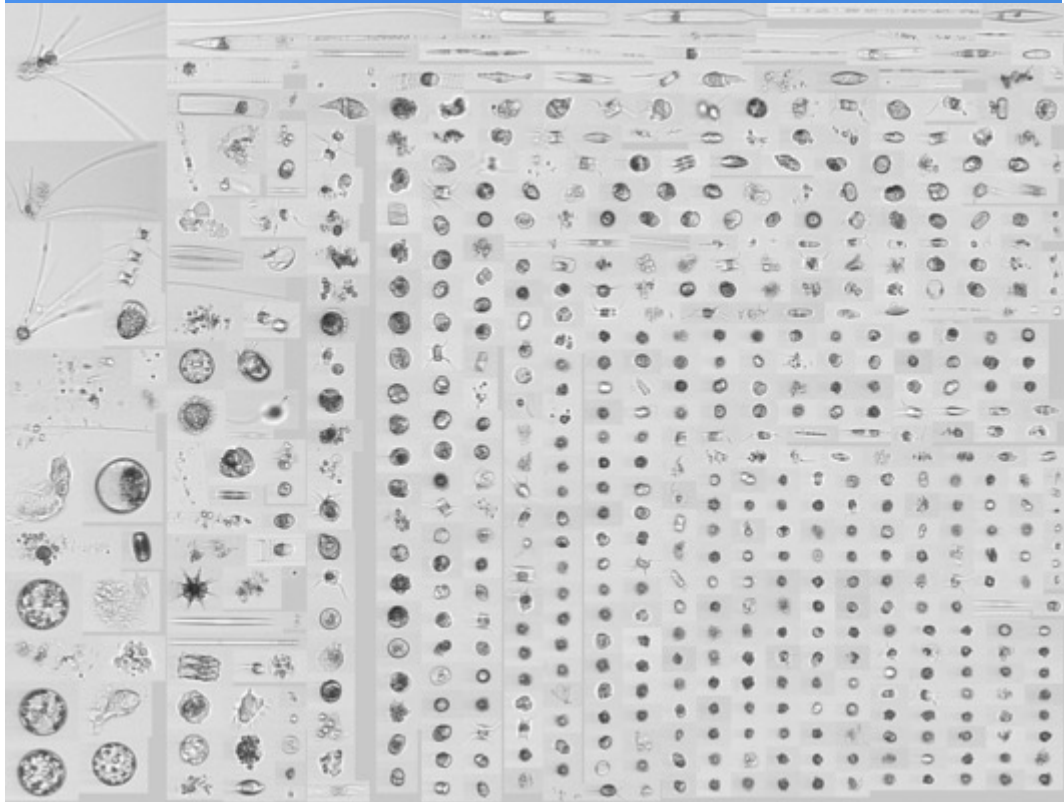


March 25, 2022



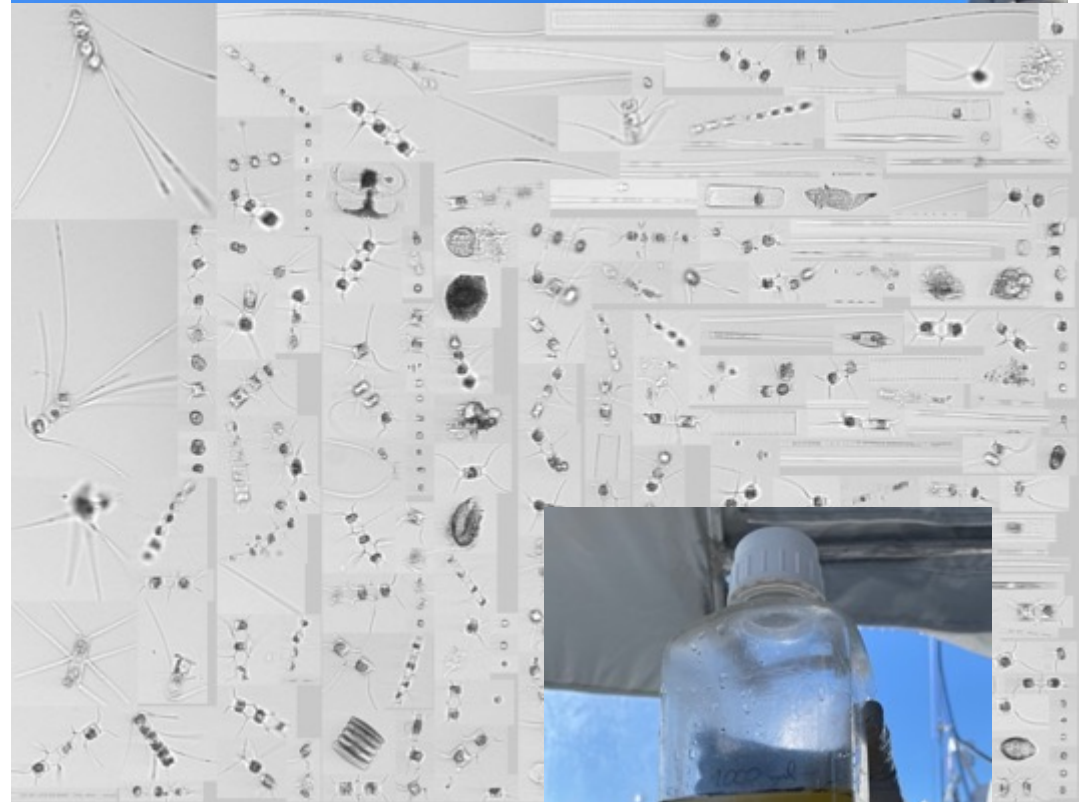
March 27, 2022

~500 ROIs/ml



March 25, 2022

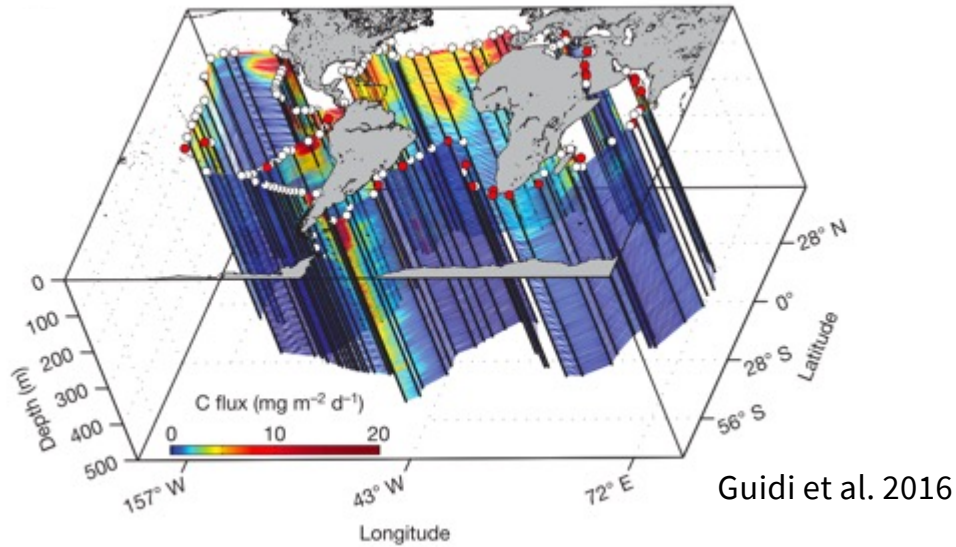
~700 ROIs/ml



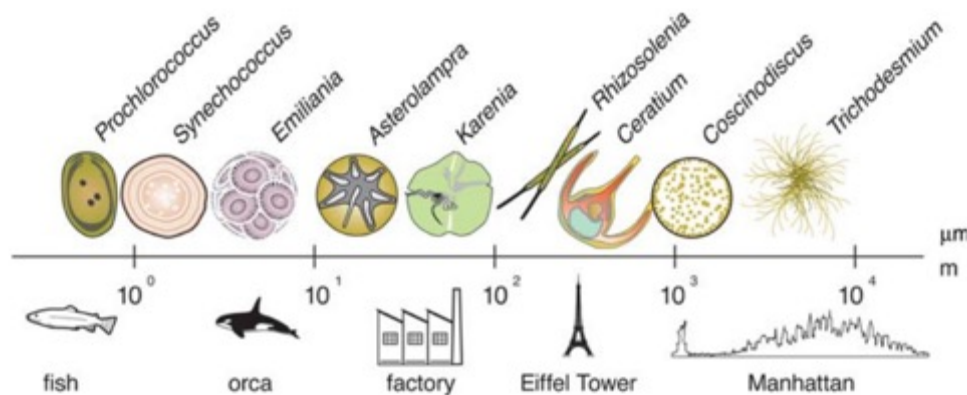
March 27, 2022



# What motivates our interest in phytoplankton community composition (PCC)?



## Variability in carbon flux & food web dynamics



Finkel et al. 2010

<p>Global change</p>	<ul style="list-style-type: none"> <li>• latitudinal distributional shifts</li> <li>• phenology shifts</li> <li>• bloom dynamics</li> </ul>	★
<p>Biogeochemical modeling</p>	<ul style="list-style-type: none"> <li>• phytoplankton community composition</li> <li>• nutrient cycling</li> <li>• export of particles</li> </ul>	★
<p>Ecological processes</p>	<ul style="list-style-type: none"> <li>• rates of primary production</li> <li>• nitrogen fixers, DMS producers, silicifiers, calcifiers</li> <li>• trophic dynamics &amp; food web efficiency</li> </ul>	★
<p>Ecological indicators</p>	<ul style="list-style-type: none"> <li>• hypoxia</li> <li>• eutrophication</li> <li>• informed monitoring and assessment</li> </ul>	★
<p>Environmental reporting</p>	<ul style="list-style-type: none"> <li>• meeting thresholds</li> <li>• species composition</li> <li>• detecting anomalies</li> </ul>	★
<p>Hazard Monitoring</p>	<ul style="list-style-type: none"> <li>• detection and tracking of harmful algal blooms</li> <li>• assessing storm impacts</li> <li>• monitoring oil spill extent and cleanup</li> </ul>	★
<p>Food Security</p>	<ul style="list-style-type: none"> <li>• finding pelagic and benthic habitats for fisheries</li> <li>• locations/monitoring for aquaculture</li> <li>• food safety &amp; toxin production</li> </ul>	★

★ = PCC plays a role

Dierssen et al. 2021

# How is Phytoplankton Community Composition defined?

PSC = Phytoplankton Size Classes (note: PSC also = Photosynthetic Carotenoids...)

- pico, nano, and micro (what should the size cutoffs be?)

PG = Phytoplankton Groups

- a catch-all terms for species and size classes?

PFT = Phytoplankton Functional Types

- biogeochemical function?

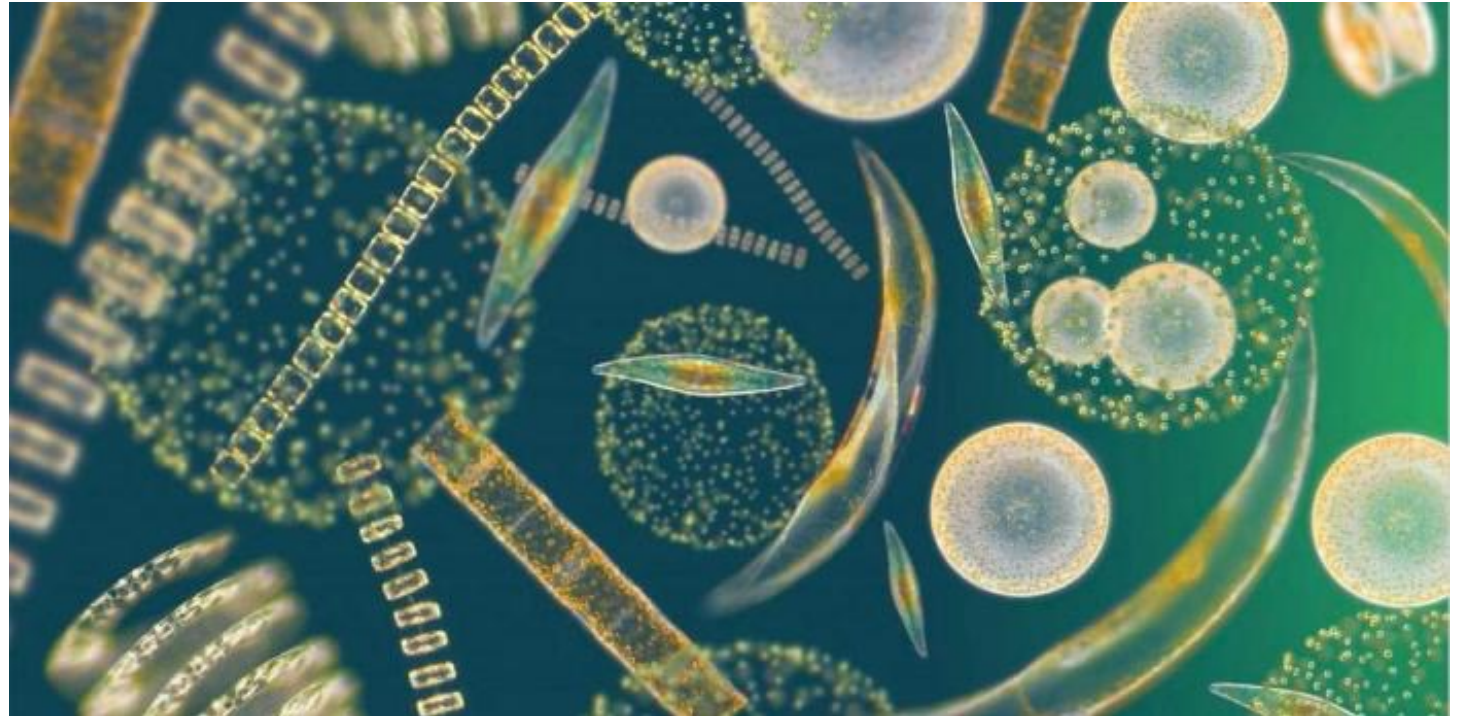
*Buyer Beware: The meanings of **all** these terms may change based on the user*

Bottom line: we want to define the phytoplankton present in the water by some metric that differs from/moves beyond total biomass (most commonly approximated via estimates of chlorophyll  $a$  concentration)



# How is Phytoplankton Community Composition measured?

- Microscopy
- Pigments
- Flow cytometry
- Automated imagery
- Merged size spectra
- Optical signatures
- Molecular methods



→ see lecture by Sasha Kramer from week 1 for a very nice detailed overview:  
[https://misclab.umeoce.maine.edu/OceanOpticsClass2023/assets/pdfs/SJK\\_phytoplankton\\_OO23.pdf](https://misclab.umeoce.maine.edu/OceanOpticsClass2023/assets/pdfs/SJK_phytoplankton_OO23.pdf)

# And what about units???

## Absolute

- Concentrations (cells/L)
- Biovolume (mg/m<sup>3</sup>)
- Biomass, carbon (mg/m<sup>3</sup>)
- Chl *a* (micrograms/L, mg/m<sup>3</sup>)

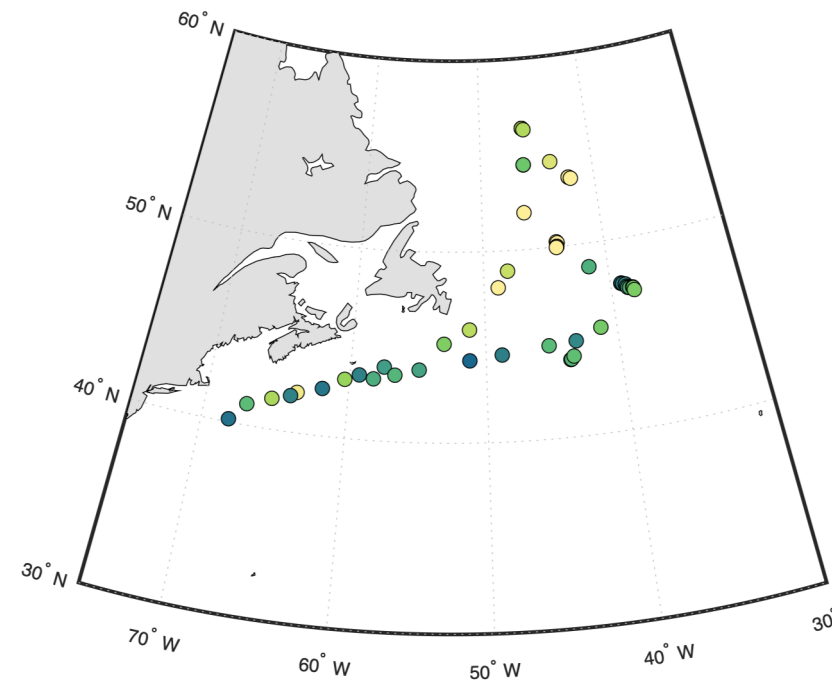
## Relative

- Fraction (%) of total Chl *a*
- Fraction (%) of total biovolume
- Fraction of some subset of the total community (e.g., % of all microplankton)
- “Dominant” group (in what units?)

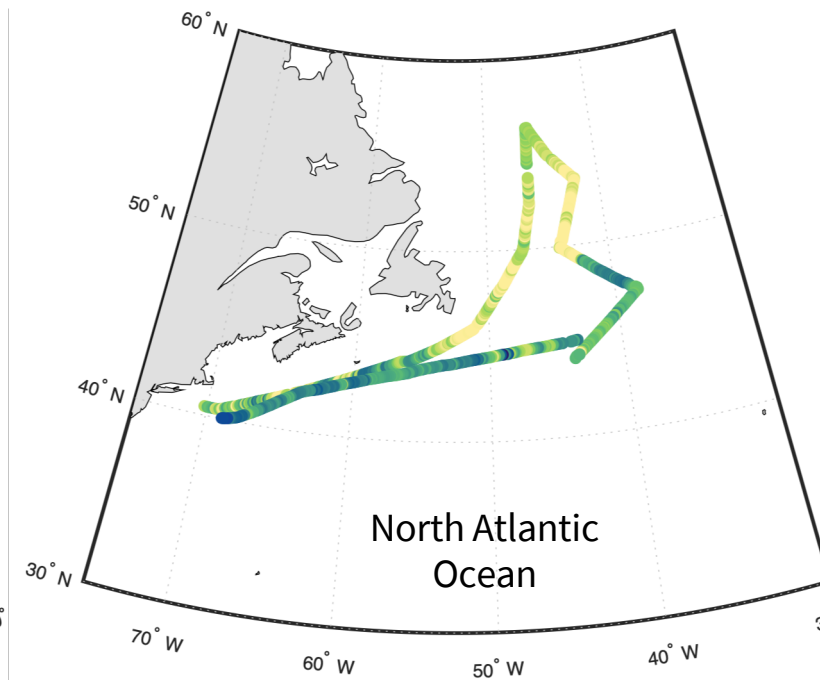
Probability of occurrence (at some threshold?)

# How can we scale up to regional and global views?

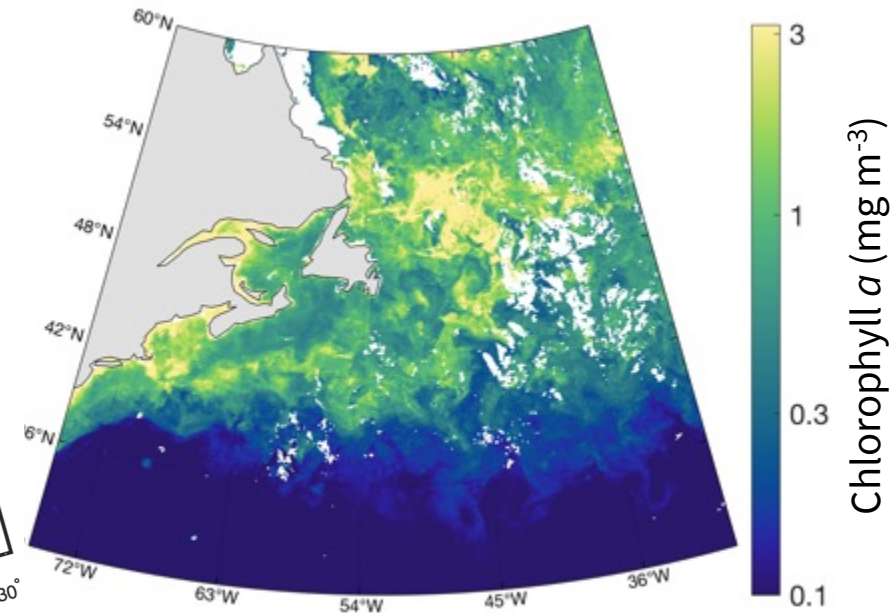
Discrete samples



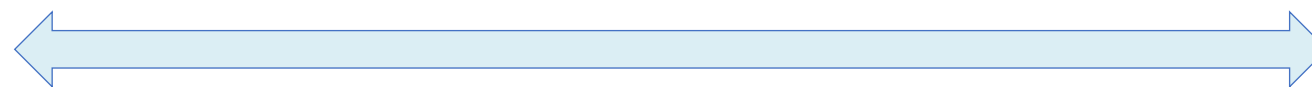
Ship-board continuous measurements



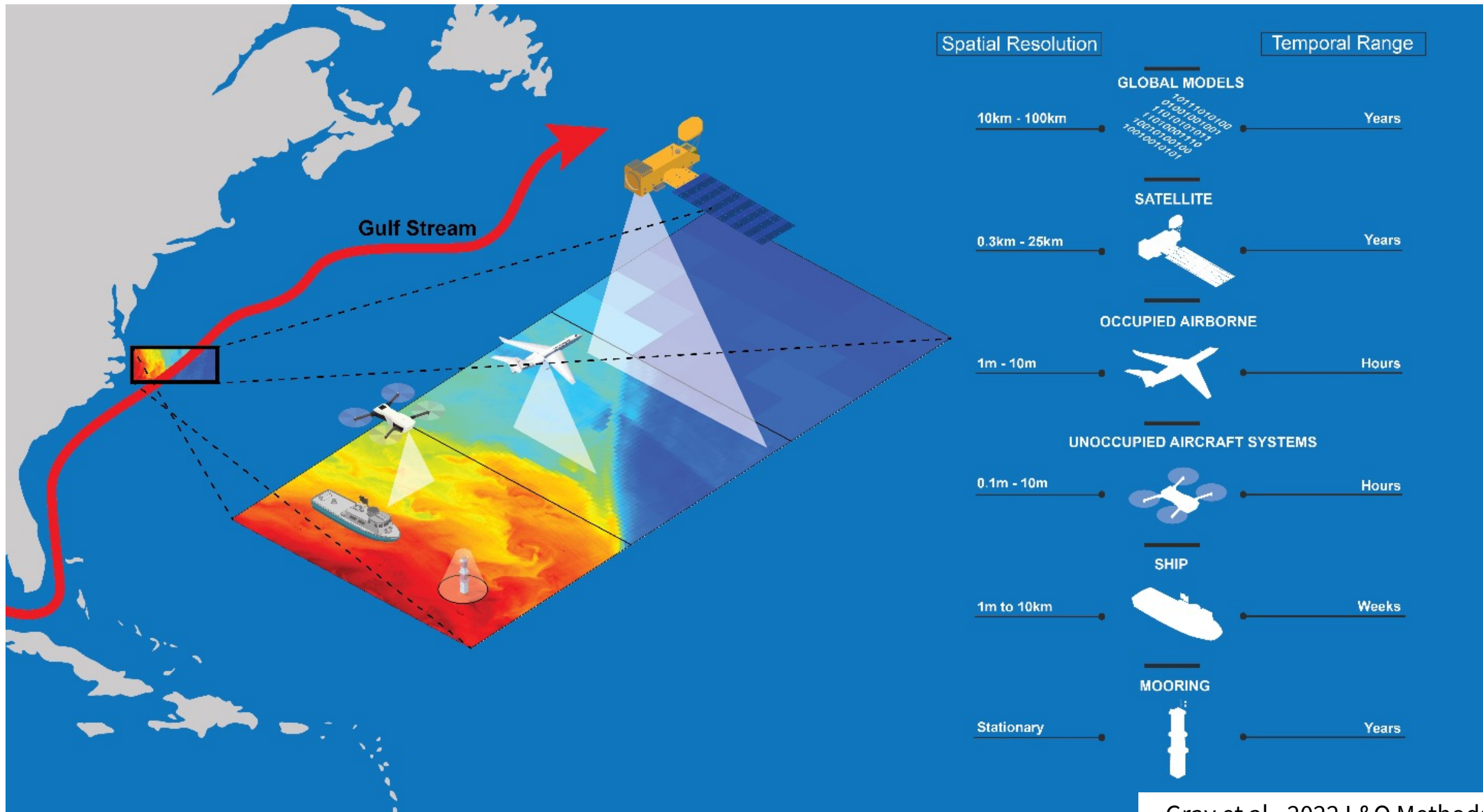
Satellite remote sensing



Direct measurement of cells & processes

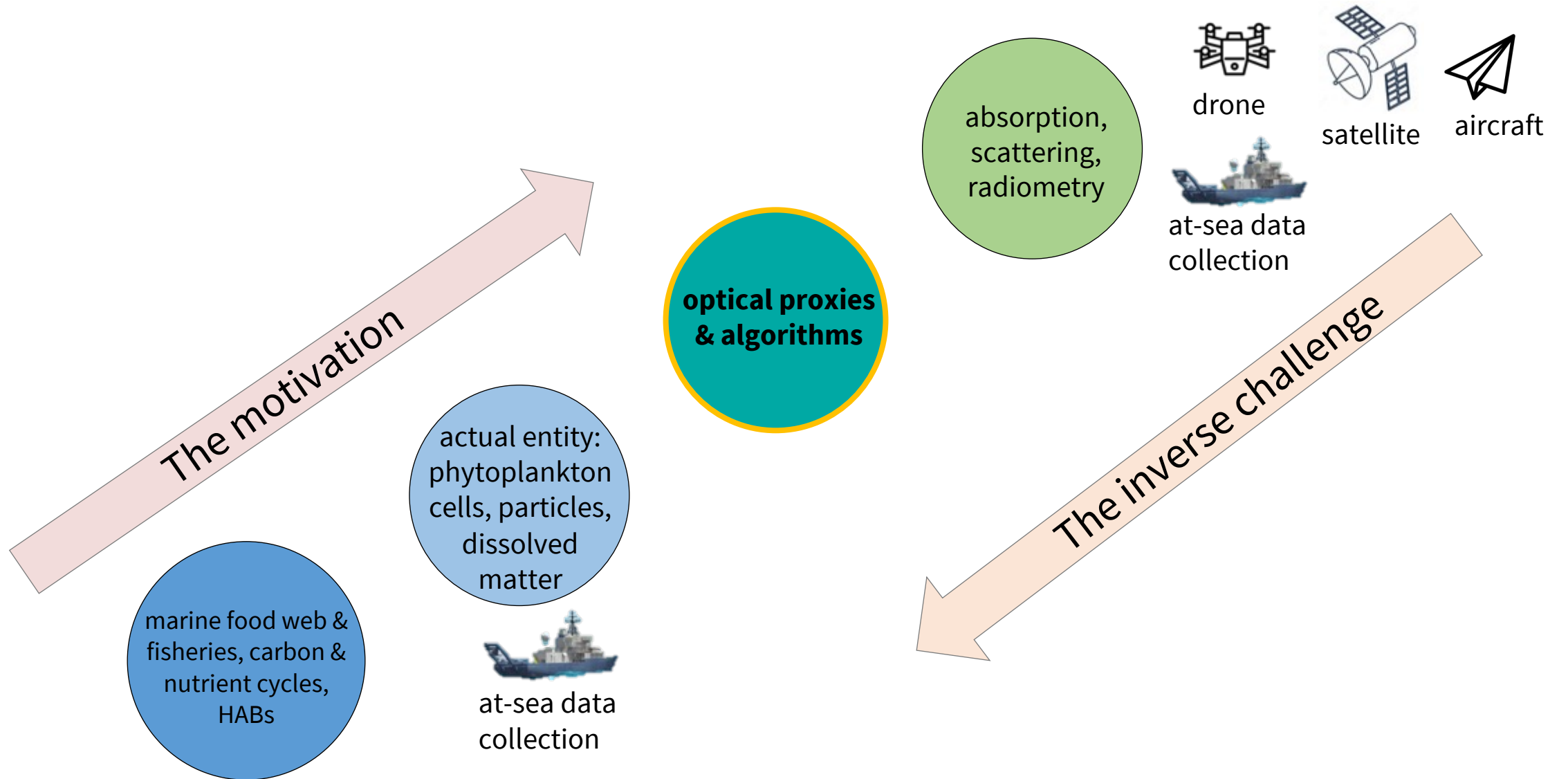


Spatial & temporal resolution\*



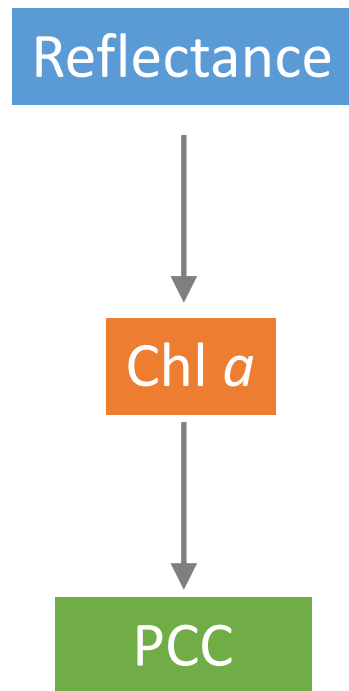


# Optics: a tool to link what we can measure to what we want to know

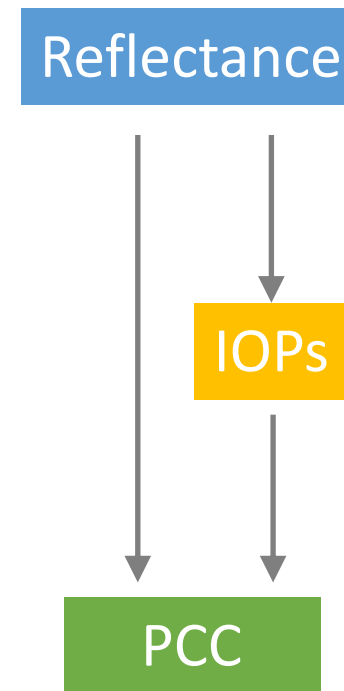


# Previously developed algorithms: two main categories

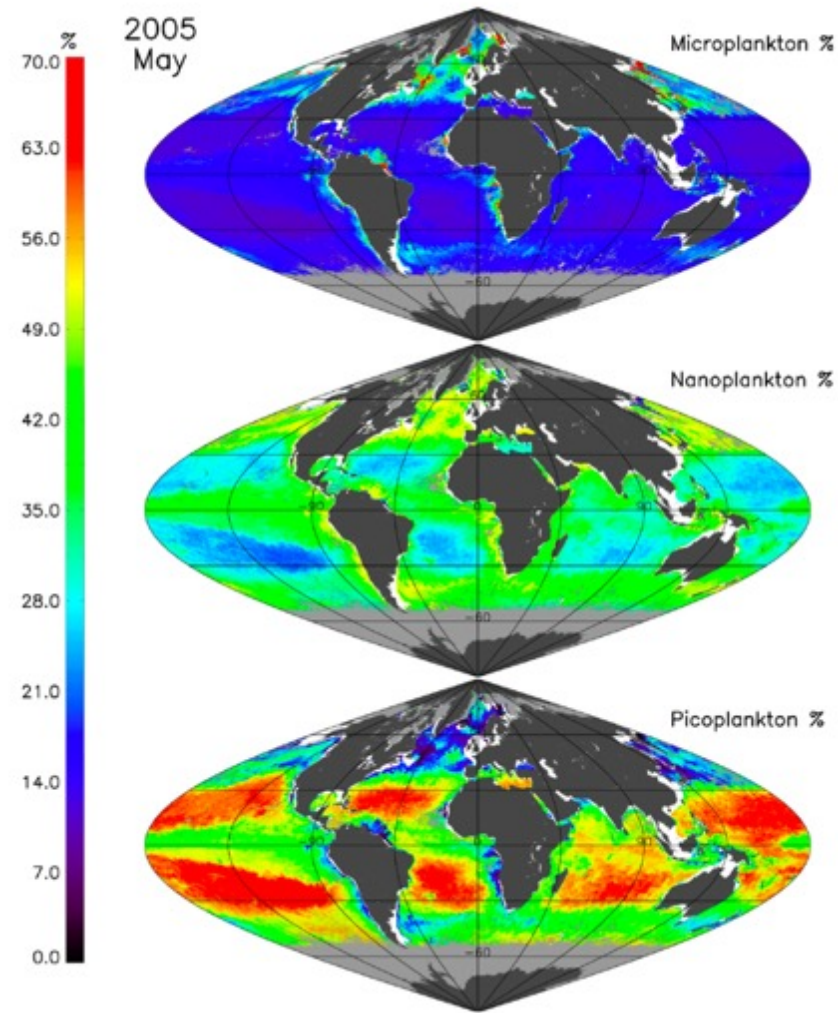
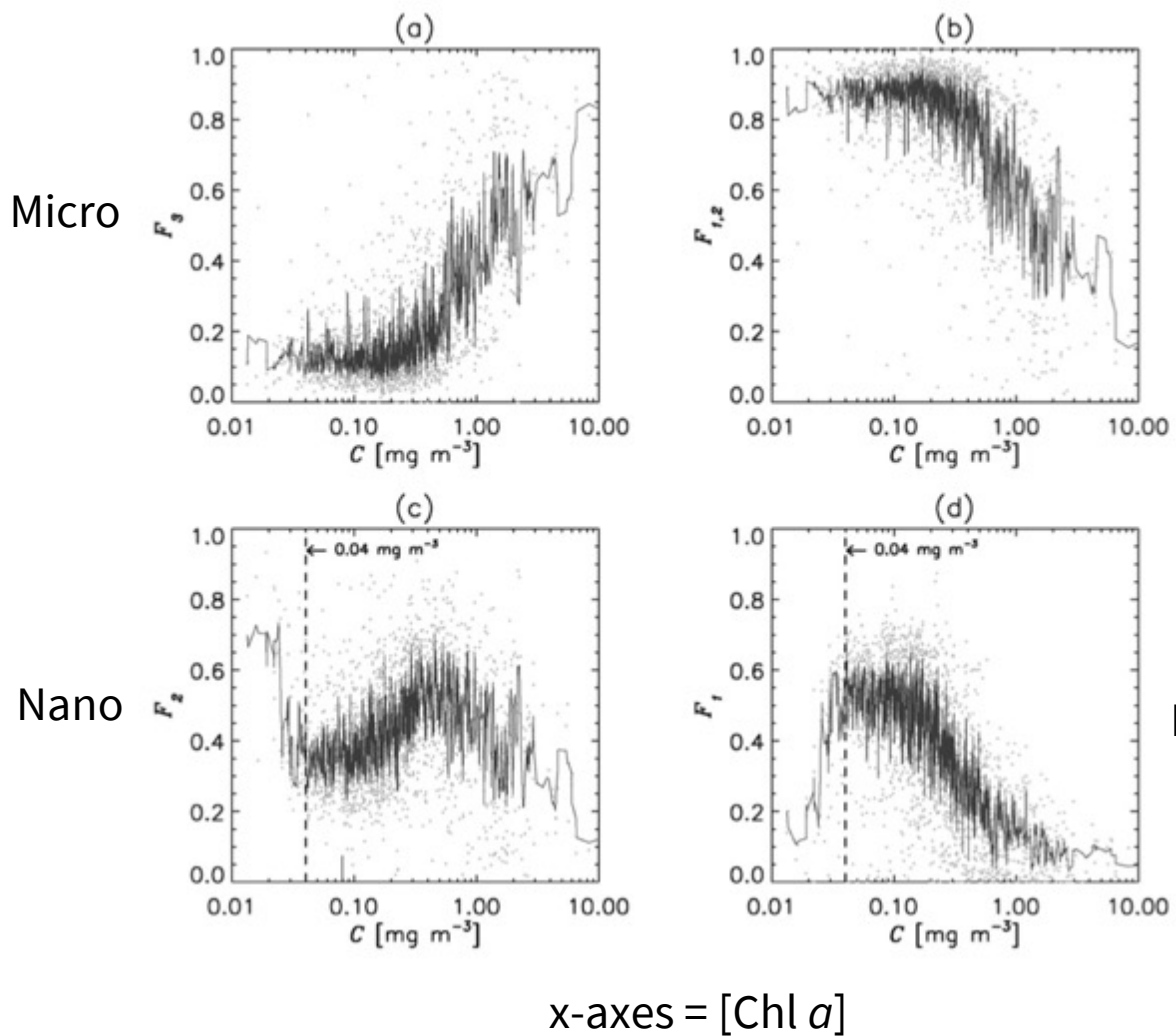
## Abundance-based



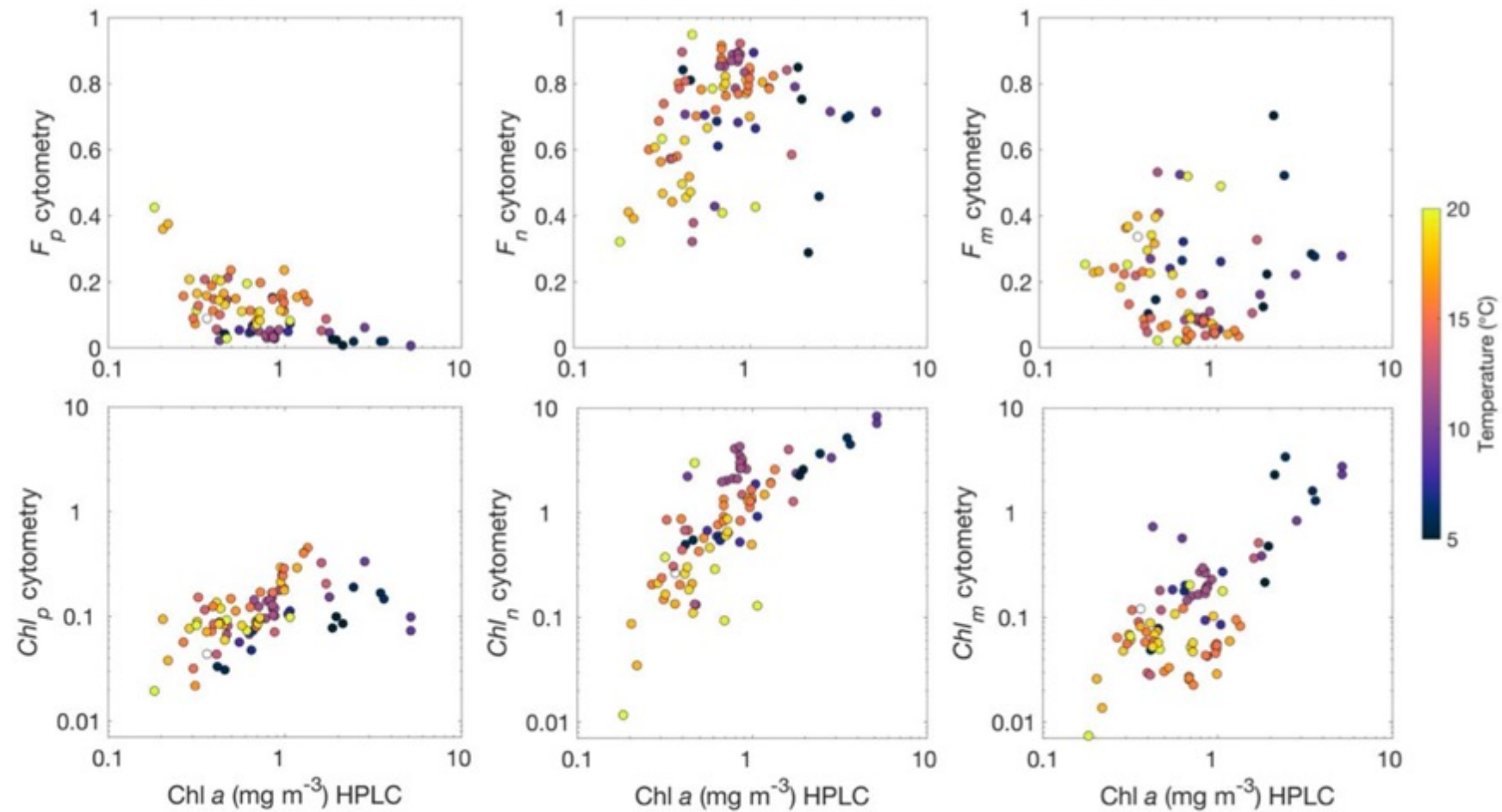
## Spectral-based



# Abundance-based - PSCs



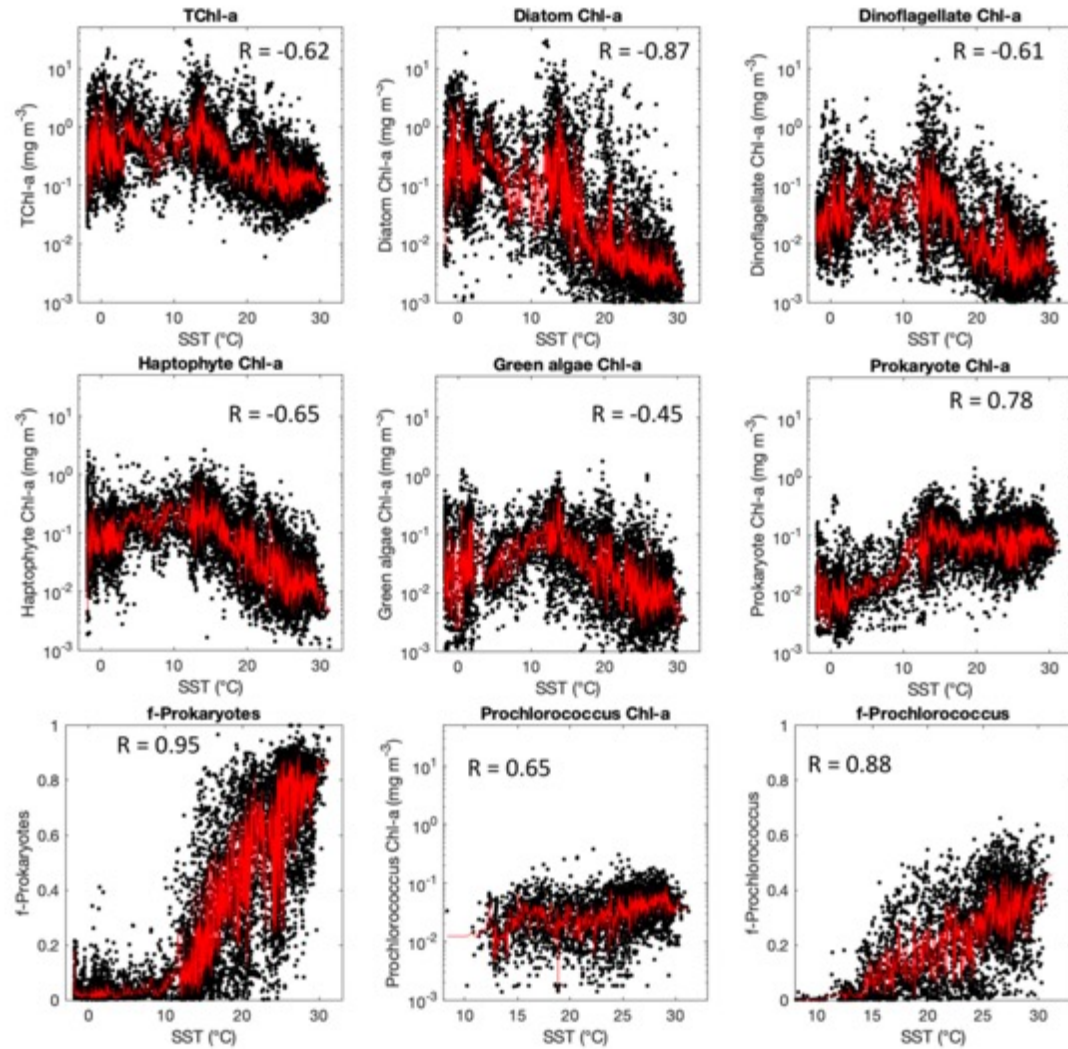
Chl *a* concentrations are related to fractions of pico-, nano-, and microplankton **as defined by pigments**



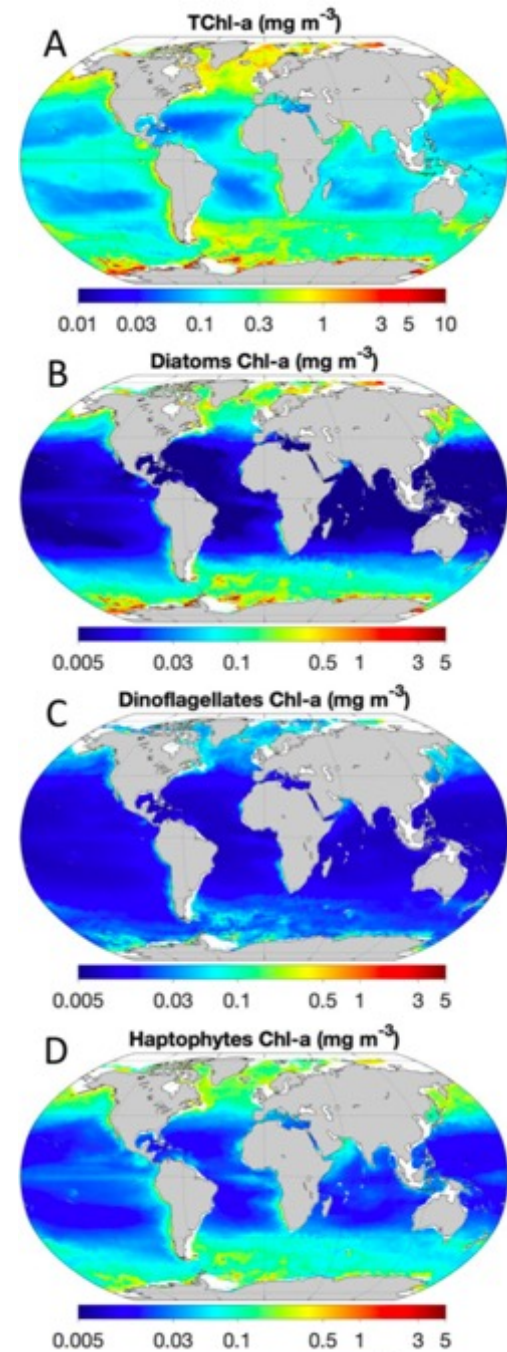
Chl *a* concentrations vs. fraction of pico-, nano-, and microplankton from cytometry



# Abundance-based – taxonomic groups



**Figure 3.** Scatterplots of in situ TChl-a, PFT Chl-a, and fractions of prokaryotes and *Prochlorococcus* versus collocated satellite SST data. The correlation coefficient ( $R$ ) was calculated based on the 10-point running mean (red curve). PFT, phytoplankton functional type; SST, sea surface temperature.



Chl *a* concentrations related to phytoplankton groups as defined by pigments

# Spectral-based - PSCs

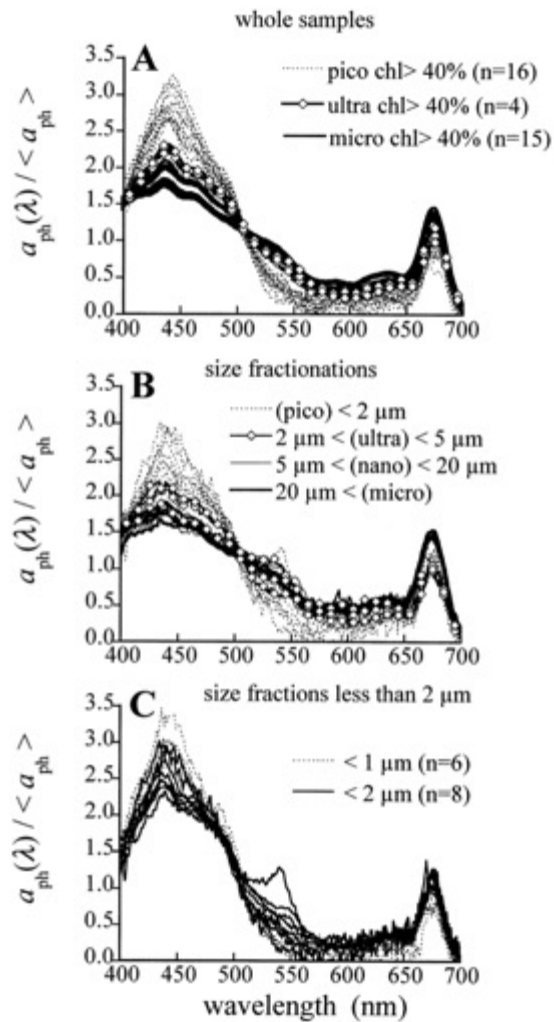
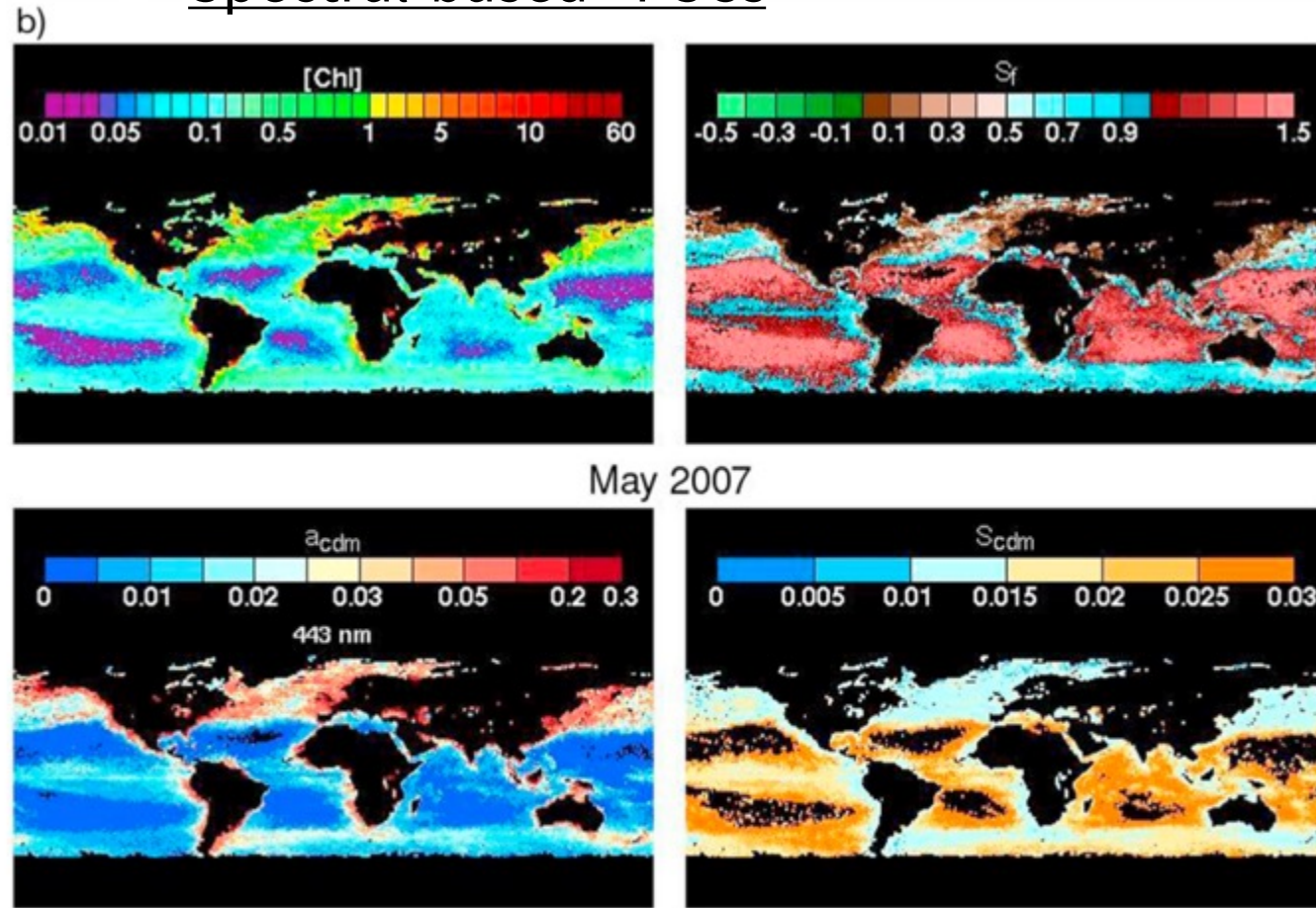


Fig. 3. (A) Phytoplankton absorption spectra measured during the Oregon cruise on whole surface samples. Spectra were normalized to the average phytoplankton absorption between 400 and 700 nm. Legend indicates the dominant Chl *a* size fractions (defined in Fig. 1). (B) Normalized phytoplankton absorption spectra measured directly for different size fractions collected on GF/F filters. (C) Comparison of absorption for size fractions from 14 stations using either 1- or 2- $\mu$ m filters.



**Figure 1.** Monthly maps derived from the SeaWiFS monthly composite of reflectance for (a) February 2007, (b) May 2007, (c) August 2007, and (d) November 2007: (top to bottom and left to right) chlorophyll *a* concentration (in  $\text{mg m}^{-1}$ ), size factor of phytoplankton  $S_f$  (dimensionless), absorption coefficient of colored detrital matter (CDM) at 443 nm (in  $\text{m}^{-1}$ ), and spectral slope of CDM absorption ( $S_{\text{cdm}}$ , in  $\text{nm}^{-1}$ ). Color scales are given for each parameter and are common to Figures 1a–1d. Scales are logarithmic for [Chl] and  $a_{\text{cdm}}(443)$ , and linear for  $S_f$  and  $S_{\text{cdm}}$ .



## Spectral-based – taxonomic groups

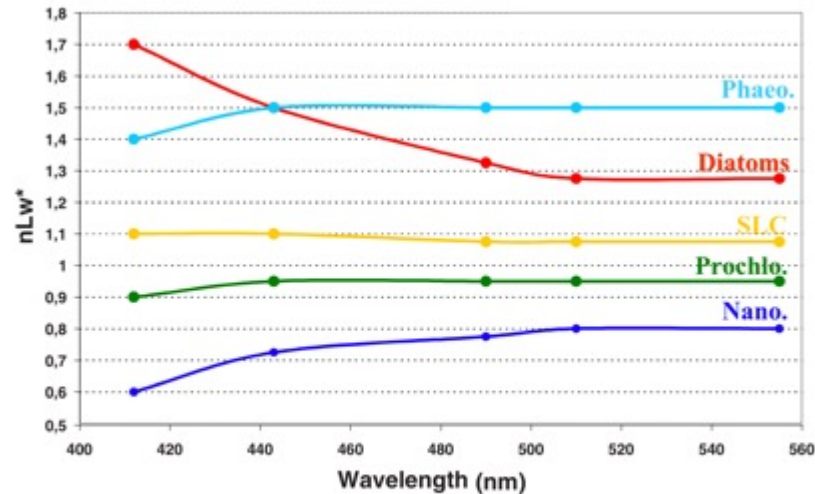


Figure 2. Mean  $nLw^*$  spectra for the five PHYSTAT phytoplankton groups: diatoms in red, nanoecaryotes in blue, Synechococcus in yellow, Prochlorococcus in green, and phaeocystis-like in light blue.

Phytoplankton taxonomic groups as defined by pigments estimated from normalized water-leaving radiance

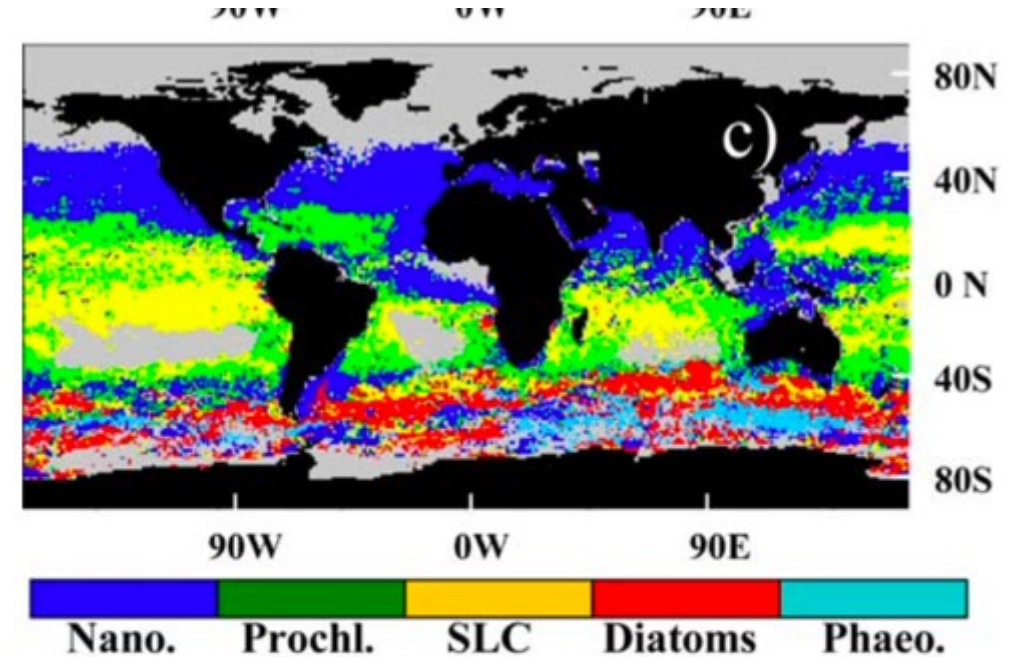
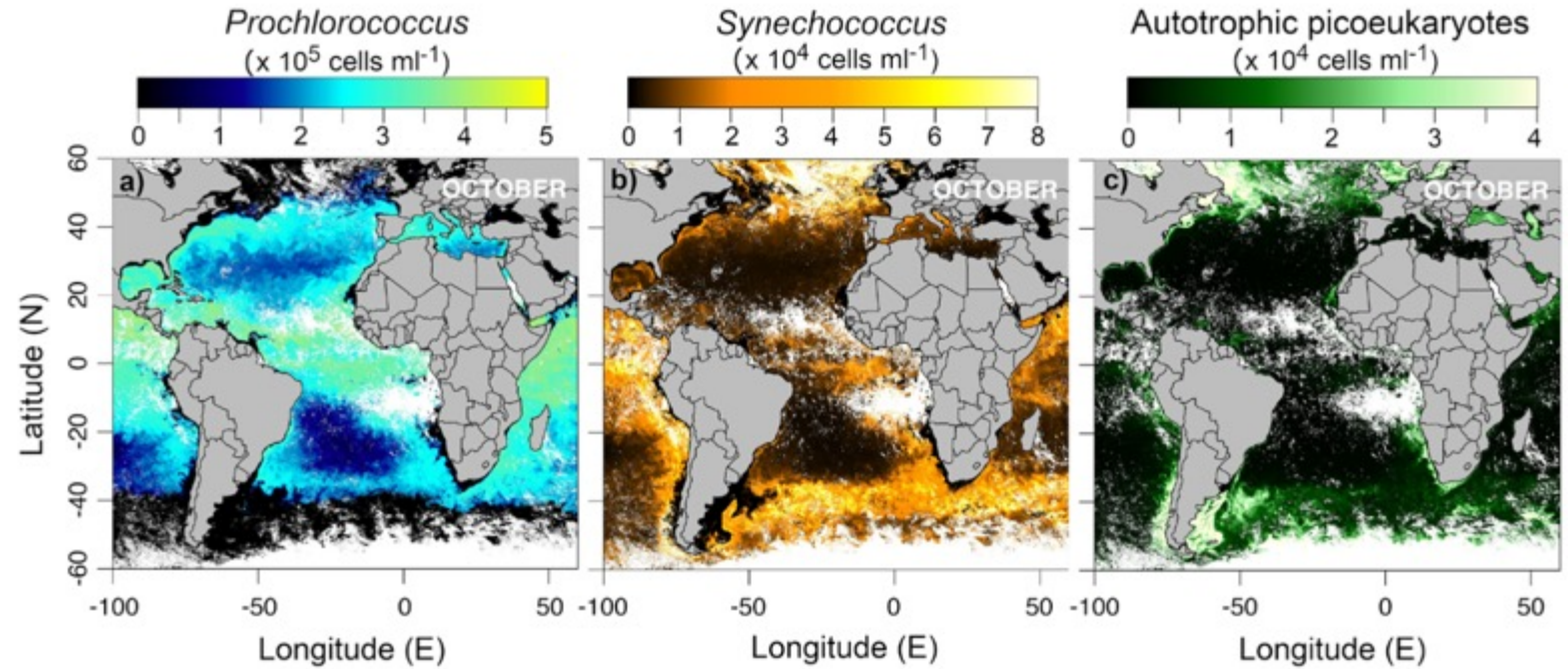
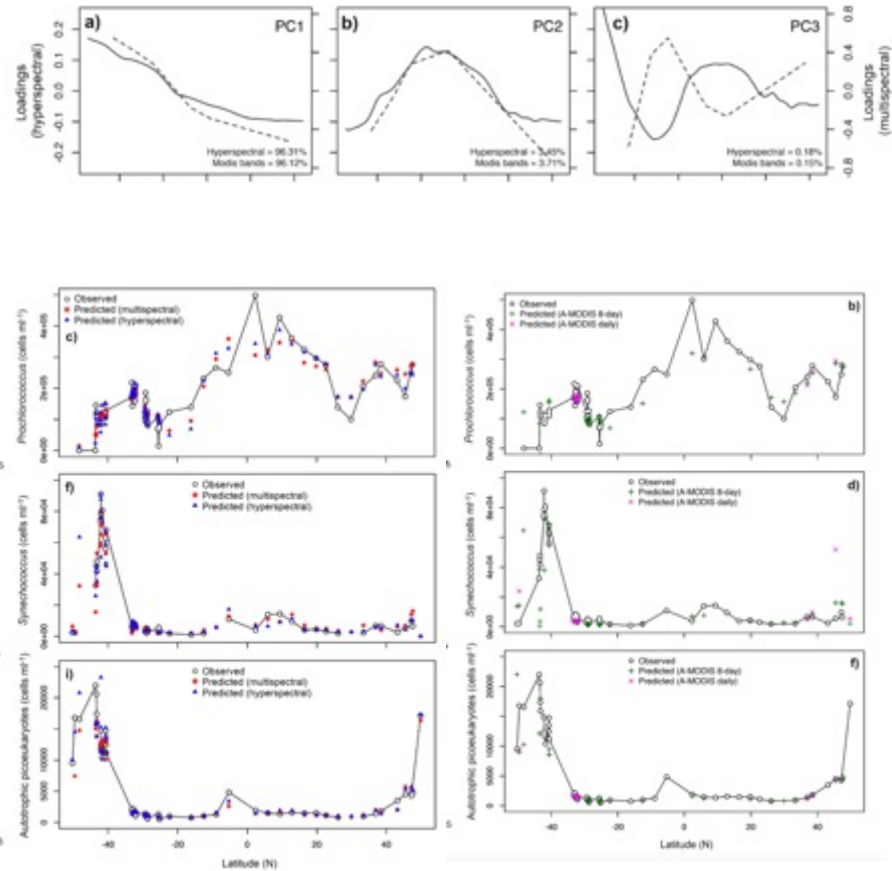


Figure 1. Maps of the dominant phytoplankton group for January 2002 obtained from (a) the standard PHYSTAT method of *Alvain et al.* [2005], (b) the improved PHYSTAT method used in this study, and (c) the improved PHYSTAT method with the additional phaeocystis-like group.

# Spectral-based – taxonomic groups



**Fig. 9.** Aqua-MODIS monthly composites (October 2014) showing cell abundances (cells ml<sup>-1</sup>) of **a) *Prochlorococcus***, **b) *Synechococcus*** and **c) autotrophic picoeukaryotes** at the sea surface.

Picophytoplankton estimated from  $R_{rs}$

**TABLE 2 | Summary of satellite inputs and outputs.**

Type	Algorithm references	Algorithm abbreviation	Development inputs							Satellite inputs				Satellite Outputs								
			<i>nLw/Rrs [Chl]</i>	<i>a<sub>ph</sub></i>	<i>a<sub>cdm</sub></i>	<i>b<sub>bp</sub></i>	<i>η</i>	<i>S</i>	HPLC pigments	<i>nLw/Rrs [Chl]</i>	<i>at</i>	<i>a<sub>ph</sub></i>	<i>a<sub>cdm</sub></i>	<i>b<sub>bp</sub></i>	Micro	Nano	Pico	Hapto (cocco)	Dino	Cyano (Pro/Syn)	Diatom	Phaeo
Abundance	Brewin et al., 2010	BR10	x						x					x	x	x						
	Brewin R. J. et al., 2011	BR10	x	x					x					x	x	x						
	Hirata et al., 2011	OC-PFT	x						x					x	x	x	x	x		x	x	
	Uitz et al., 2006	UITZ06							x					x	x	x						
Radiance	Alvain et al., 2005, 2008	PHYSAT	x	x					x						x		x		x	x	x	
	Li et al., 2013	LI13	x						x					x	x	x						
Absorption	Bracher et al., 2009	PhytoDOAS			x								x							x	x	
	Sadeghi et al., 2012a	PhytoDOAS	x		x								x				x	x			x	
	Ciotti and Bricaud, 2006; Bricaud et al., 2012	CB06	x	x	x	x		x				x	x	(x)		x						
	Devred et al., 2011	DSSP11	x	x	x	x		x	x				x	x	x							
	Fujiwara et al., 2011	FUJI11	x	x	x				x				x		(x)							
	Hirata et al., 2008	HIRATA08		x	x									x	x	x						
	Mouw and Yoder, 2010a	MY10	x	x	x	x		x					x		(x)							
	Roy et al., 2013	ROY13		x	x									x	x	x						
Scattering	Kostadinov et al., 2009, 2010	KSM09					x	x					x			x						

The four algorithm types are indicated by color: abundance (green), radiance (red), absorption (yellow), scattering (blue). The development inputs, satellite inputs, and satellite outputs are indicated with "x" for each algorithm. Instances where other size classes could be inferred but are not directly retrieved are indicated with "(x)". Notation for column headers can be found in **Table 1**.

**Inputs** ≠ **Outputs** is a fundamental algorithm limitation



**Table 3. Compilation of published algorithms to assess phytoplankton community composition. Algorithms are considered global if they are designed for/applied to more than one major ocean.**

Application	PCC product(s)	Algorithm validation data	Remote sensing approaches	Hyperspectral (or polarization?) in situ approaches
Global	Taxonomic group(s)	Direct cell observation (cultures and/or field microscopy)	Subramaniam et al. (2001); Westberry et al. (2005) Subramaniam and Carpenter (1994)	
		Pigment concentrations	Alvain et al. (2005); Alvain et al. (2008); Ben Mustapha et al. (2014); Bracher et al. (2009); Hirata et al. (2011); Losa et al. (2017); Moore et al. (2012); Palacz et al. (2013); Sadeghi et al. (2012); Soppa et al. (2014); Xi et al. (2020)	Torrecilla et al. (2011)
		Spectral signatures	Brown and Yoder (1994)	
	Size classes, size index, or PSD	Pigment concentrations	Brewin et al. (2010); Brewin et al. (2015); Devred et al. (2006); Devred et al. (2011); Fujiwara et al. (2011); Hirata et al. (2008); Hirata et al. (2011); Kostadinov et al. (2010); Li et al. (2013); Moore and Brown (2020); Mouw and Yoder (2010); Roy et al. (2013, spectral a <sub>ph</sub> also used in development); Uitz et al. (2006)	
		Mie modeling, Coated Spheres model	Kostadinov et al. (2009); Kostadinov et al. (2022)	
		Spectral signatures	Bricaud et al. (2012)	
	Accessory pigments	Pigment concentrations	O'Shea et al. (2021); Wang et al. (2018)	Bracher et al. (2015); Chase et al. (2013); (Chase et al. 2017); Kramer et al. (2022); Taylor et al. (2013); Uitz et al. (2015)
Regional /Local	Taxonomic group(s)	Direct cell observation (microscopy of cultures and/or field data or imaging-in-flow cytometry)	Chase et al. (2022); Raitzos et al. (2008) Rêve-Lamarche et al. (2017)	Kirkpatrick et al. (2000); Lubac et al. (2008); Millie et al. (1997); Xi et al. (2017); Xi et al. (2015)
		Pigment concentrations	Di Cicco et al. (2017); Kramer et al. (2018); Palacios et al. (2015); Sathyendranath et al. (2004); Werdell et al. (2014)	Catlett and Siegel (2018); Isada et al. (2015); Shaju et al. (2015)
		Spectral signatures		Craig et al. (2006)
	Size classes, size index, or PSD	Pigment concentrations	Gittings et al. (2019)	
		Spectral signatures	Ciotti and Bricaud (2006)	
	Accessory pigments	Pigment concentrations	Bracher et al. (2015); Pan et al. (2010); Sun et al. (2022)	Aguirre-Gómez et al. (2001); Hoepffner and Sathyendranath (1991); Hoepffner and Sathyendranath (1993); Liu et al. (2019); Lohrenz et al. (2003); Wang et al. (2016); Ye et al. (2019)

# What are the **advantages** and **limitations** of defining PCC via phytoplankton pigments during algorithm development?

- Pigments are ubiquitously measured (global coverage)
- Standardized laboratory protocols (and intercalibrations possible)
- Absorption by pigments is directly related to optical properties of the water
- Pigments  $\neq$  cellular carbon/biomass, and this relationship varies widely
- Taxonomic resolution is limited (and phycobiliproteins are excluded)
- Discrete samples have lower sampling resolution relative to continuously operated instruments

# Obtaining Phytoplankton Diversity from Ocean Color: A Scientific Roadmap for Future Development

Astrid Bracher<sup>1,2\*</sup>, Heather A. Bouman<sup>3</sup>, Robert J. W. Brewin<sup>4,5</sup>, Annick Bricaud<sup>6,7</sup>, Vanda Brotas<sup>8</sup>, Aurea M. Ciotti<sup>9</sup>, Lesley Clementson<sup>10</sup>, Emmanuel Devred<sup>11</sup>, Annalisa Di Cicco<sup>12</sup>, Stephanie Dutkiewicz<sup>13</sup>, Nick J. Hardman-Mountford<sup>14</sup>, Anna E. Hickman<sup>15</sup>, Martin Hieronimi<sup>16</sup>, Takafumi Hirata<sup>17,18</sup>, Svetlana N. Losa<sup>1</sup>, Colleen B. Mouw<sup>19</sup>, Emanuele Organelli<sup>4</sup>, Dionysios E. Raitsos<sup>4</sup>, Julia Uitz<sup>6,7</sup>, Meike Vogt<sup>20</sup> and Aleksandra Wolanin<sup>1,2,21</sup>

<https://www.frontiersin.org/articles/10.3389/fmars.2017.00055/full>

Gap 1: **Information mismatch** between satellite-derived phytoplankton composition products and user group target variables

Gap 2: Lack of traceability of **uncertainties** in phytoplankton group algorithms

Gap 3: Missing **capabilities of** current ocean color **satellite measurements**

Gap 4: Lack of **regional capability** of phytoplankton group algorithms



# Hyperspectral measurements can capture features missed by multi-spectral

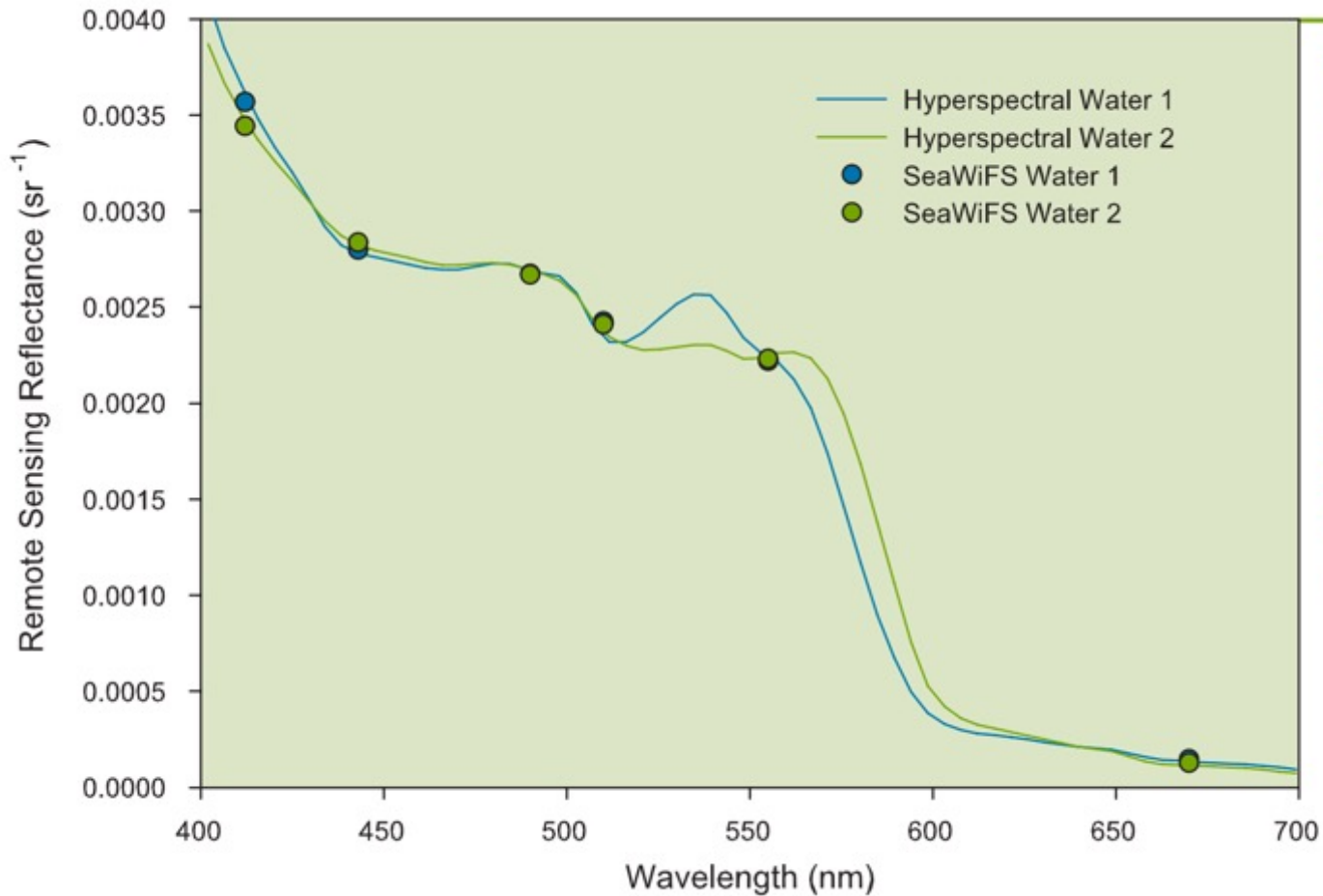


Figure 2. Bottom effects in shallow coastal waters may lead to inaccurate remote sensing retrievals of bottom depth if limited spectral bands are utilized for analysis. This figure shows modeled hyperspectral (solid lines) and multispectral (SeaWiFS wavebands; circles) spectra for two water types, generated by the Hydrolight radiative transfer model (Mobley, 1994). Water 1 (blue) is 6.5 m deep and has low chlorophyll-a and CDOM concentrations with a bottom type of a mixture of soft coral and *Sargassum*, while Water 2 (green) is 13 m deep, “pure water” with a flat green sponge bottom type. By inspection of the hyperspectral spectra, the difference between the two curves is obvious in the 500-600 nm range. However, spectra for the two water types produced using only the SeaWiFS wavebands appear almost identical. (SeaWiFS spectra in this figure were derived by applying the SeaWiFS spectral response function to the hyperspectral signatures).



# Living up to the Hype of Hyperspectral Aquatic Remote Sensing: Science, Resources and Outlook

Heidi M. Dierssen<sup>1\*</sup>, Steven G. Ackleson<sup>2</sup>, Karen E. Joyce<sup>3</sup>, Erin L. Hestir<sup>4</sup>, Alexandre Castagna<sup>5</sup>, Samantha Lavender<sup>6</sup> and Margaret A. McManus<sup>7</sup>

## Data Transformations

**Spectra subject to one or more transformations**

- Band Math
- Derivative Analysis
- Coordinate Transformations

## Retrieval Approaches

**Spectra as Descriptors**  
*used as indices or categories*

- Hue Angle
- Cluster Analysis
- Object Based Image Analysis

**Spectra as Predictors**  
*used as independent variables to predict system properties*

- Parametric Regression
- Neural Networks
- Decision Trees

**Spectra as References**  
*used as a reference against modeled or measured spectra*

- Optimization Algorithms
- Linear Matrix Inversion

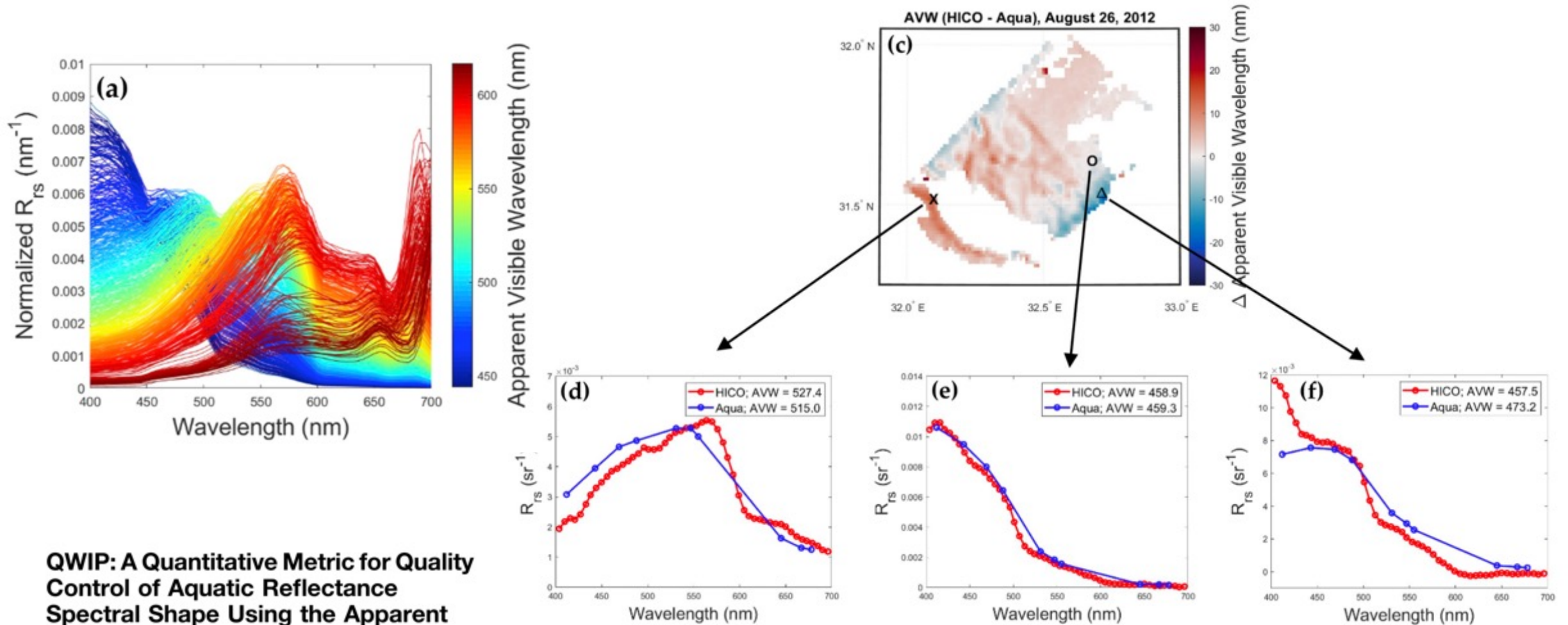


# Approaches to extract information from hyperspectral data

Approach	Input measurements	Result/product	Target/validation data	Reference
Direct use of optical measurements: Similarity Index, EOF, and/or clustering analysis	$a_{\phi}(\lambda)$ & 4 <sup>th</sup> derivative of spectra	% contribution of <i>G. breve</i>	<i>G. breve</i> field and culture data	Millie et al. 1997
	2 <sup>nd</sup> derivative of $a_{\phi}(\lambda)$	Diatom contribution to Chl <i>a</i>	CHEMTAX diatom Chl <i>a</i>	Isada et al. 2015
	$a_p(\lambda)$	Cell counts and Chl <i>a</i> fraction of <i>G. breve</i>	<i>G. breve</i> field and culture data	Kirkpatrick et al. 2000
	2 <sup>nd</sup> derivative of $R_{rs}(\lambda)$	Detection of <i>Phaeocystis</i> blooms	Microscopic identification of phytoplankton	Lubac et al. 2008
	4 <sup>th</sup> derivative of $a_{\phi}(\lambda)$ and $R_{rs}(\lambda)$	Differentiation of phytoplankton groups; cyanobacteria dominance in inland waters	Cultures, Hydrolight simulations, field $R_{rs}(\lambda)$ measurements	Xi et al. 2015; 2017
	Derivatives of $a_p(\lambda)$ or $a_{\phi}(\lambda)$	Pigment assemblages or concentrations	HPLC pigments or Chl <i>a</i> concentration from fluorescence	Catlett and Siegel 2018; Shaju et al. 2015; Torrecilla et al. 2011
	$R_{rs}(\lambda)$	Pigment concentrations	HPLC pigments	Bracher et al. 2015; Kramer et al. 2022
	$a_{\phi}(\lambda)$ and $R_{rs}(\lambda)$ , and derivatives	Bio-optical water categories	HPLC pigments	Uitz et al. 2015
	$L_u(\lambda)$	Relative phycoerythrin concentrations	PE concentration	Taylor et al. 2013
Methods of spectral inversion: Spectral inversion and Gaussian decomposition	$a_{\phi}(\lambda)$ and $R_{rs}(\lambda)$ , and $a_{\phi}(\lambda)$ derivatives	<i>K. brevis</i> relative bloom strength	<i>K. brevis</i> absorption spectrum	Craig et al. 2006
	$R_{rs}(\lambda)$	Apparent Visible Wavelength		Vandermuelen et al. 2020; Dierssen et al. 2022
	$a_p(\lambda)$ or $a_{\phi}(\lambda)$	Pigment concentrations or absorption	HPLC pigments	Aguirre-Gomez et al. 2001; Chase et al. 2013; Hoepffner and Sathyendranath 1991, 1993; Liu et al. 2019; Lohrenz et al. 2003; Ye et al. 2019
	$R_{rs}(\lambda)$	Contribution of phytoplankton groups to absorption	Microscopic cell counts	Roesler et al. 2004
	$R_{rs}(\lambda)$	Pigment concentrations	HPLC pigments	Chase et al. 2017; Wang et al. 2016
$R_{rs}(\lambda)$	$a_{\phi}(\lambda)$ and Chl <i>a</i> concentrations	In situ $R_{rs}(\lambda)$	Pahlevan et al., 2020; Pahlevan et al., 2021	

# Retrieval Algorithms

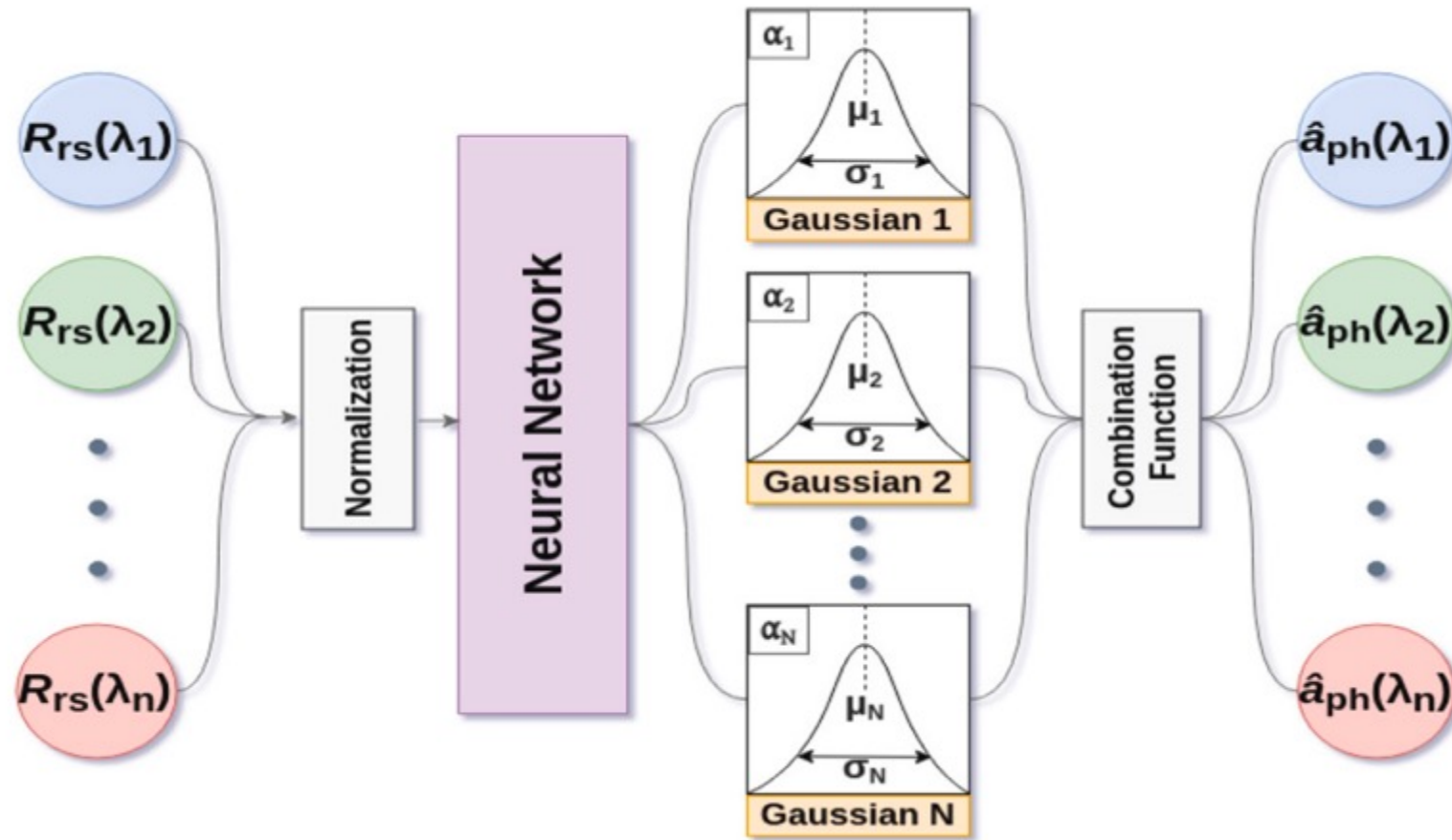
- Spectra as descriptors: optical indices, cluster analyses



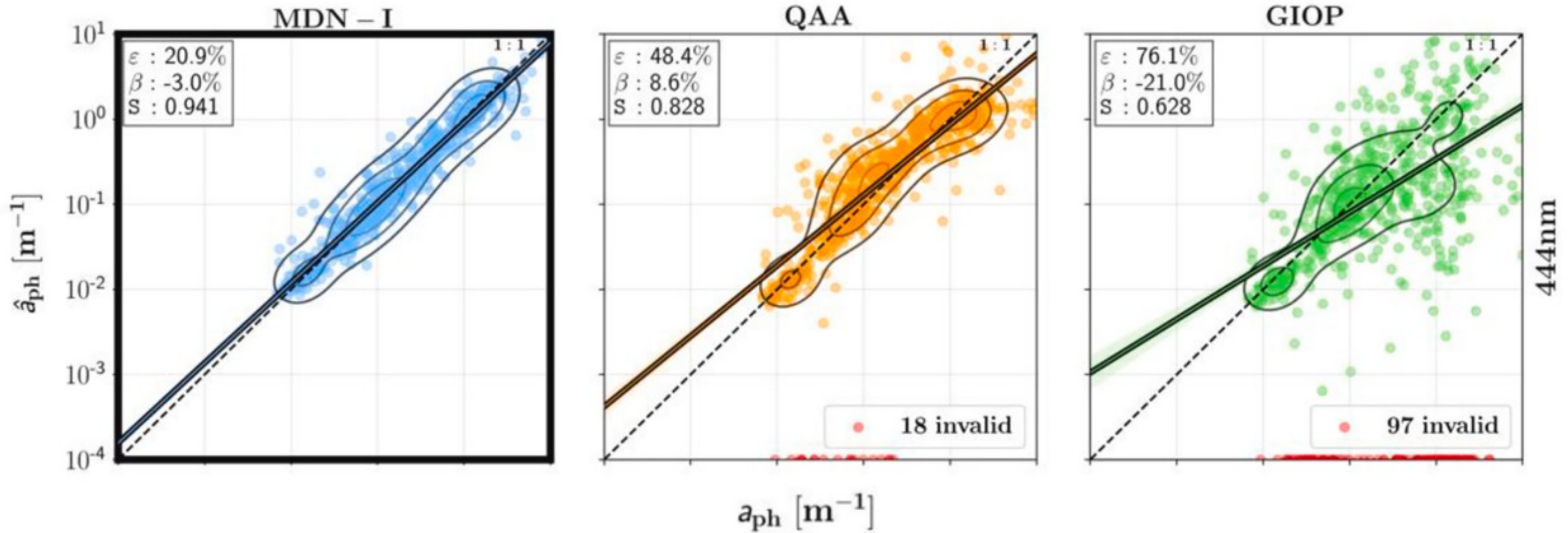
**QWIP: A Quantitative Metric for Quality Control of Aquatic Reflectance Spectral Shape Using the Apparent Visible Wavelength**

Heidi M. Dierssen<sup>1\*</sup>, Ryan A. Vandermeulen<sup>2,3</sup>, Brian B. Barnes<sup>4</sup>, Alexandre Castagna<sup>5</sup>, Els Knaeps<sup>6</sup> and Quinten Vanhellemont<sup>7</sup>

# Applying Mixture Density Networks (MDN) to hyperspectral $R_{rs}$

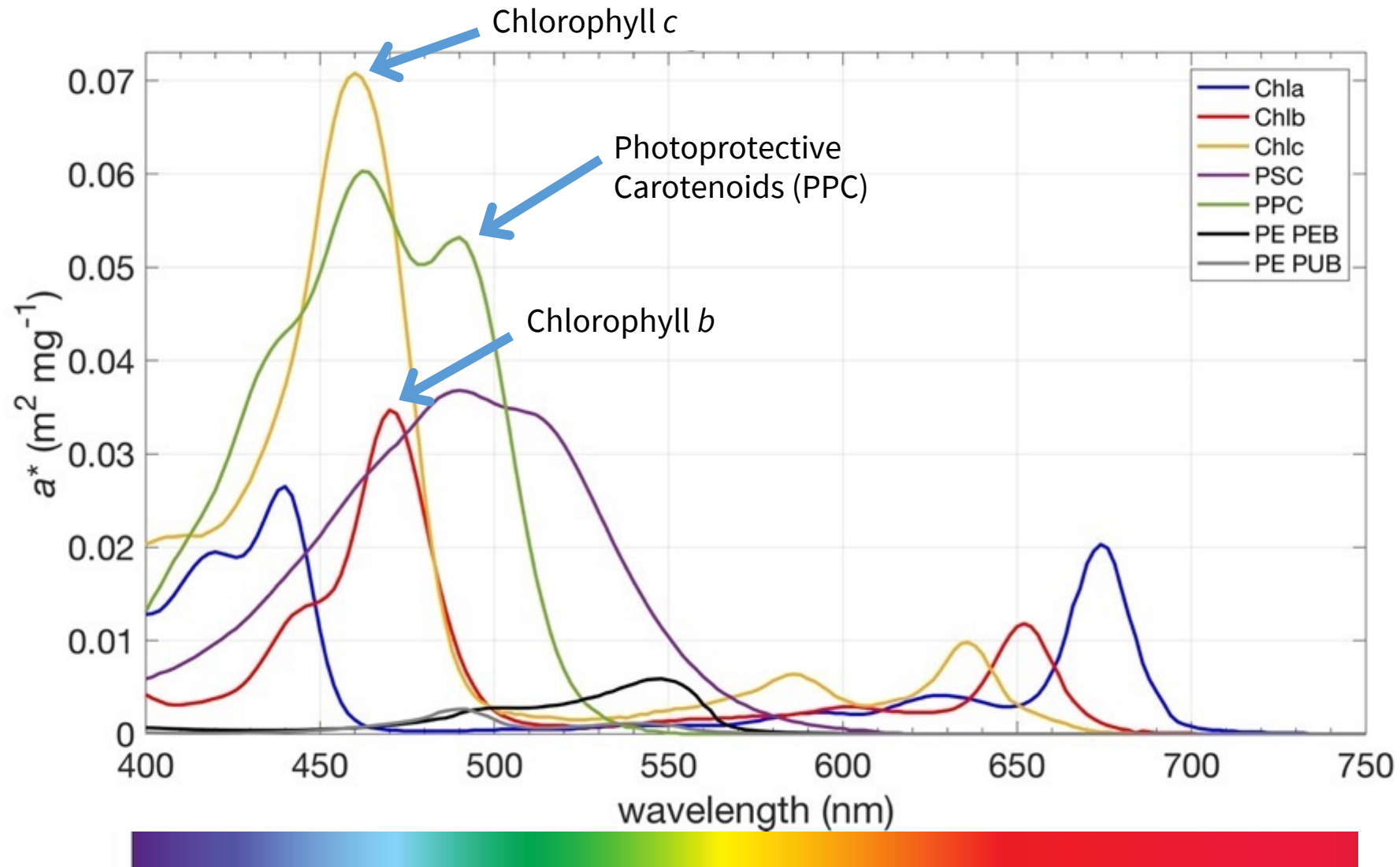


# Applying Mixture Density Networks (MDN) to hyperspectral $R_{rs}$

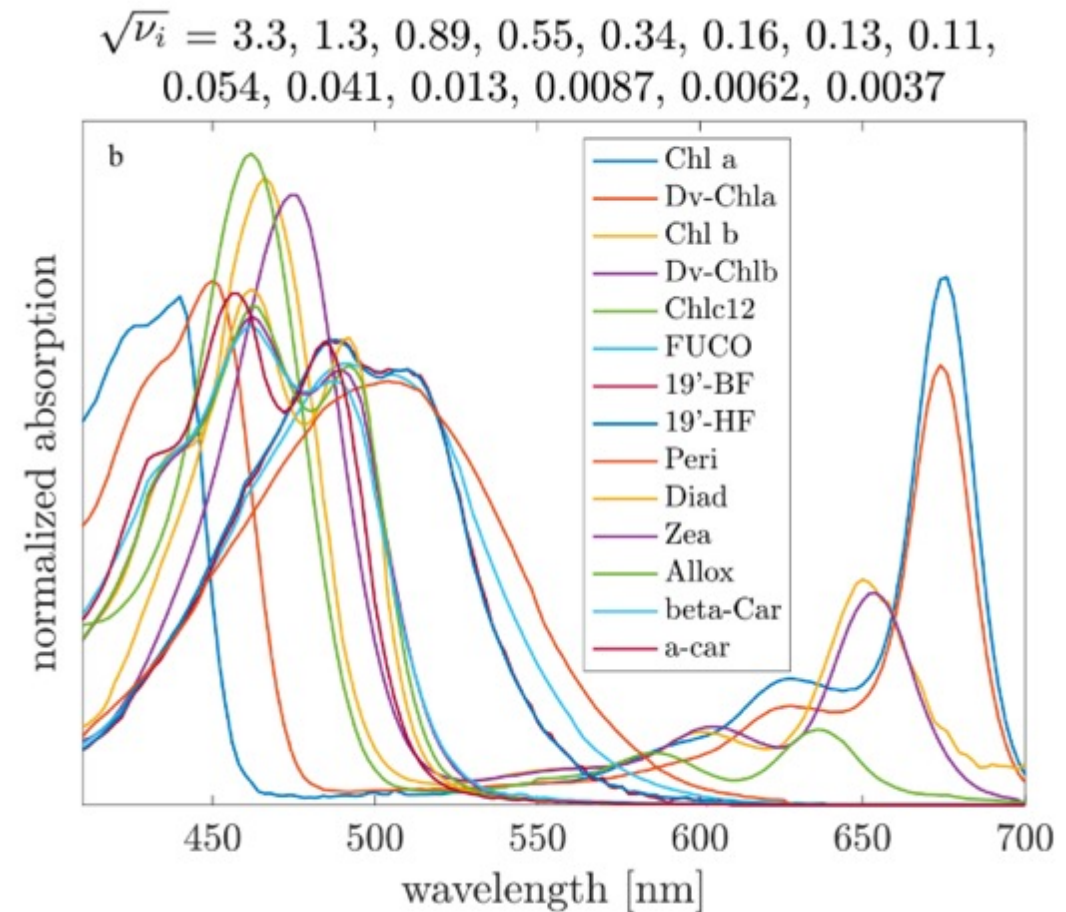
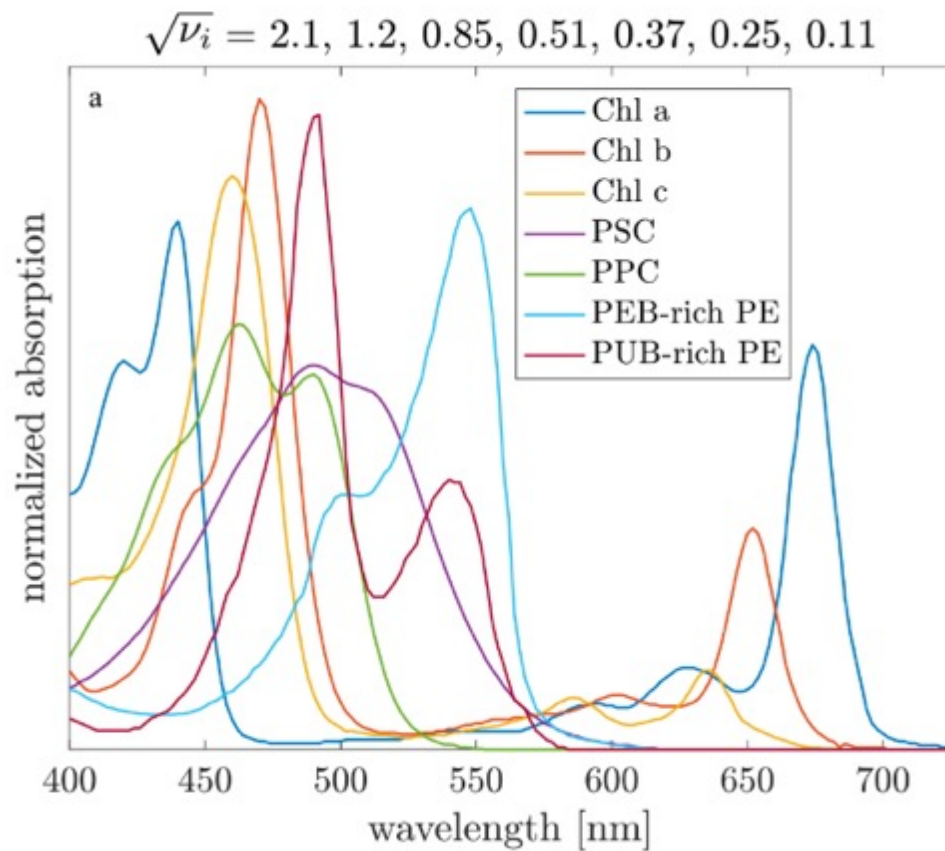




# Phytoplankton pigments drive spectral absorption features



# But does the inversion problem become ill-posed?



# Phytoplankton pigments estimated using Gaussian decomposition

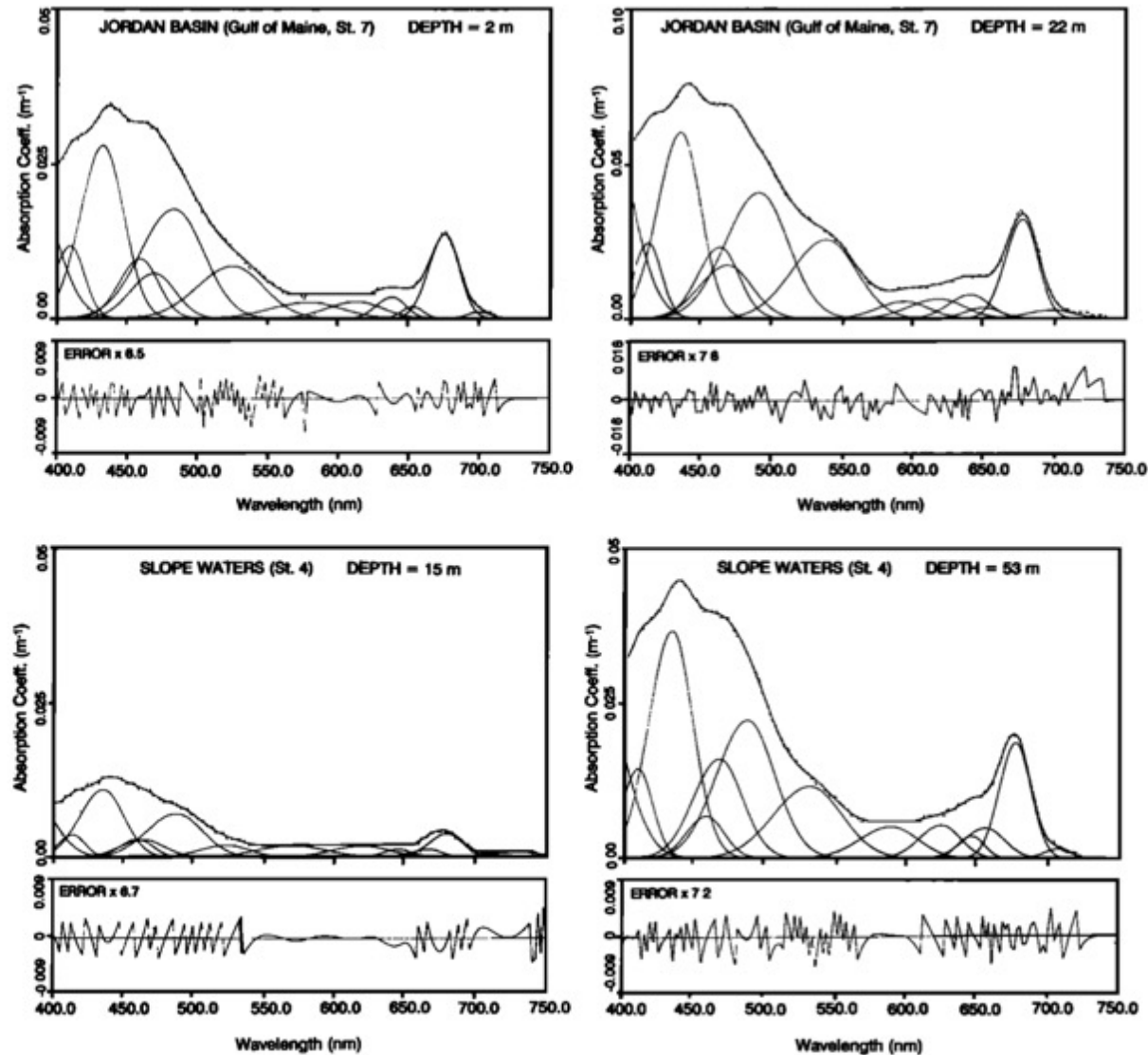
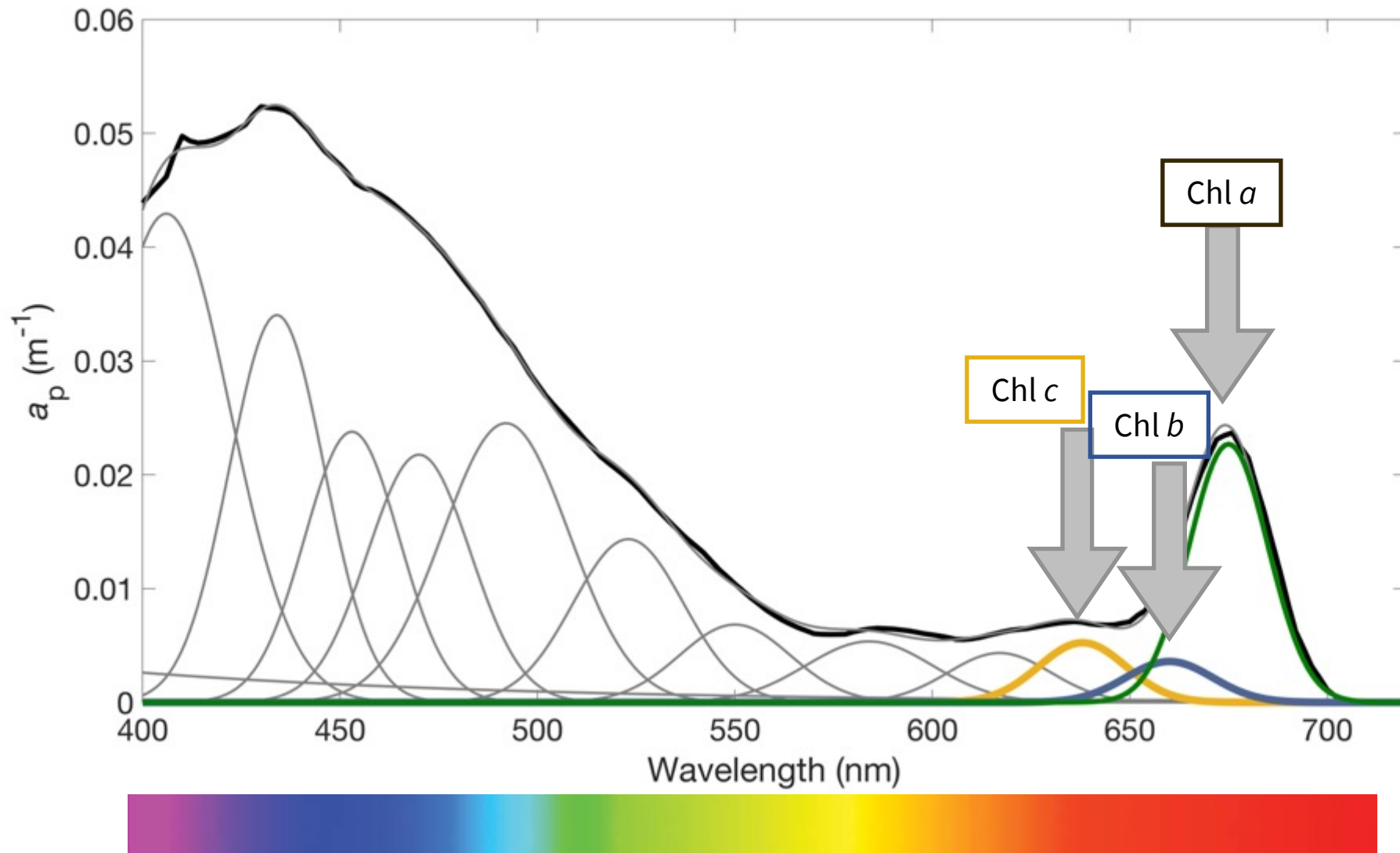


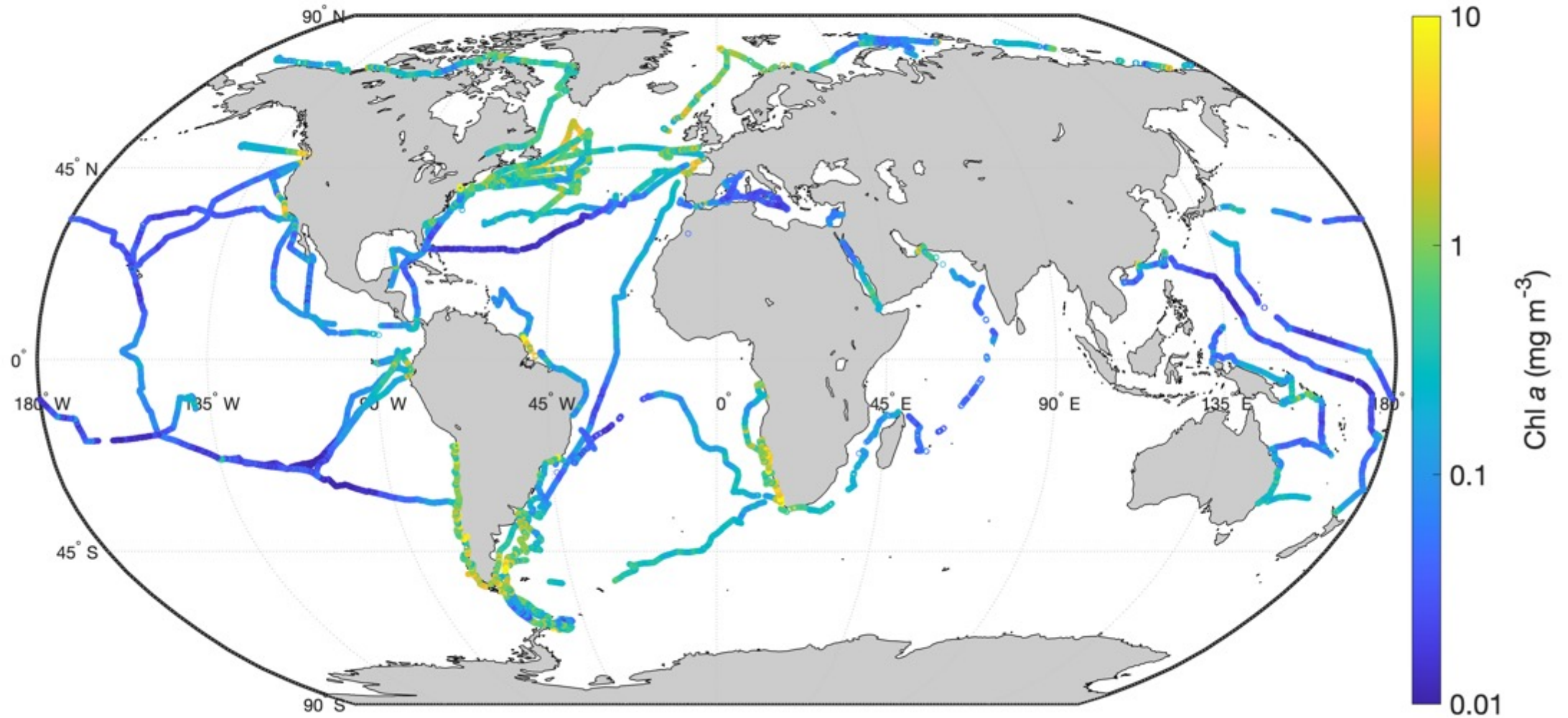
Fig. 7. Decomposition of absorption spectra of natural phytoplankton communities into 13 Gaussian bands, reflecting the absorption characteristics of chlorophylls *a*, *b*, and *c* and of carotenoids at two locations in the western North Atlantic. Variations in the residual error are shown in the lower panel for each spectrum.



# Phytoplankton pigments estimated from ac-s absorption spectra



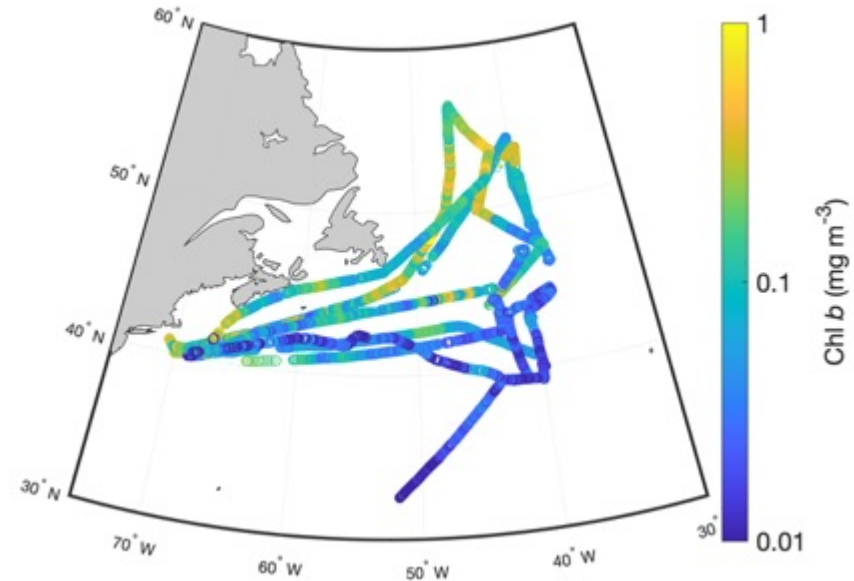
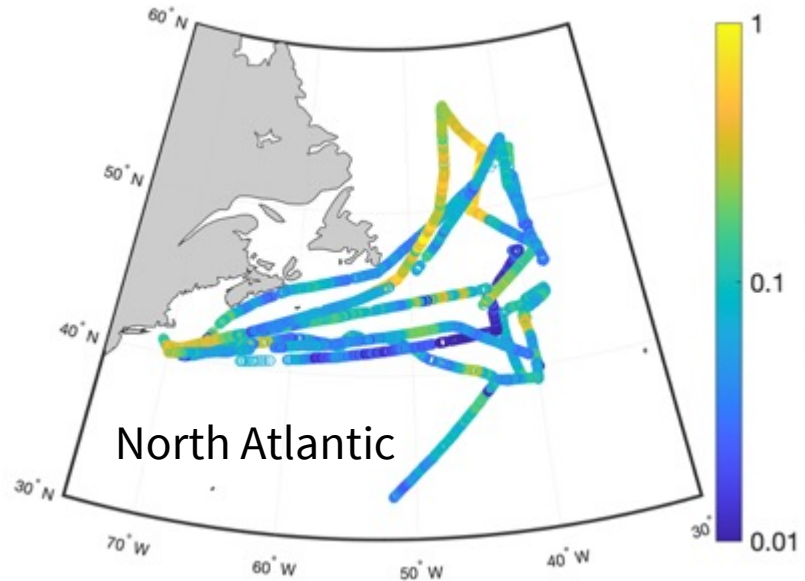
# Chlorophyll $a$ estimated from hyperspectral $a_p$ measurements



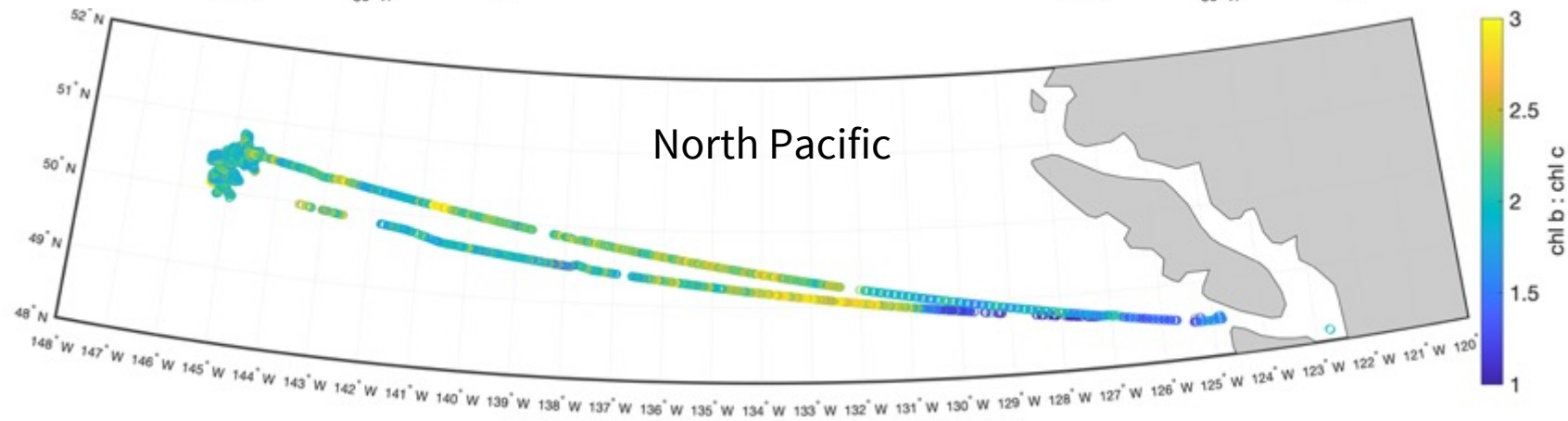
ac-s

# Phytoplankton accessory pigments estimated from hyperspectral $a_p$

Accessory pigment absolute concentrations:

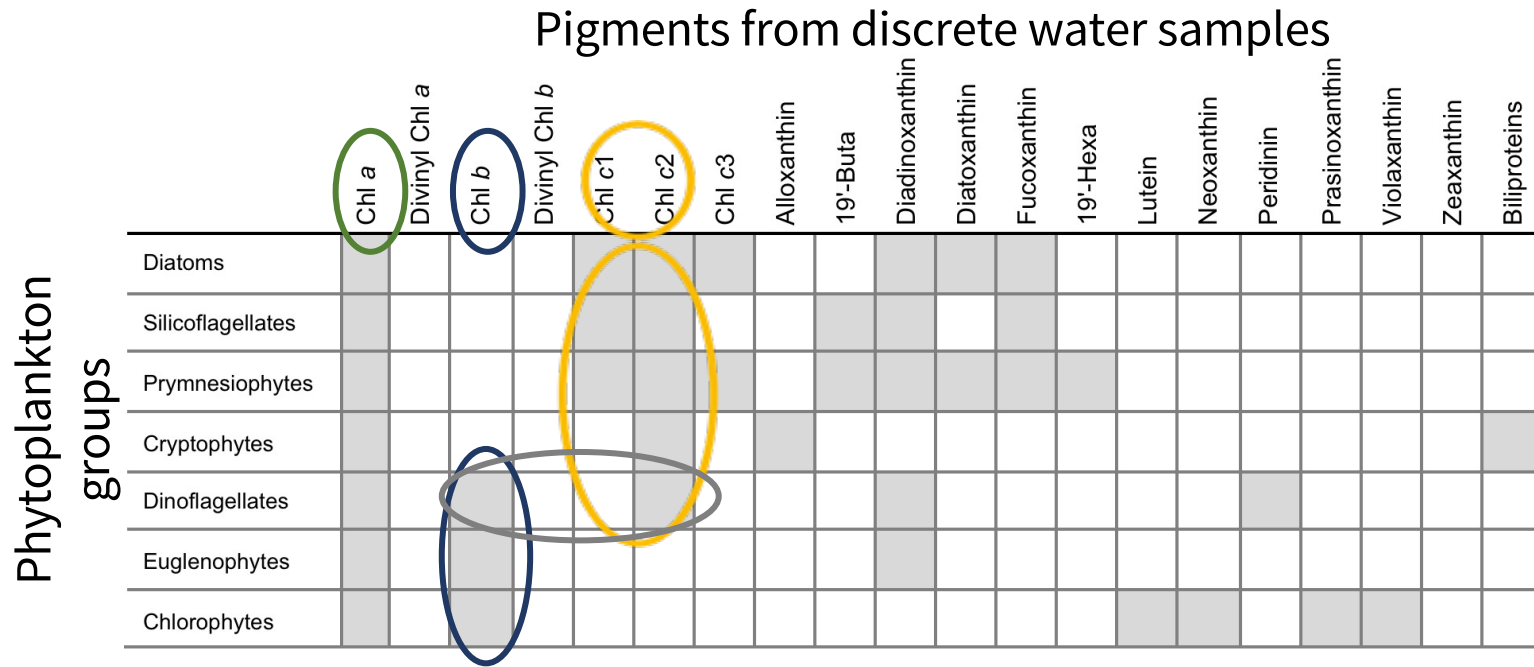


Accessory pigment ratios:



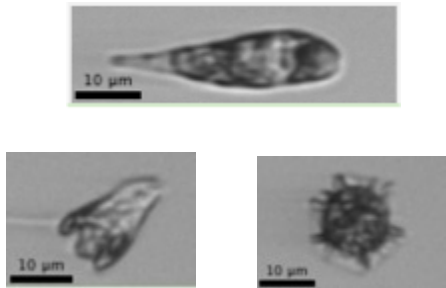


# Phytoplankton pigments attributed to different groups



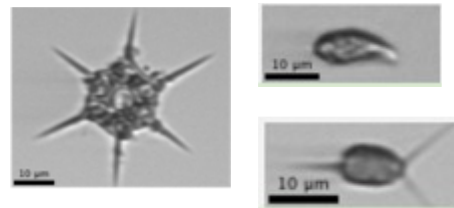
Chlorophyll b

Chlorophytes, Euglenoids

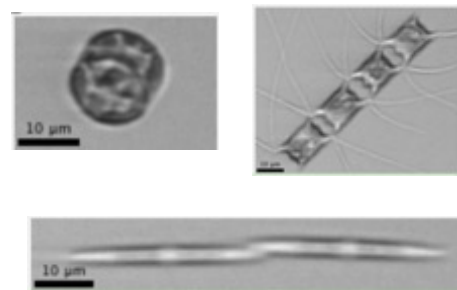


Chlorophyll c

Silicoflagellates  
Prymnesiophytes  
Cryptophytes

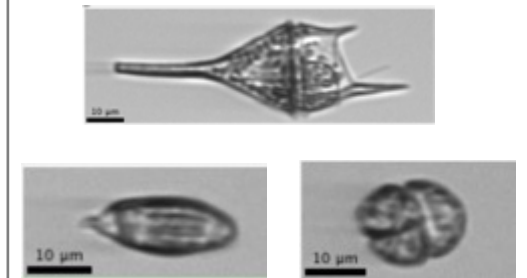


Diatoms



Chlorophylls b & c

Dinoflagellates



# Incorporating Gaussian functions into $R_{rs}(\lambda)$ inversion



$$u(\lambda) \equiv \frac{b_b(\lambda)}{a(\lambda) + b_b(\lambda)},$$

$$r_{rs}(\lambda) = g_1 u(\lambda) + g_2 u(\lambda)^2,$$

$$u = u_{meas}$$

$$g_1 = 0.0949 \text{ and } g_2 = 0.0794$$

(Gordon et al. 1988)

$$u_{mod}(\lambda) = \frac{b_{bp}(\lambda) + b_{bw}(\lambda)}{a_\varphi(\lambda) + a_{CDOM}(\lambda) + a_{NAP}(\lambda) + a_w(\lambda) + b_{bp}(\lambda) + b_{bw}(\lambda)},$$

$$a_\varphi(\lambda) = \sum_{i=1}^8 a_{gaus}(peak_i, \lambda) e^{\left(-0.5 \left(\frac{\lambda - peak_i}{\sigma_i}\right)^2\right)},$$

↓

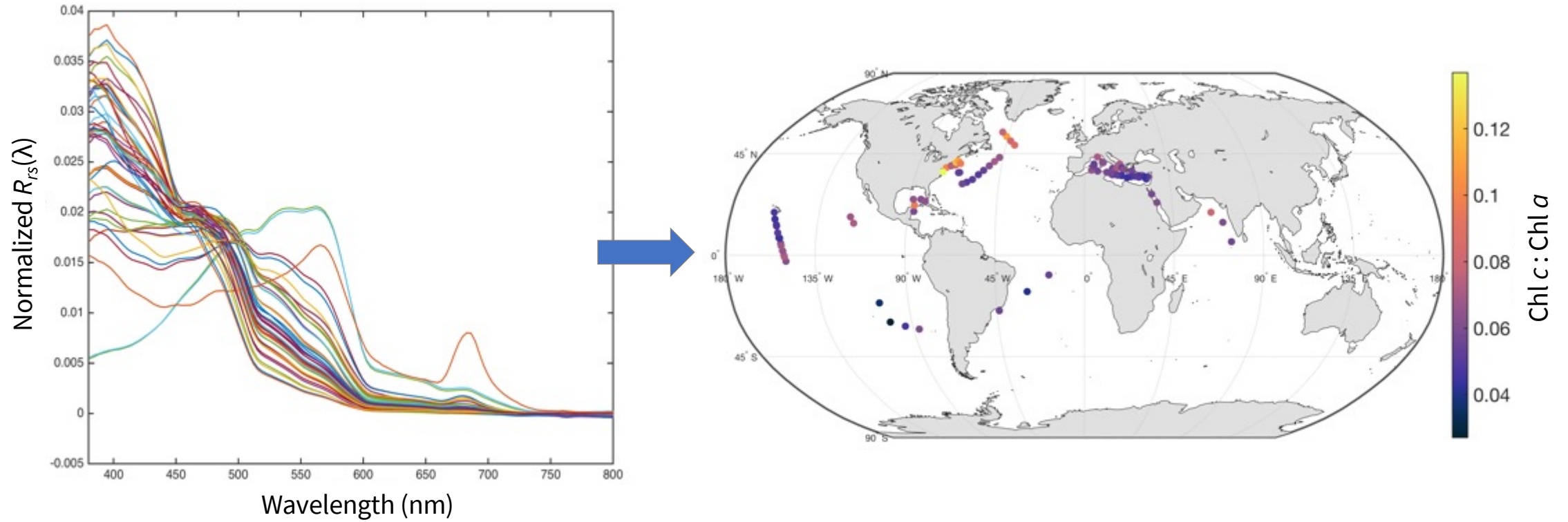
$$r_{rs}(\lambda) = \frac{R_{rs}(\lambda)}{0.52 + 1.7 R_{rs}(\lambda)}$$

Lee et al. 2002

$$\chi^2 = \sum_{i=1}^{60} \left( \frac{u_{meas}(\lambda_i) - u_{mod}(\lambda_i)}{u_{std}(\lambda_i)} \right)^2,$$

60 wavelengths  
between 400-600 nm

# Pigments estimated from $R_{rs}(\lambda)$ spectra measured *in situ*





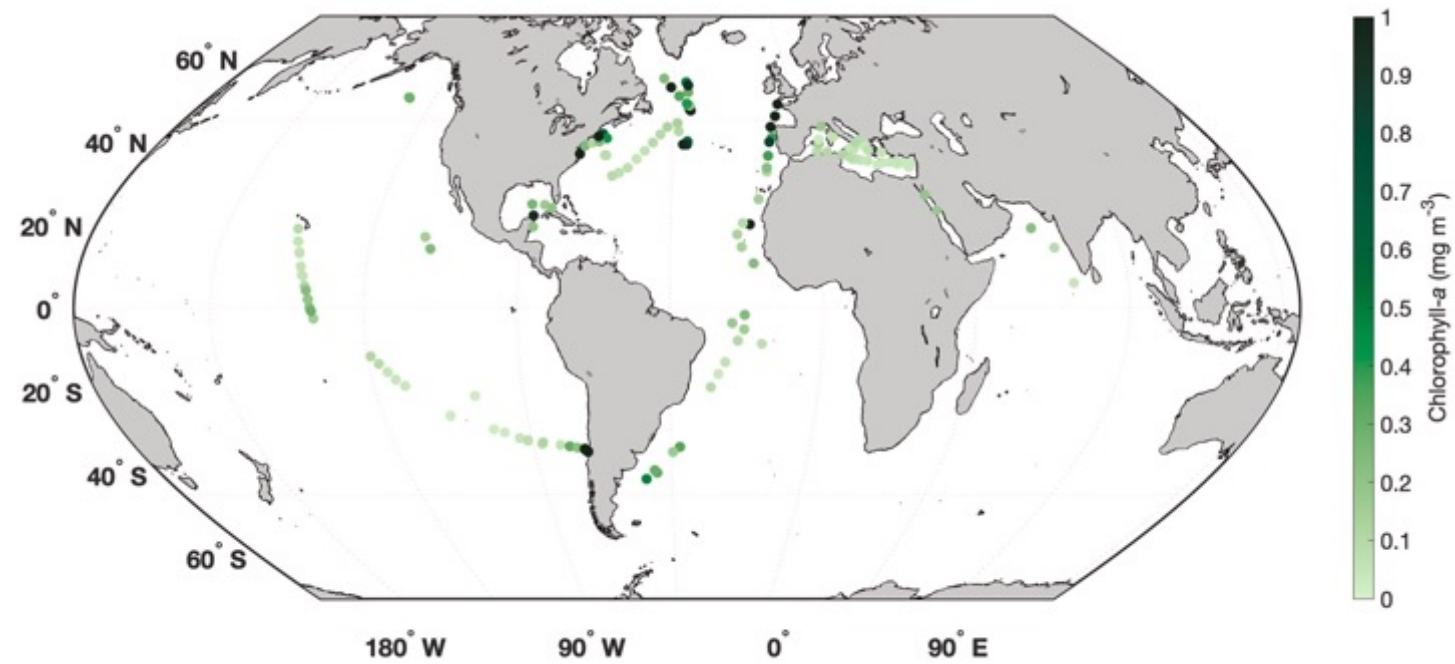
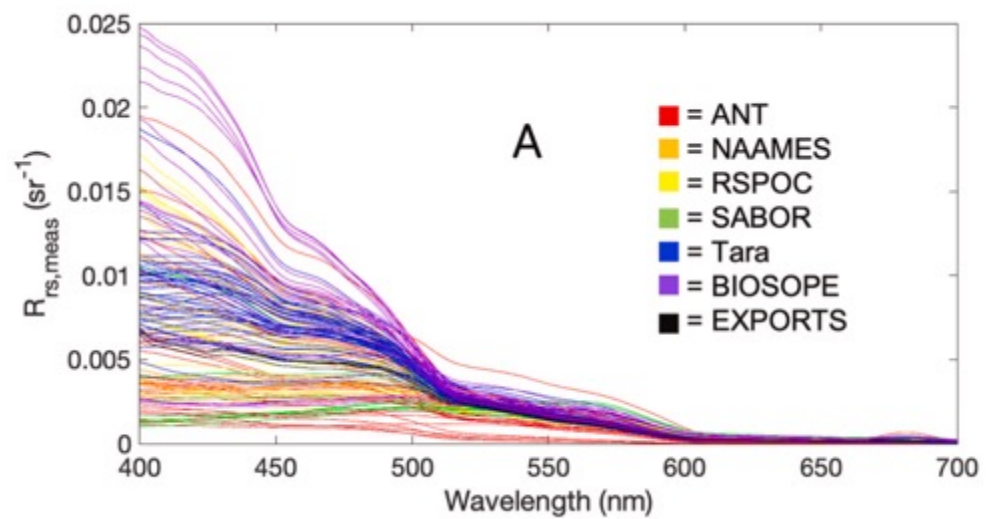
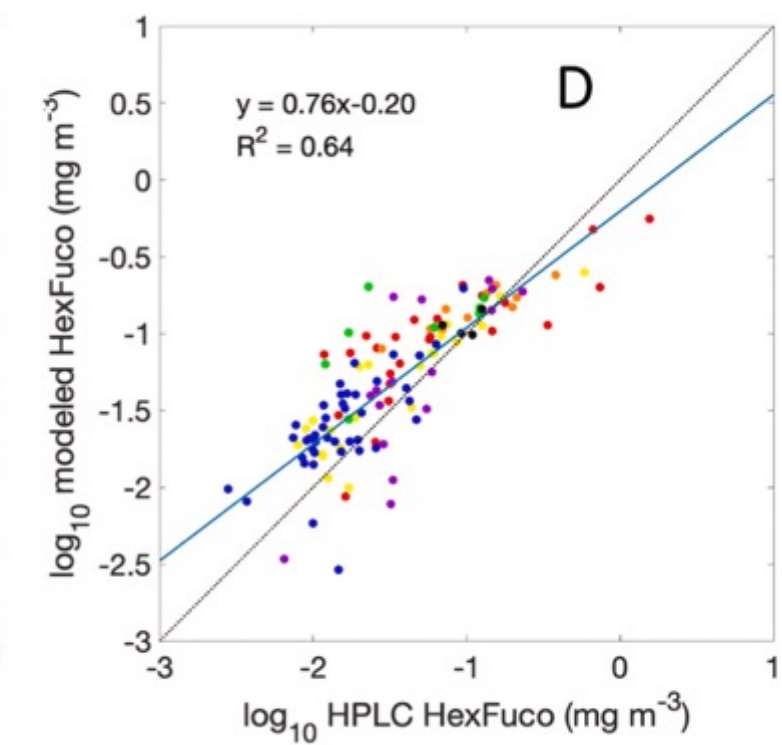
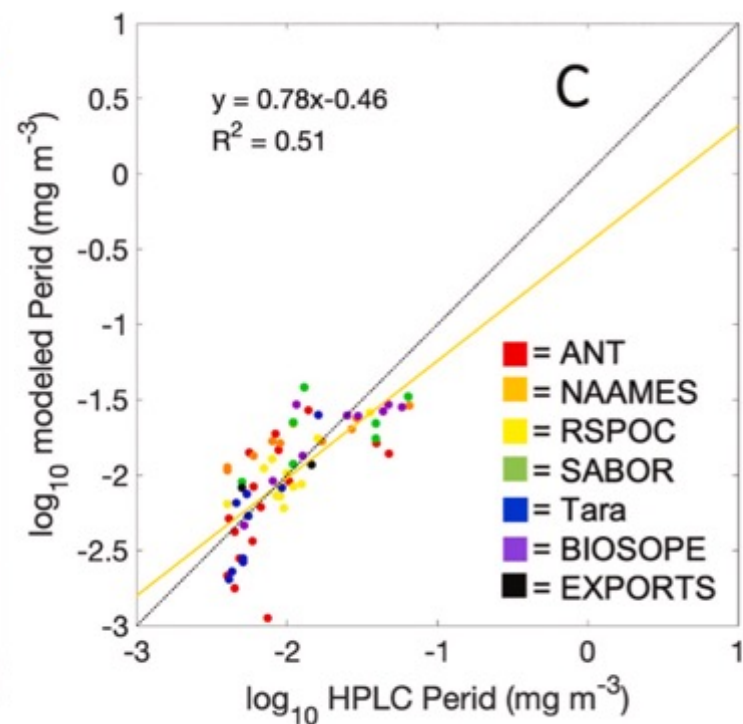
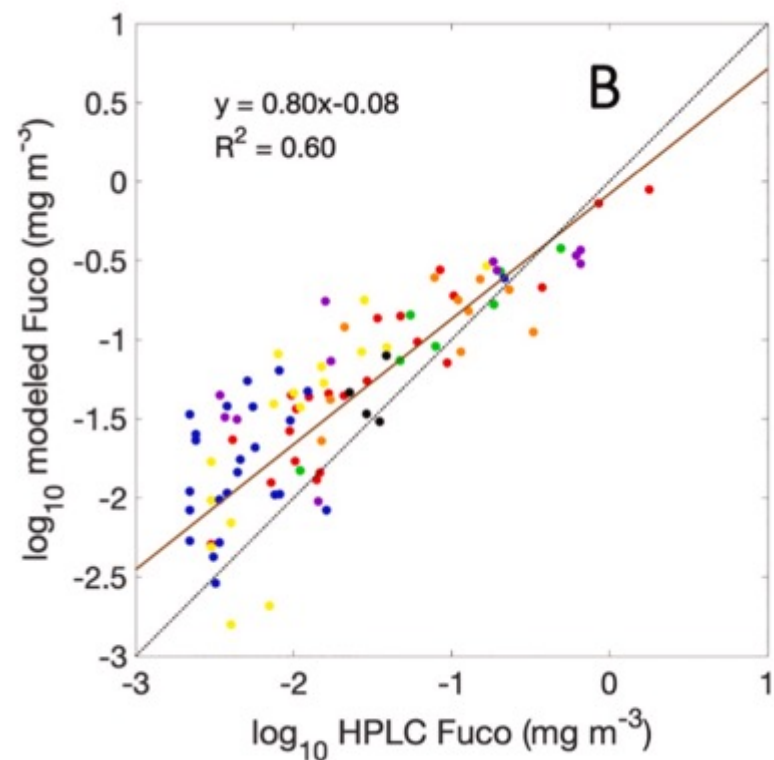
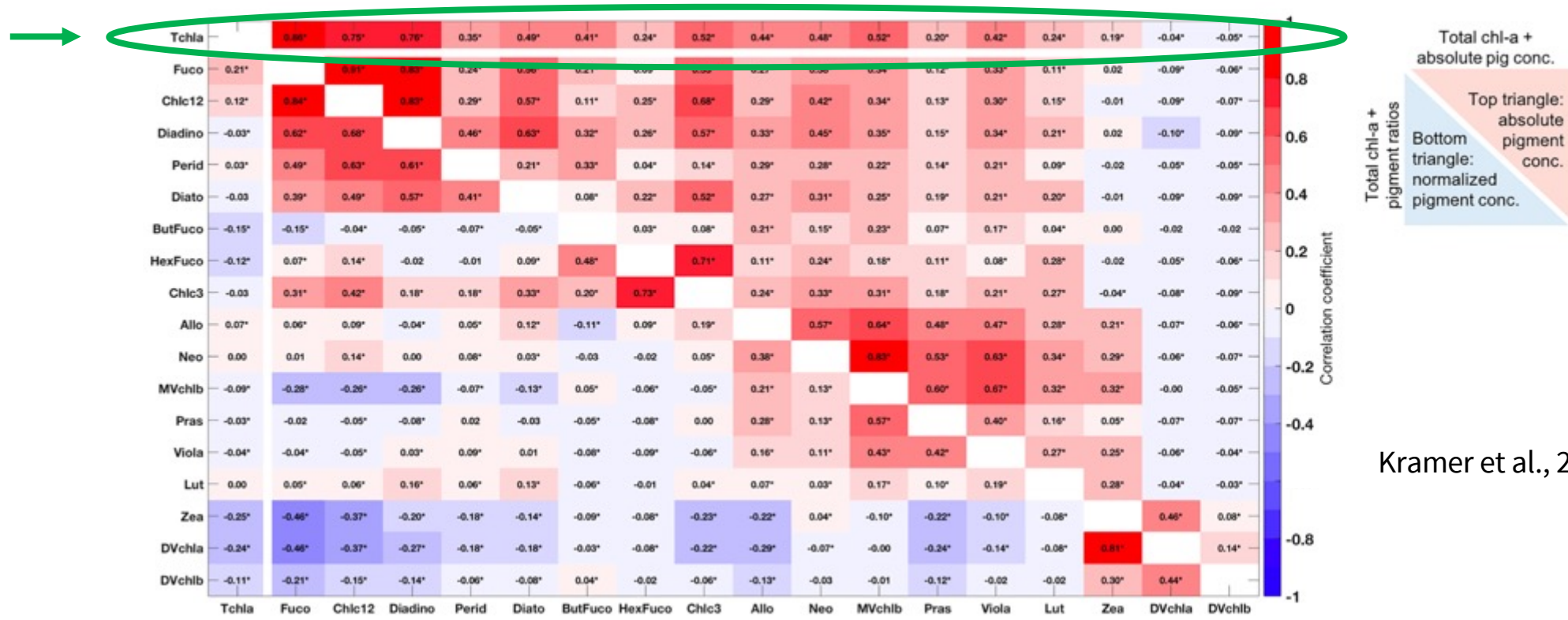


Fig. 1. Global distribution of 145 matched HPLC and hyperspectral  $R_{rs}(\lambda)$  samples, colored by chlorophyll-a concentration (Tchl<sub>a</sub>).

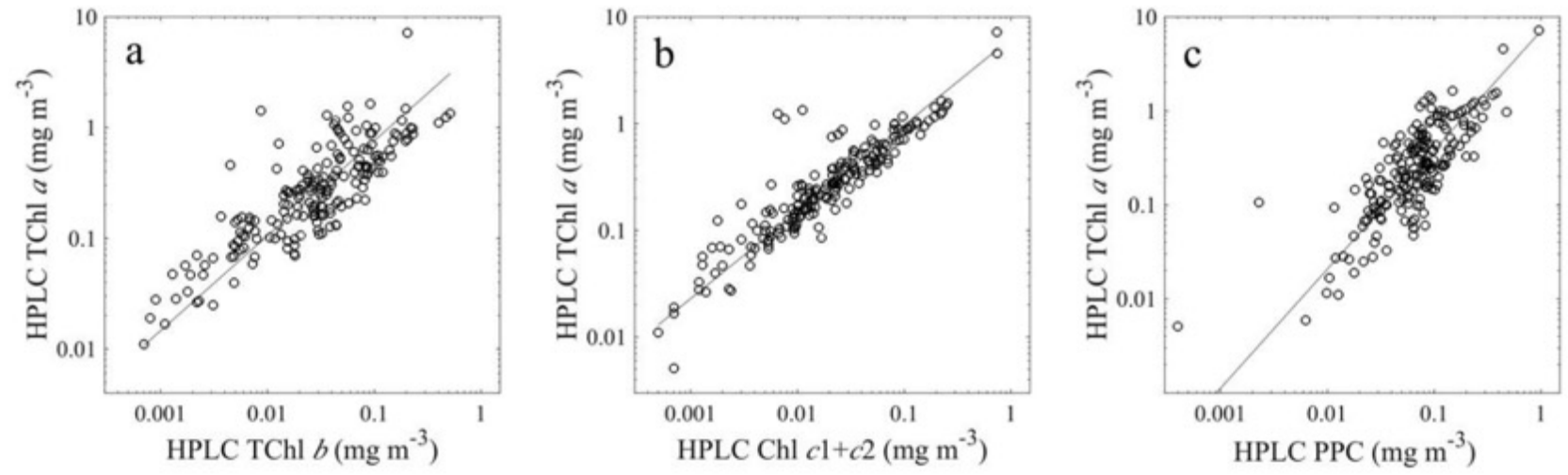


Pigment	Mean R <sup>2</sup>	SD R <sup>2</sup>	Mean normalized MAD	SD normalized MAD
Allo	0.40	0.19	1.221	0.400
But	0.62	0.16	0.588	0.185
Chlc3	0.68	0.13	0.639	0.212
Chlc12	0.70	0.13	0.703	0.235
DVchla	0.55	0.12	0.594	0.103
Fuco	0.65	0.15	0.844	0.274
Hex	0.54	0.16	0.692	0.201
MVchlb	0.42	0.19	0.975	0.295
Neo	0.42	0.21	1.127	0.354
Perid	0.49	0.13	0.783	0.166
Tchla	0.72	0.15	0.498	0.127
Viola	0.38	0.18	1.101	0.370
Zea	0.37	0.10	0.472	0.071

# But most pigments are correlated with Chl $a$ ...



Kramer et al., 2019



Chase et al., 2017



# Considerations of error, & “going beyond Chl $a$ ”

From Cael et al. (2020):

- Error is the difference between having four to five DoF rather than  $>60$ , and the difference between being able to meaningfully invert for four spectra versus 44
- Some errors such as random electronic noise can be reduced by averaging many measurements in time or space. Others, such as a bias in calibration, cannot.
- While all optical variation in the water cannot be said to fall along a single axis, it does appear that much of the variation in the surface covaries with [Chl]. Thus, the interest in going “beyond chlorophyll” can be considered an interest in deviations from this axis.
- Polarization will help better separate oceanic and atmospheric contributions to the total signal, and UV will help better separate CDOM, NAP, and phytoplankton contributions to the oceanic signal. These deviations are by definition second order—though we note emphatically that this does not make them unimportant or uninteresting!
- Take home: Judicious use of available DoF; use basis vectors that are specific to your needs in the case of a regional or tuned algorithm

Take-home messages re: hyperspectral measurements:

The question is not as simple as “*how much information can we extract from hyperspectral measurements?*”, but rather,

“*which approaches and methods that take advantage of the added information in hyperspectral measurements are relevant to my research question(s)?*”

With limited degrees of freedom in hyperspectral measurements alone, consider the incorporation of other types of optical and/or environmental data during algorithm development and application, as well as spatial and temporal resolution requirements.

**Recent work, new approaches, and expanding  
data types & tools**



# phytclass: A pigment-based chemotaxonomic method to determine the biomass of phytoplankton classes

Alexander Hayward <sup>1,2\*</sup> Matthew H. Pinkerton <sup>1</sup> Andres Gutierrez-Rodriguez <sup>1,3</sup>

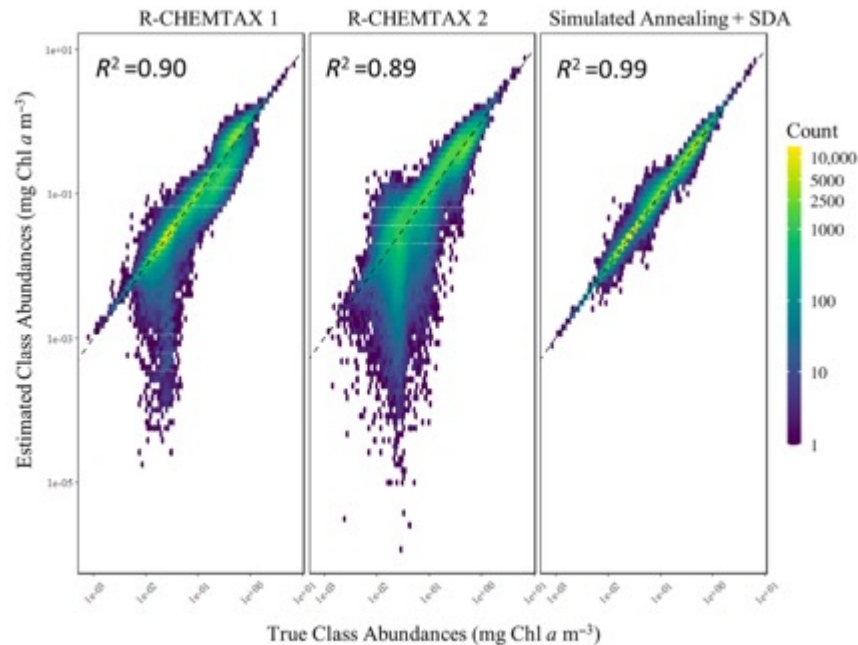
<sup>1</sup>National Institute of Water and Atmospheric Research, Wellington, New Zealand

<sup>2</sup>University Of Otago, Dunedin, New Zealand

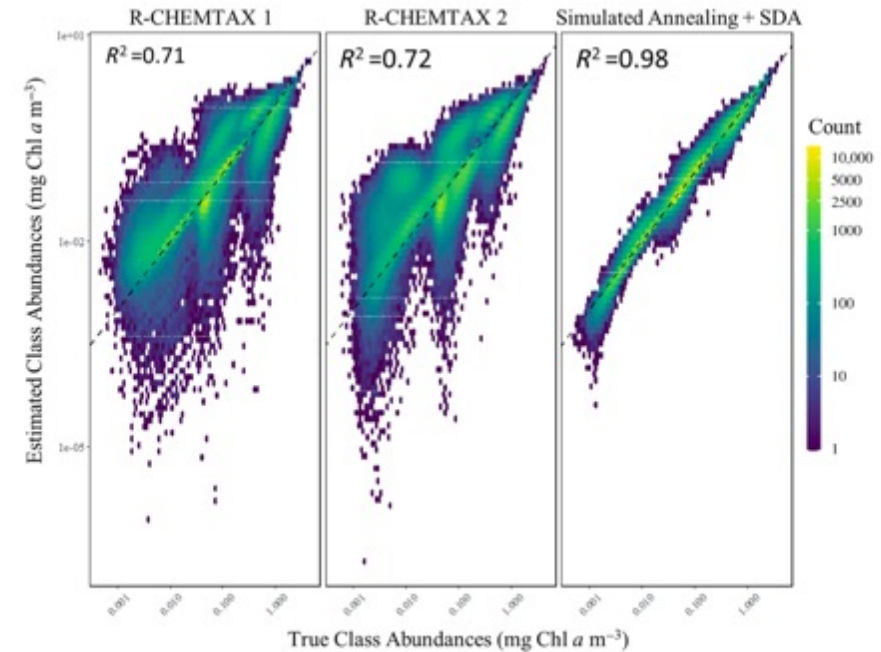
<sup>3</sup>Instituto Español de Oceanografía, Centro Oceanográfico de Gijón, Gijón, Spain

*Limnol. Oceanogr.: Methods* 2023

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**Fig. 7.** Density plot of true class abundances and predicted class abundances for R-CHEMTAX-1, R-CHEMTAX-2, and simulated annealing + SDA approaches in synthetic dataset-1.



**Fig. 13.** Density plots of true class abundances and predicted class abundances for R-CHEMTAX-1, R-CHEMTAX-2, and simulated annealing + SDA approaches using synthetic datasets in synthetic dataset-2.

→ New method to estimate phytoplankton groups from pigments

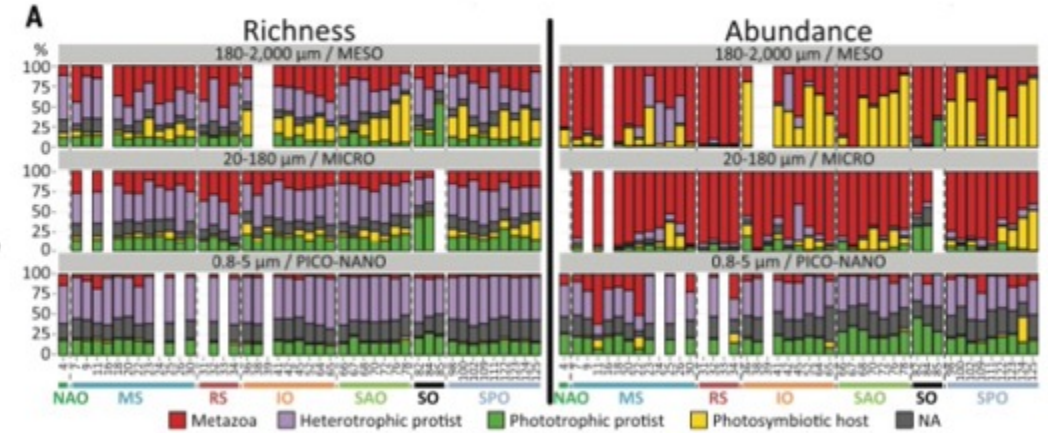
# Molecular methods

Quick method summary: Large sample (2-10L) collected, filtered, DNA is extracted, and “barcode” genes are targeted for amplification and sequencing

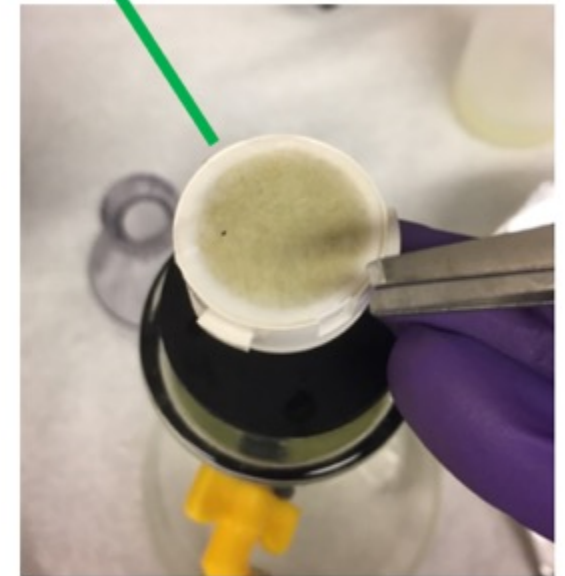
Strengths: High taxonomic resolution (often to genus or species level), can compare well to other methods (microscopy, pigments)

Weaknesses: Primers may be limited for some groups, gene copies  $\neq$  abundance

Output: *Relative* sequence abundances



de Vargas et al., 2015

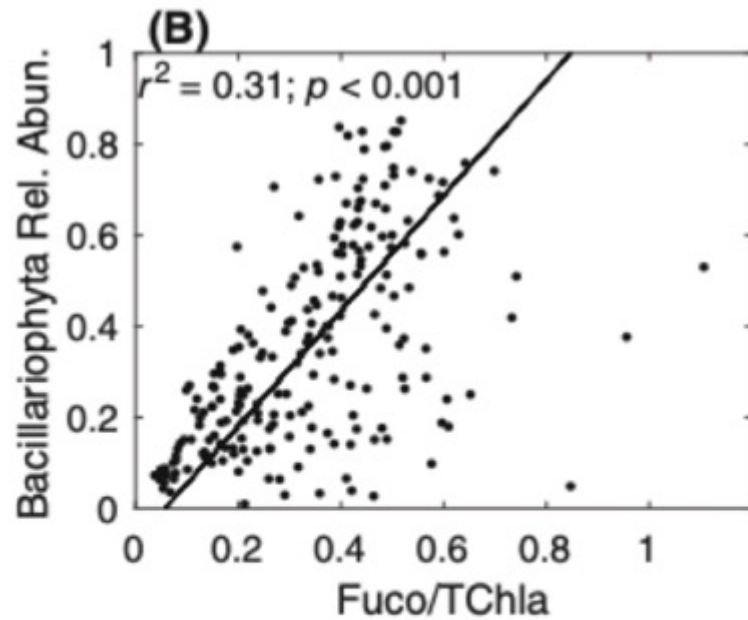


Slide credit: S. Kramer

# Molecular methods

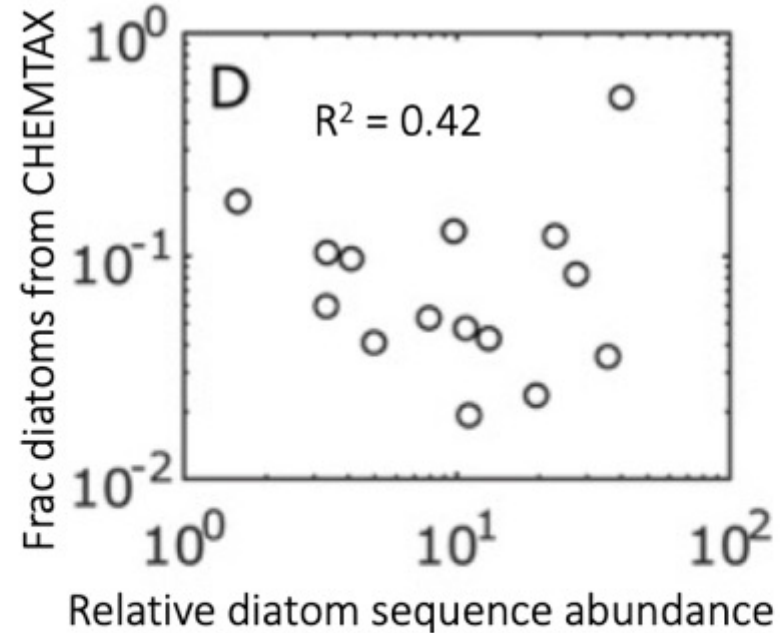
Comparing DNA metabarcoding to other methods: results can really depend on ecosystem dynamics

Santa Barbara Channel



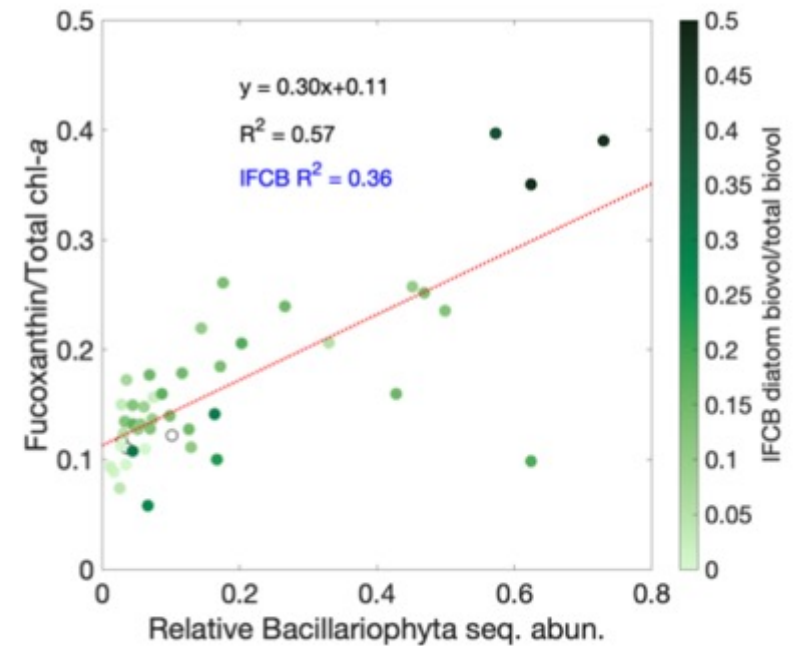
Catlett et al., 2022

West Antarctic Peninsula



Lin et al., 2019

Open ocean (N. Atl + N. Pac)

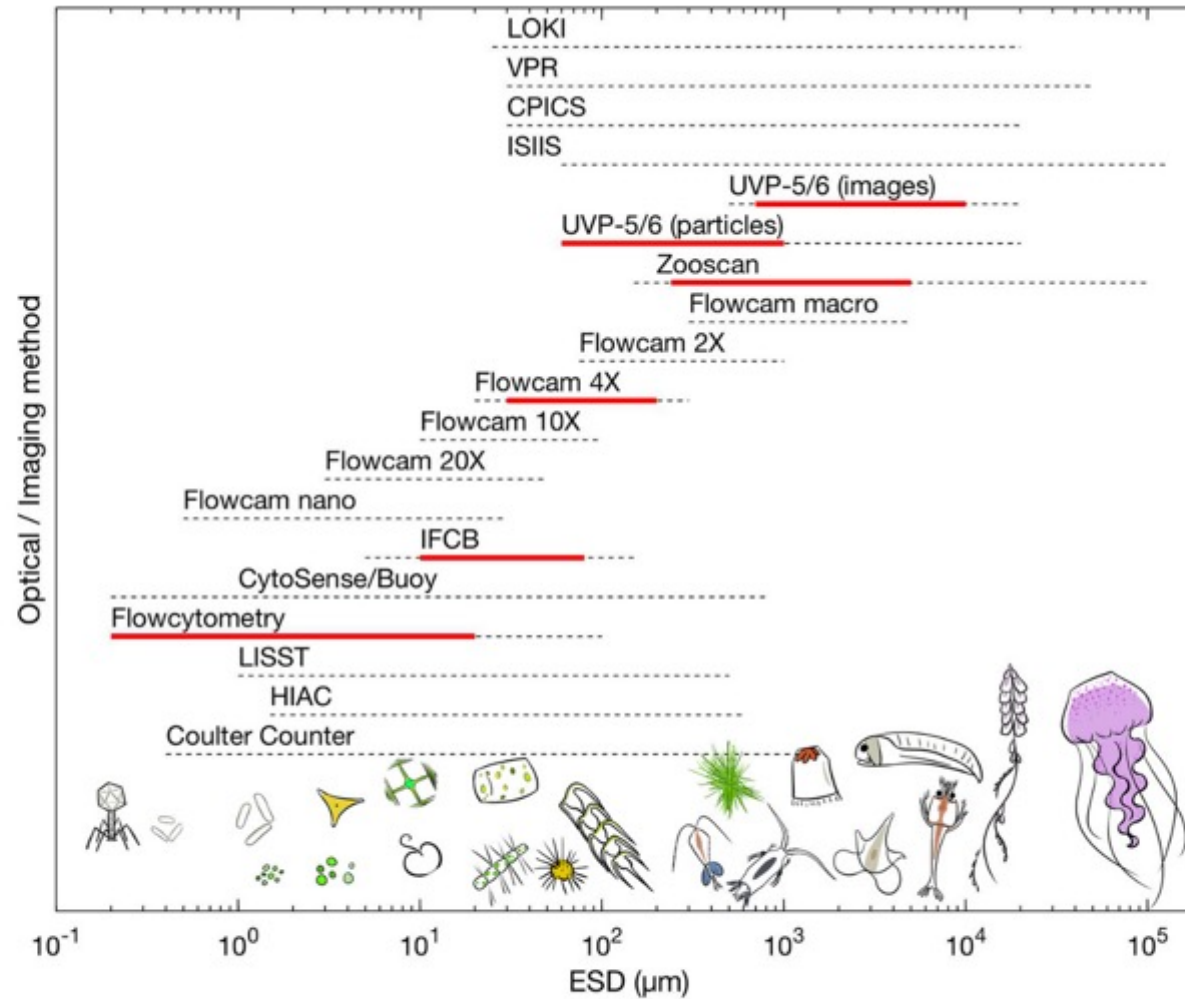


Kramer et al., *in prep*

Slide credit: S. Kramer



# Globally Consistent Quantitative Observations of Planktonic Ecosystems

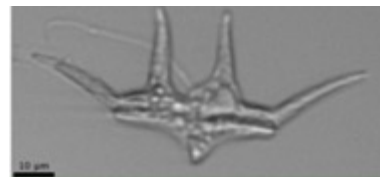
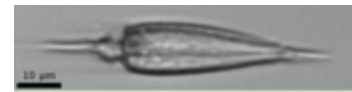
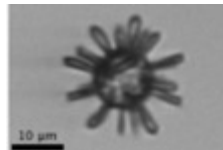
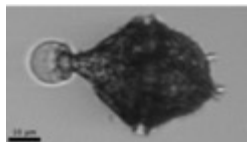
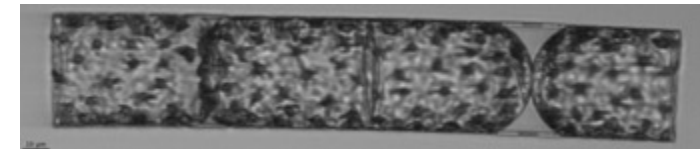
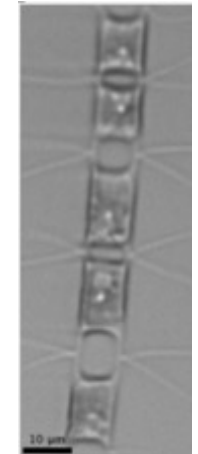
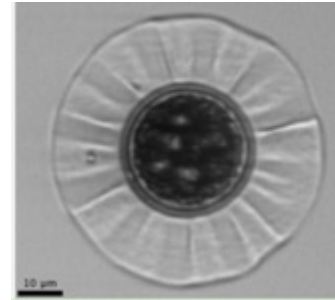
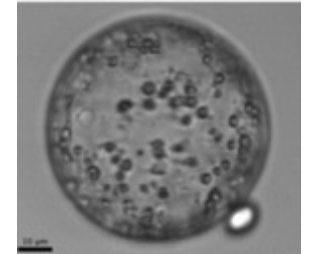
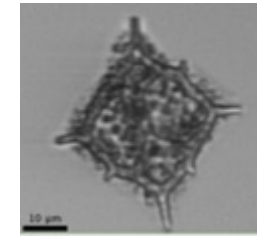
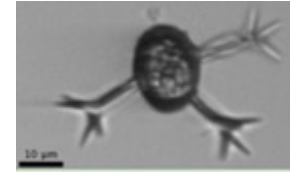
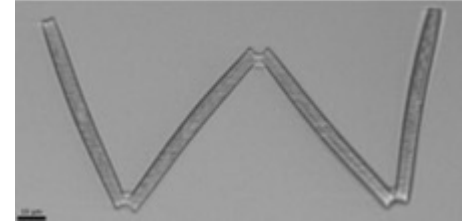
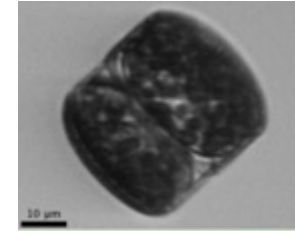
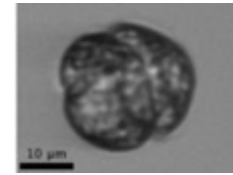
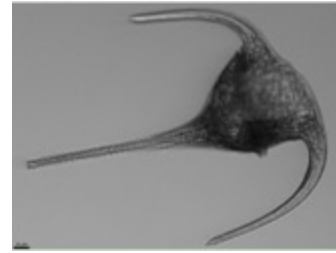


**FIGURE 1** | Comparison of the total size range of plankton (in equivalent spherical diameter; ESD) that available optical and imaging methods can sample. Dashed lines represent the total operational size range from commercial information while the red line represent the practical size range which is efficient to obtain quantitative information, for an example see **Figure 2**. Drawings by Justine Courboules.

# Plankton imagery used to determine community composition of cells ~8-150 $\mu\text{m}$

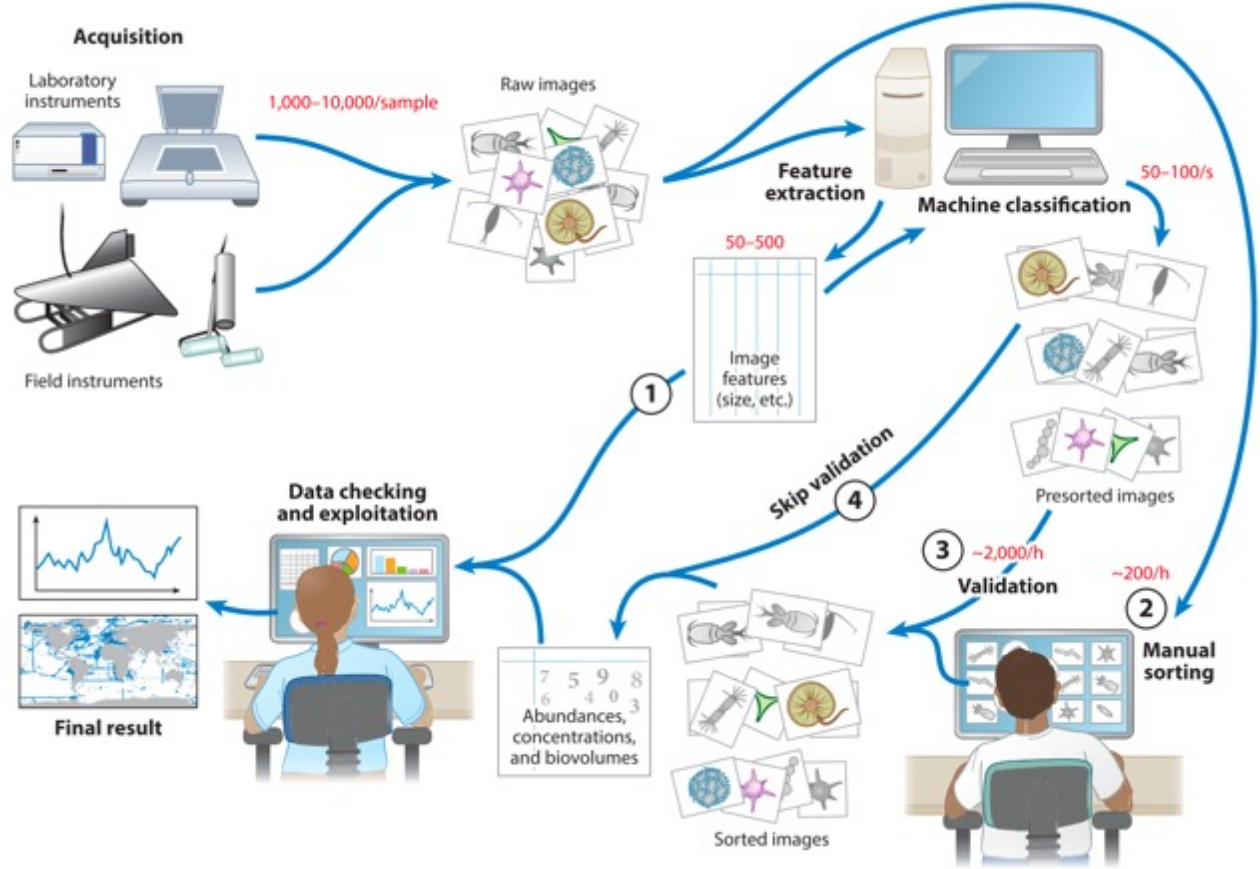


Imaging FlowCytobot (IFCB)



# Machine Learning for the Study of Plankton and Marine Snow from Images

Jean-Olivier Irisson,<sup>1</sup> Sakina-Dorothee Ayata,<sup>1</sup> Dhugal J. Lindsay,<sup>2</sup> Lee Karp-Boss,<sup>3</sup> and Lars Stemann<sup>1</sup>

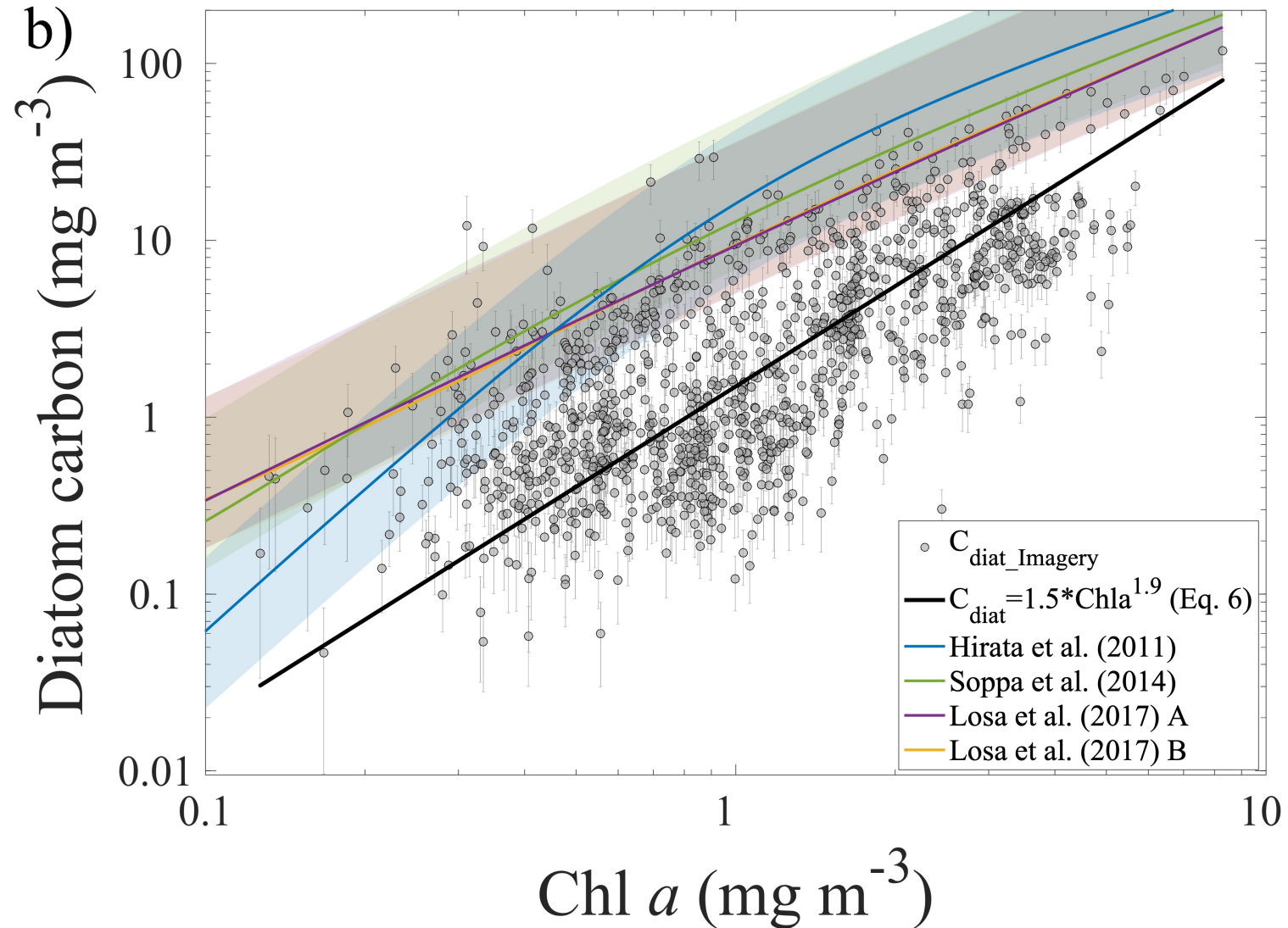


→ Note that deep learning networks do not necessarily require a separate feature extraction step

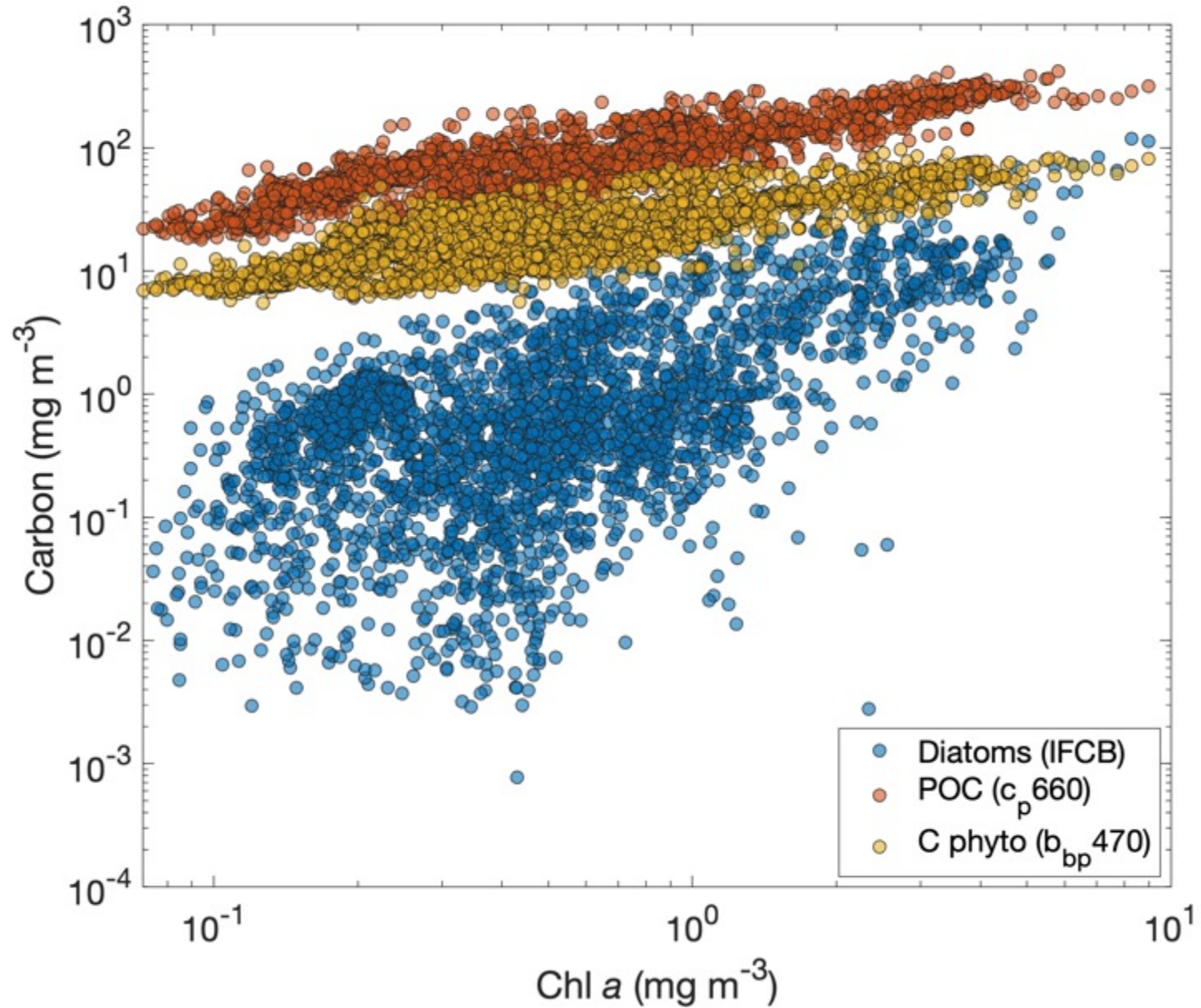
<https://github.com/ifcb-utopia> - Tools for processing IFCB images including a CNN demo w/a “toy” dataset



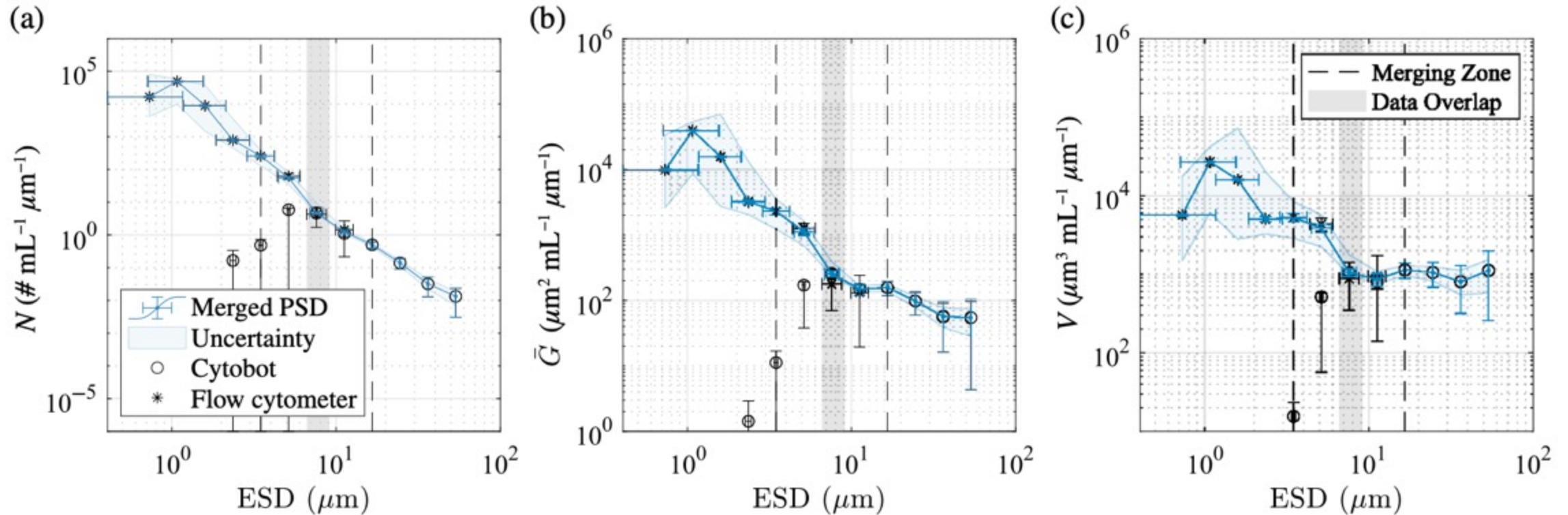
# Variability in diatom carbon across chlorophyll *a* concentrations



# Variability in diatom carbon, phytoplankton carbon, and POC across chl $a$

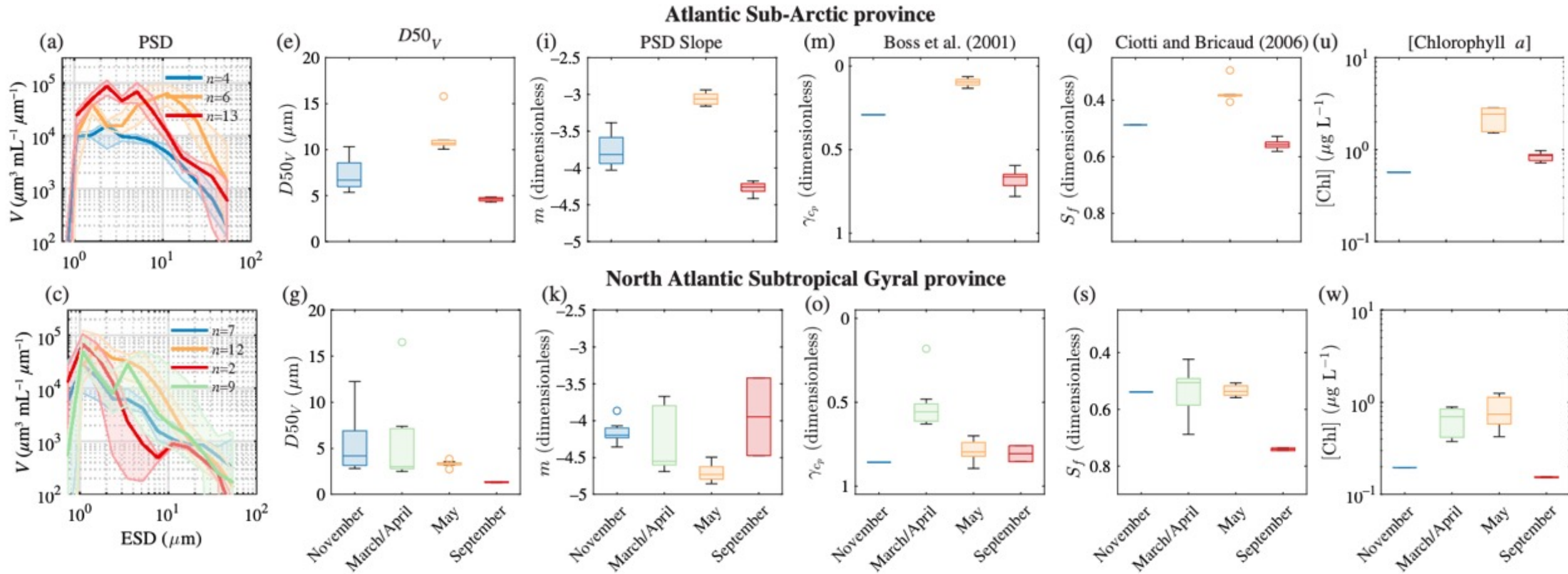


# Merged cytometry-based phytoplankton size distributions





# PSDs and optical size proxies



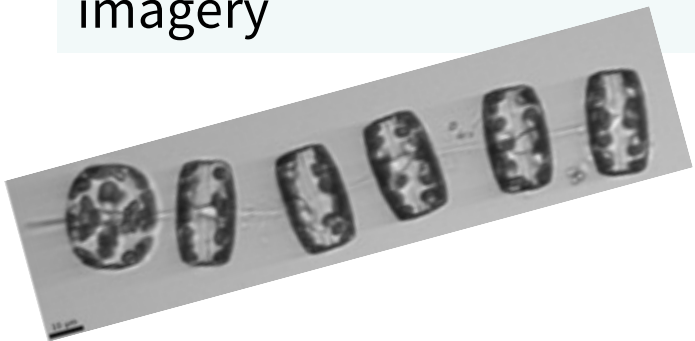


# Complementary machine learning workflows

Prepare phytoplankton imagery data and train CNNs

Apply trained network to unlabeled phytoplankton images

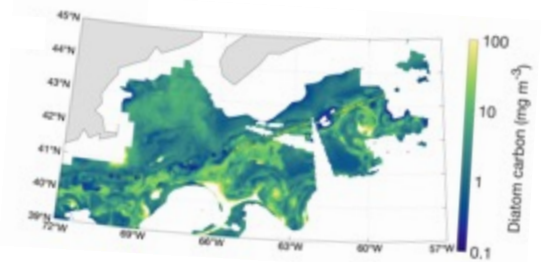
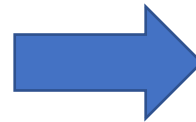
Database of classified plankton imagery



Prepare in situ datasets of environmental measurements & optical properties

Assess how well data represent global conditions

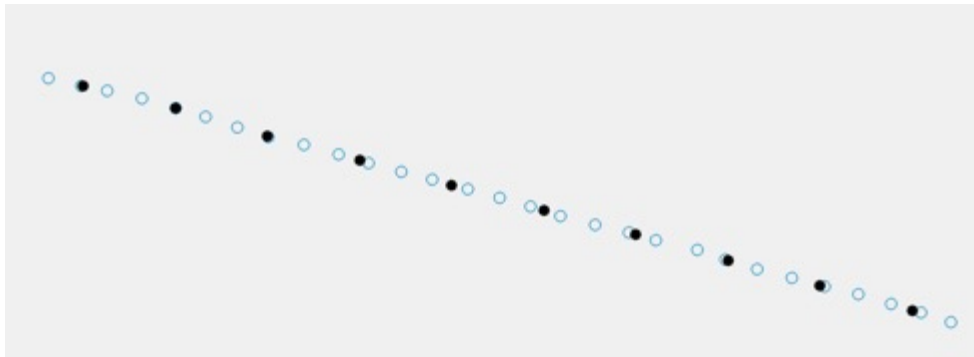
Train ML networks to estimate diatom biomass from environmental/optical data



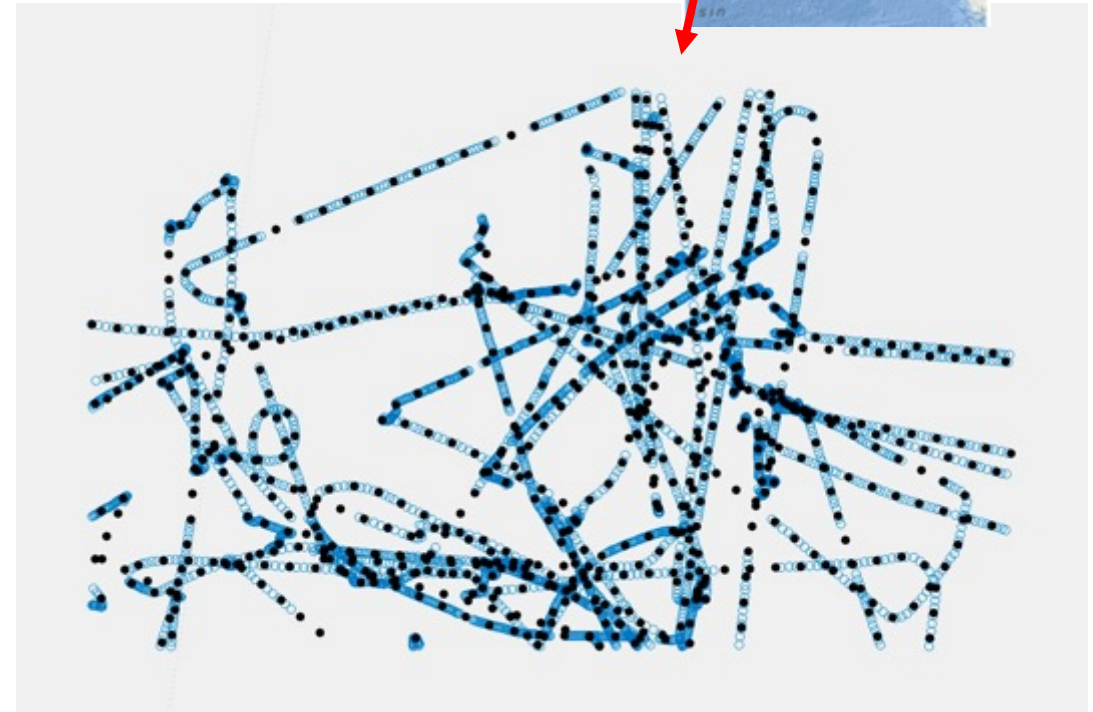
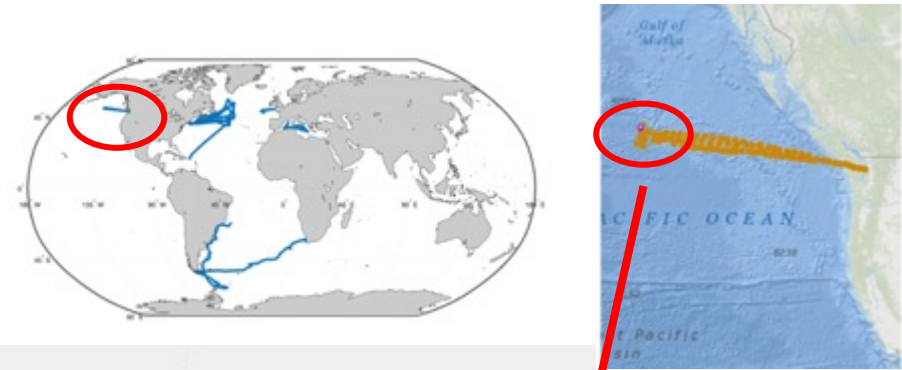
# Averaging & merging all input data to a 1-km along-track “grid”



Above: example underway data 1-min binned data  
Below: 1-min binned (open blue) & 1-km grid (black)

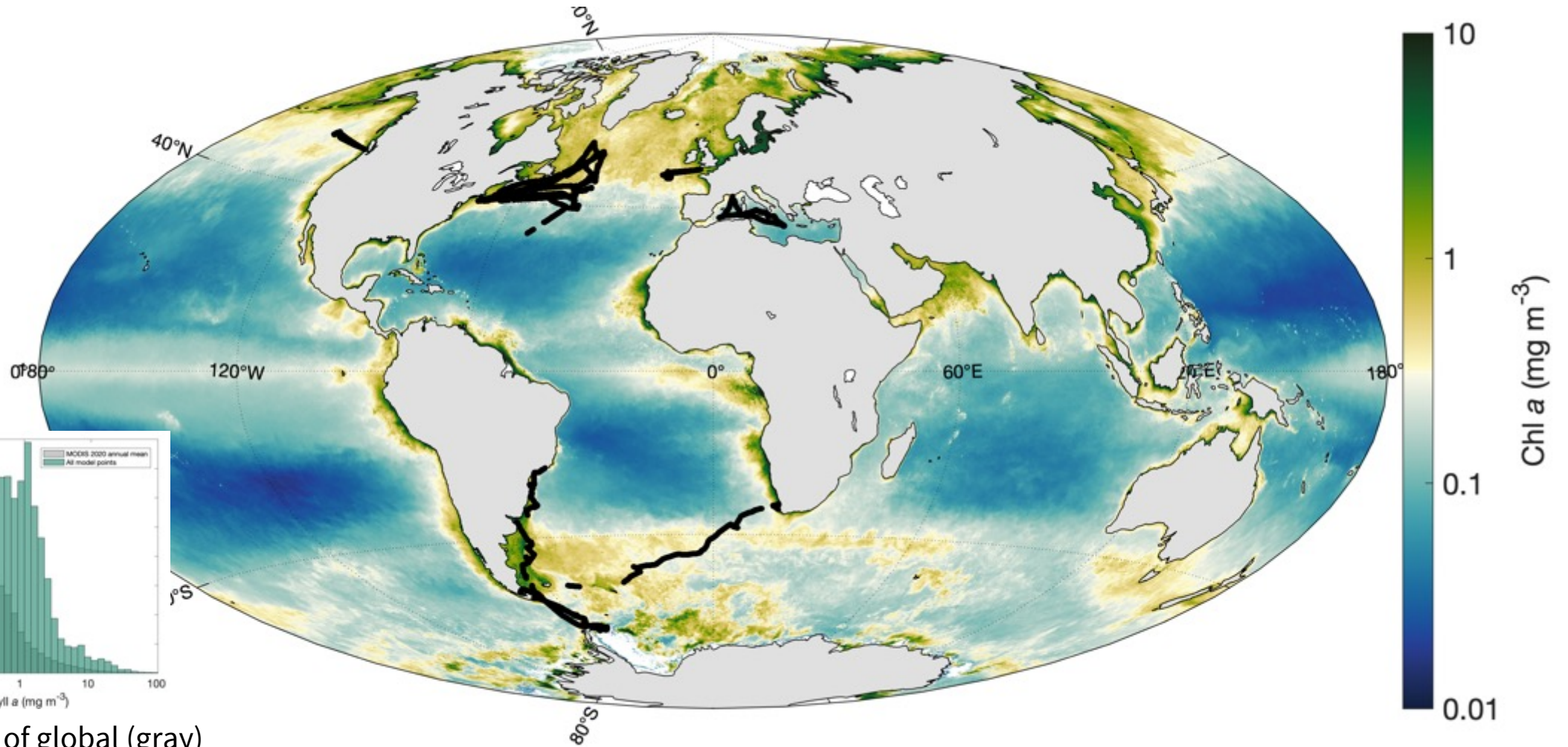


- Mean and standard deviation are stored during averaging for subsequent error propagation and uncertainty analysis
- Various types of datasets can be easily compared based on grid indices



Example when the ship is focusing on one location or feature in the ocean

# How well do our model training data represent global conditions?



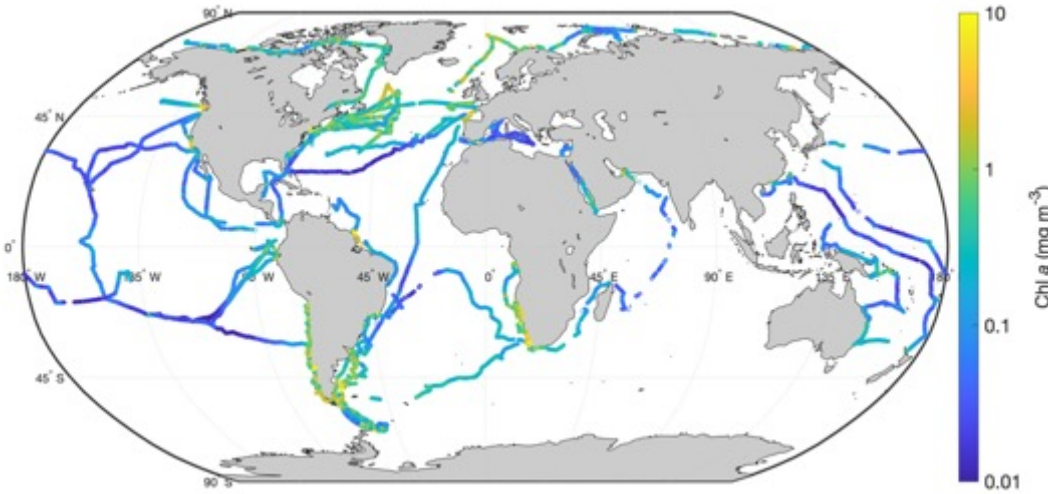
Distributions of global (gray) and algorithm training (green) chlorophyll *a*

NASA MODIS Aqua 2020 annual mean

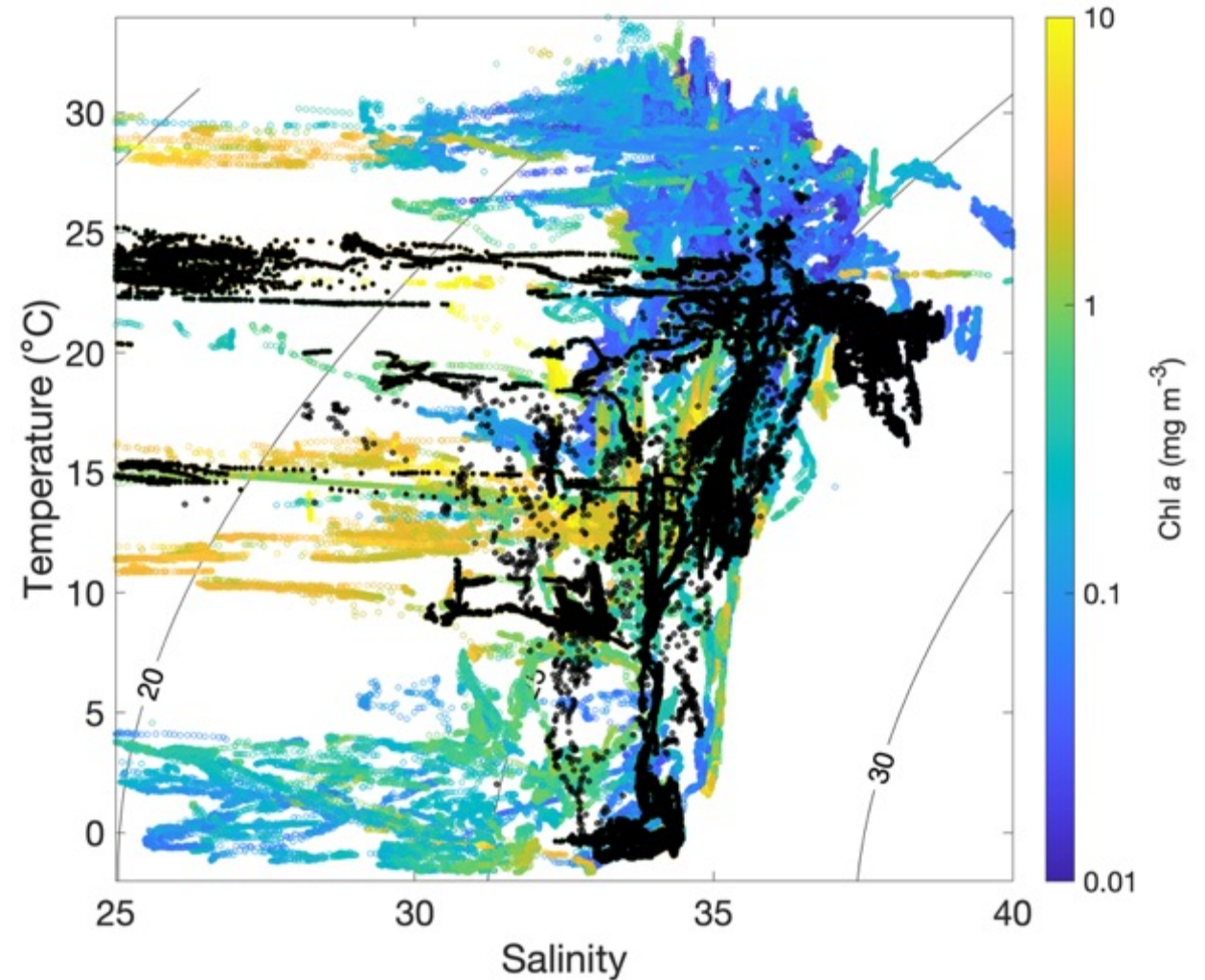
Dots show locations with both plankton imagery data & model input variables



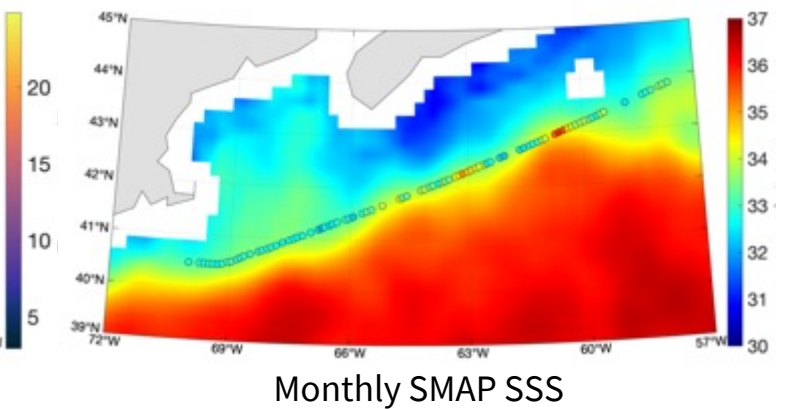
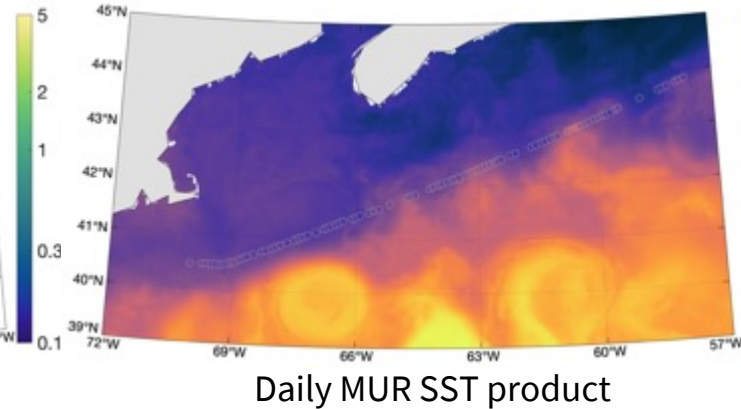
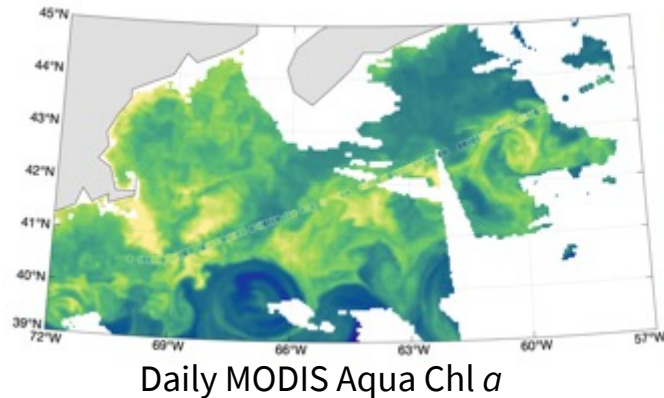
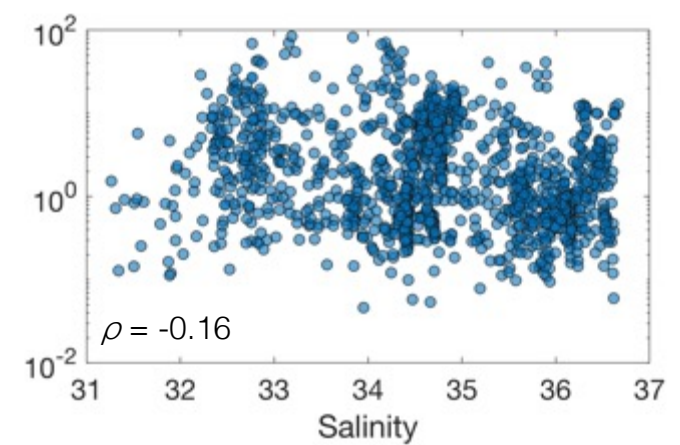
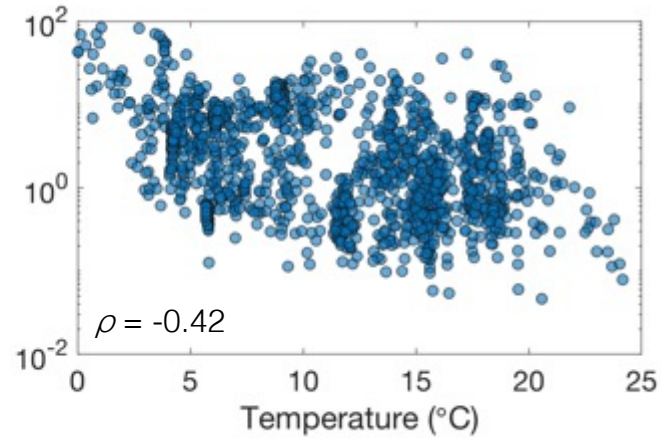
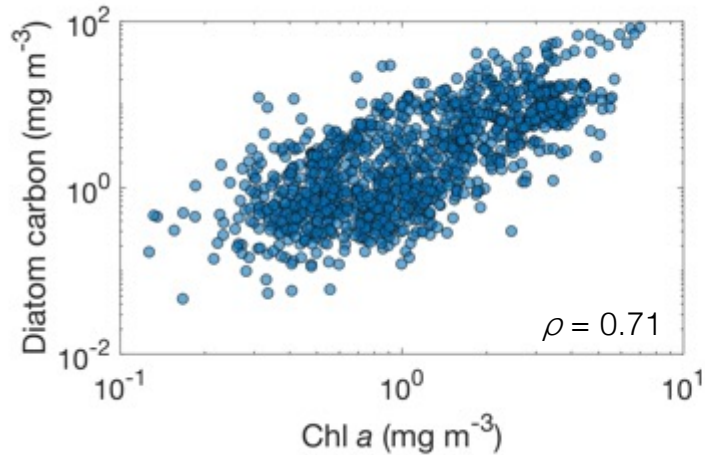
# How well do our model training data represent large-scale variability?



- Black dots at right represent cruises with both input data and plankton imagery and thus can be used for network training
- Some portions of the TS/Chl space are underrepresented



# Addition of ancillary environmental data

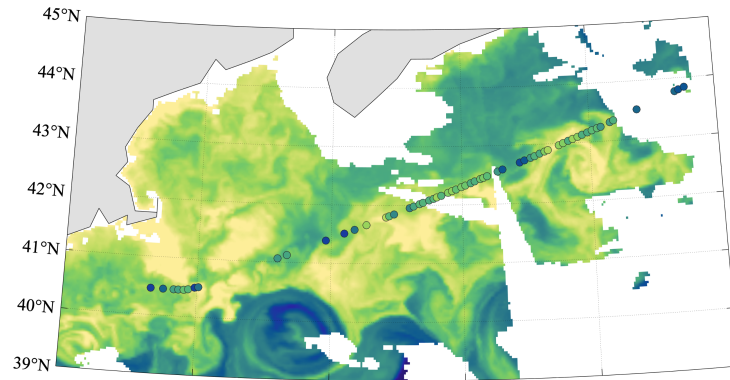


- Diatom carbon and environmental variables are correlated but with high variability
- Chl  $a$ , temperature, and salinity are all available from satellite

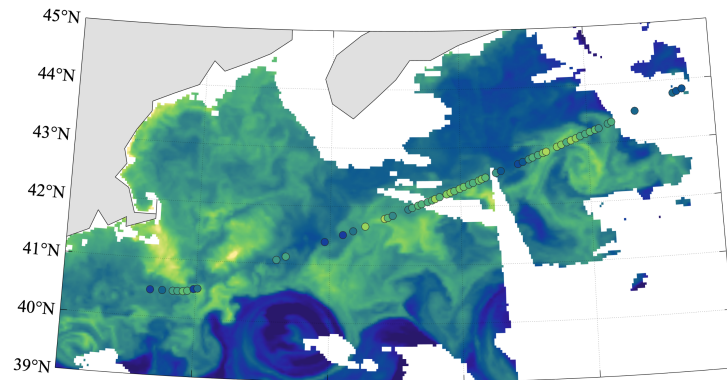


# Environmental data + plankton imagery + machine learning

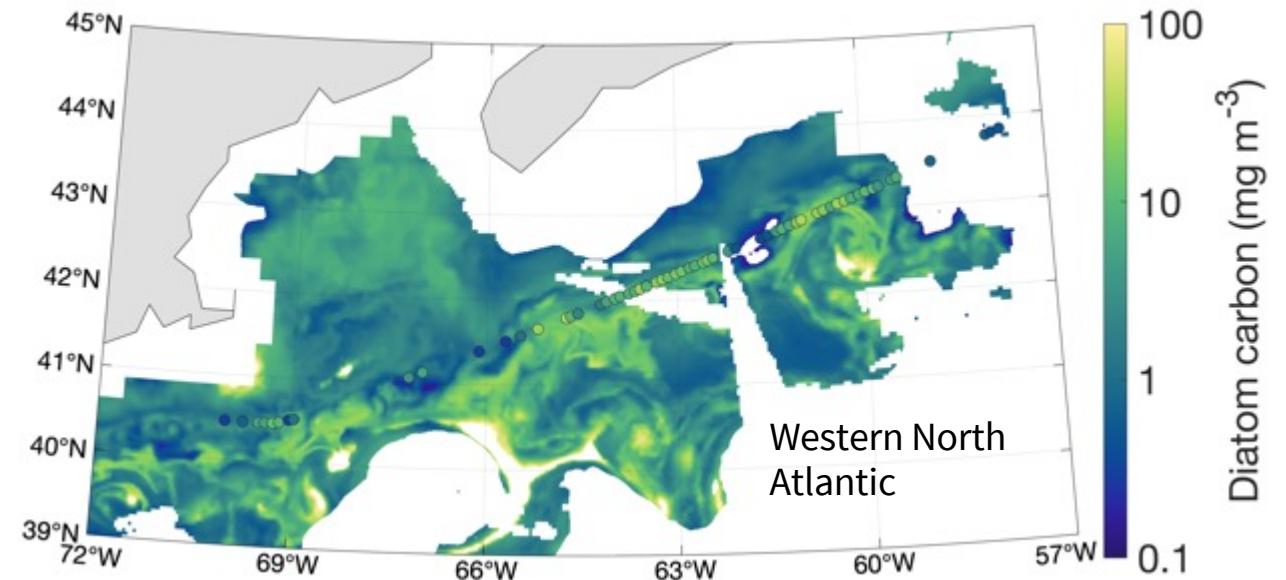
Previous Chl *a*-based method (Hirata et al. 2011)



Updated Chl *a*-based method



Neural network-based method



Chase et al. 2022

- Different spatial patterns are observed compared to estimates of diatoms solely from Chl *a*
- Full error propagation: uncertainty in diatom carbon = 65%



# Uncertainty calculations are necessary!

Cell biovolume estimate

Diatom ID accuracy

$$\mathbf{Unc}_{\text{data}} = \sqrt{0.17^2 + 0.18^2 + 0.1^2 + 0.29^2} = 0.39,$$

Statistical counting error

Chl *a* uncertainty

$\mathbf{Unc}_{\text{data}}$

Neural network uncertainty

$$\mathbf{Unc}_{\text{NN}} = \sqrt{0.39^2 + 0.52^2} = 0.65,$$

At low estimated diatom carbon values, the absolute error dominates over the relative error, and thus  $\mathbf{Unc}_{\text{NN}} = \max(1.05 \text{ mg m}^{-3}, 65\%)$

Is it good enough???

# Overcoming the Challenges of Ocean Data Uncertainty

*In oceanography, as in any scientific field, the goal is not to eliminate uncertainty in data, but instead to better quantify and clearly communicate its size and nature.*

By Shane Elipot, Kyla Drushka, Aneesh Subramanian, and Mike Patterson 12 January 2022

“

*An ocean data set may otherwise be of the highest scientific quality, but if quantified uncertainties do not accompany it, it will not be useful to scientists or other stakeholders.*

“

*Some concepts that are applicable to bench measurements are difficult to translate to the oceanographer's laboratory—the ocean—because the ocean and the climate system in which it is embedded are constantly changing.*



This view from the International Space Station shows sea ice floes and eddy currents near the coast of Russia's Kamchatka Peninsula. Credit: NASA JSC Earth Science and Remote Sensing Unit

<https://eos.org/opinions/overcoming-the-challenges-of-ocean-data-uncertainty>

# (near) real-time use of optics to locate features of interest

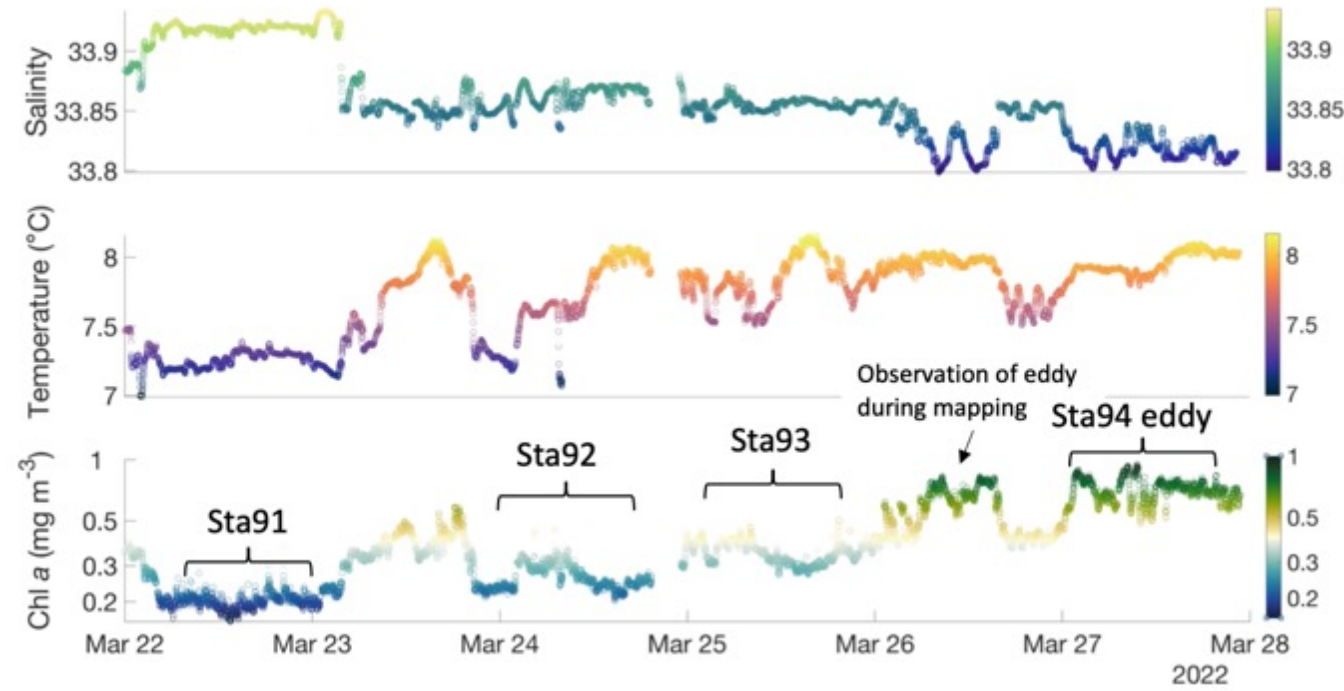
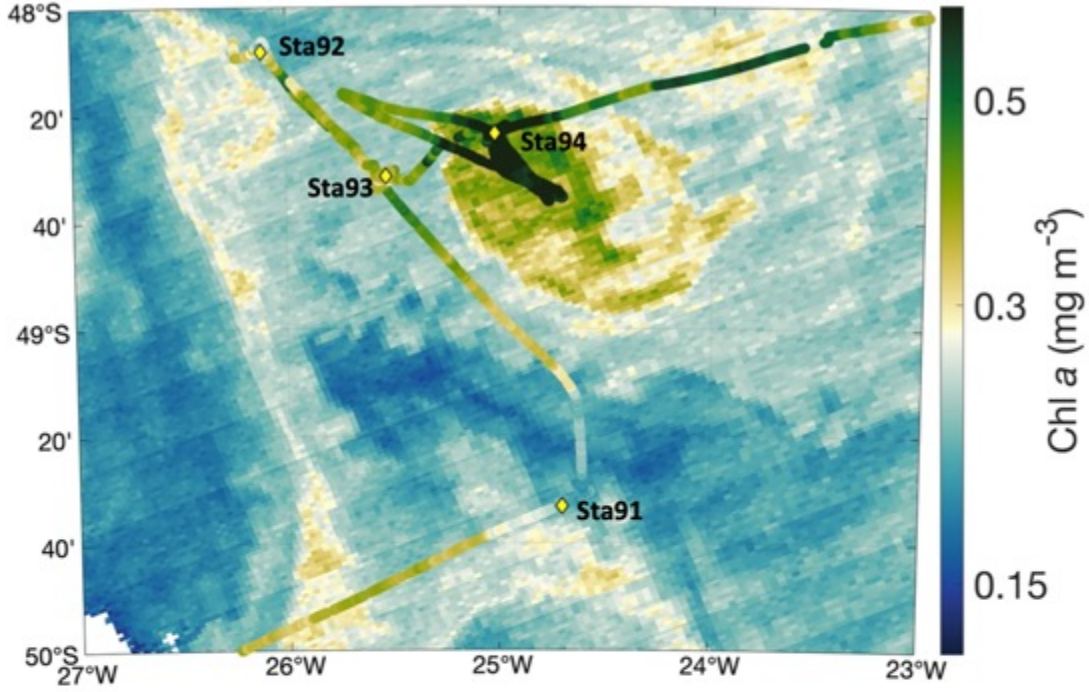
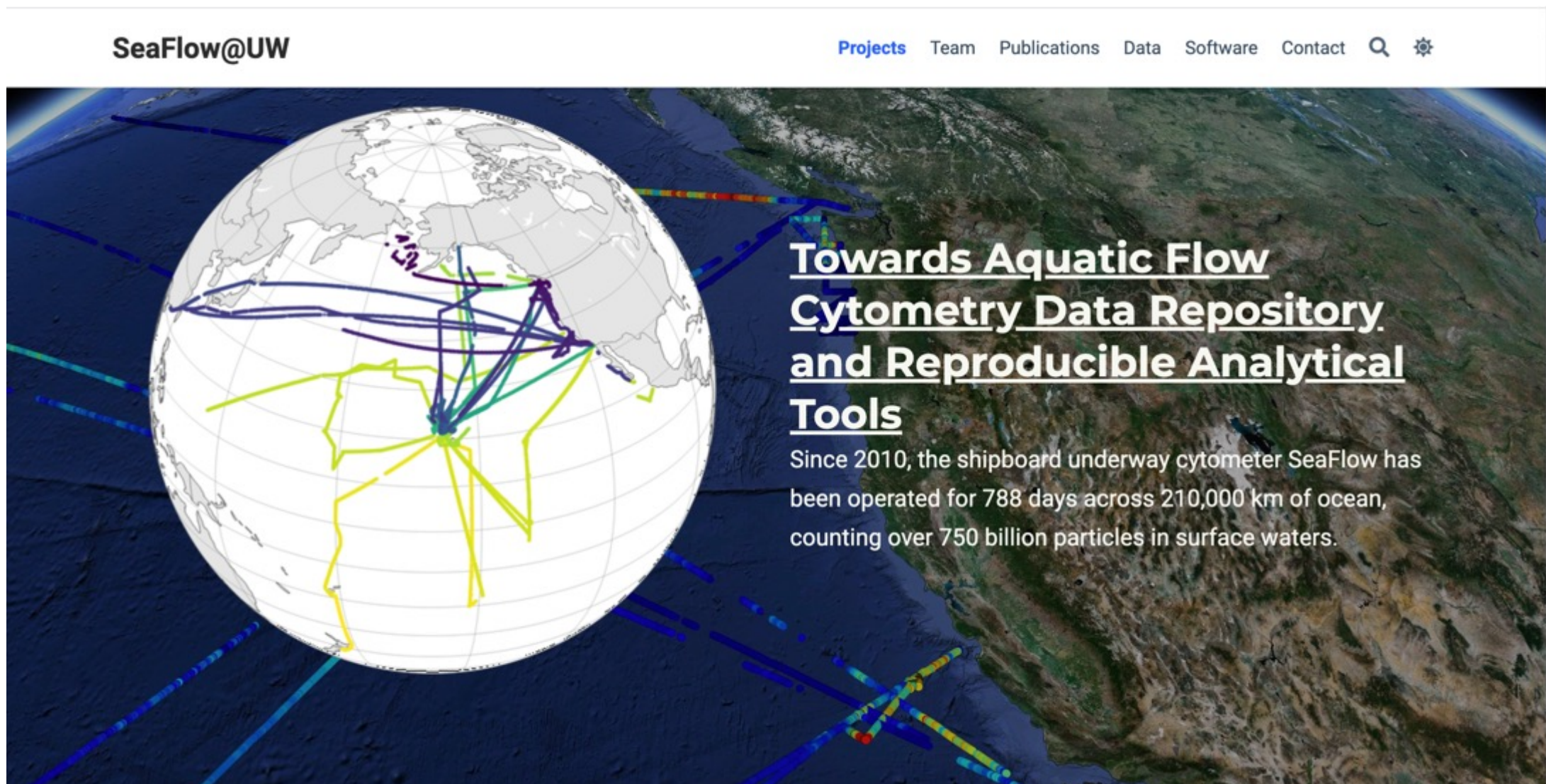


Figure 5. Satellite (MODIS AQUA) chlorophyll a (Chl a) from March 27. Ship-track from March 22-27 overlain with points colored by Chl a derived from absorption spectra, and with four stations labeled.



# Open-source data repository of picoplankton in the open ocean



SeaFlow@UW

Projects Team Publications Data Software Contact 🔍 ⚙️

## Towards Aquatic Flow Cytometry Data Repository and Reproducible Analytical Tools

Since 2010, the shipboard underway cytometer SeaFlow has been operated for 788 days across 210,000 km of ocean, counting over 750 billion particles in surface waters.

<https://seaflo.netlify.app/>





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Simons

# CMAP

Collaborative Marine Atlas Project

MARINE DATA, UNIFIED

A collection of harmonized data and open-source tools to investigate the hidden worlds of ocean microbes

<https://simonscmap.com/>

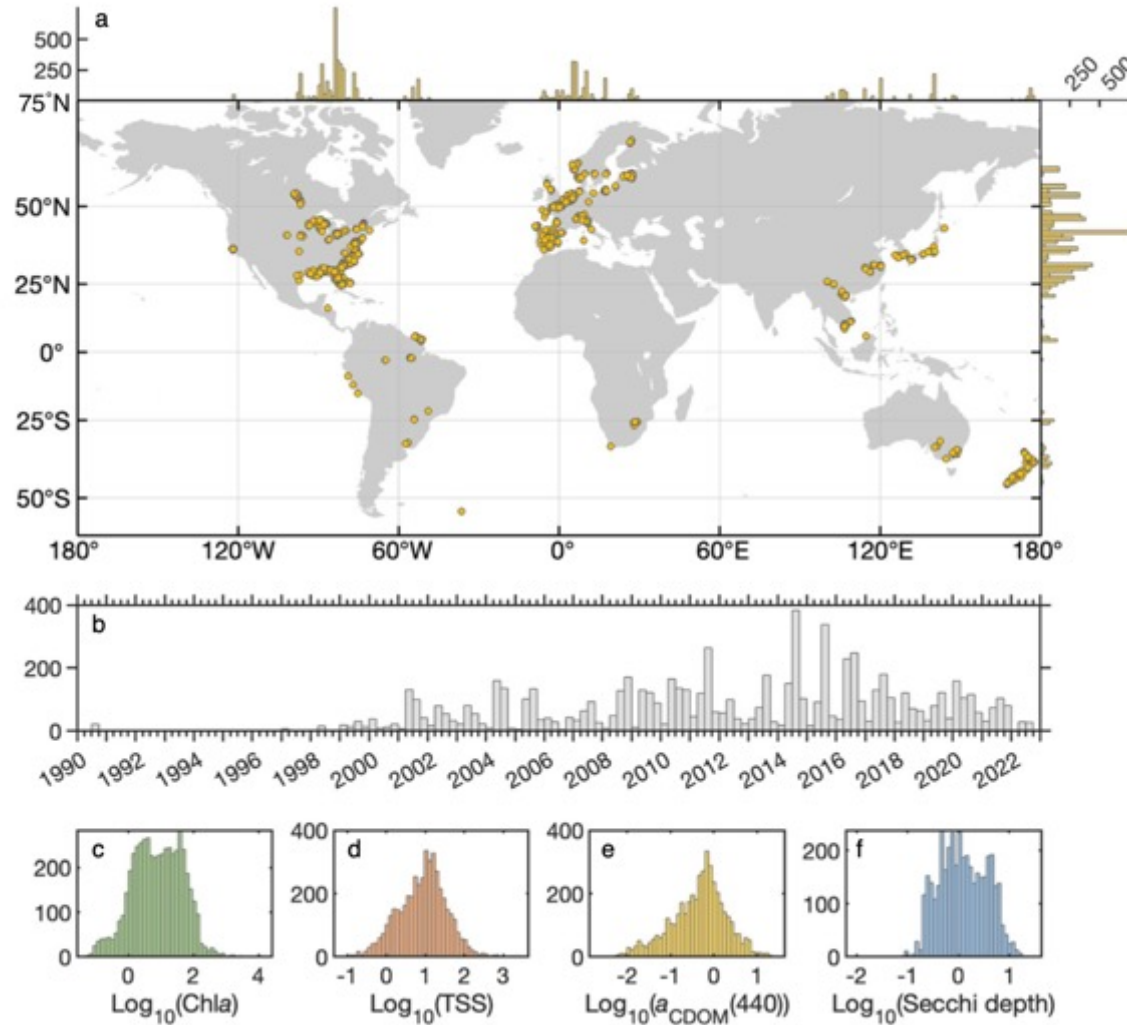
OPEN

**GLORIA - A globally representative hyperspectral *in situ* dataset for optical sensing of water quality**

Moritz K. Lehmann et al.\*

Check for updates

DATA DESCRIPTOR





How can we navigate the push-pull of the untapped potential in PCC algorithms and the inherent challenges?

*Different questions will have different data needs. Consider when a given data product is applicable, and when it is not. **What** do you want to know, and **why**?*

- Consider scales of spatial and temporal variability
- Remember that uncertainties “complete the data”

# What are the major challenges in PCC algorithm work?

- Sensitivity of methods to the uncertainties in measured products and/or intermediate derived products
- Target variables (PCC groups) are often defined by proxy, ultimately limiting algorithm refinement
- Sufficient datasets for model development and testing are not trivial to collect
- Linking products to what is needed by end users (e.g., climate & ecosystem modelers, water quality management & HAB detection)

# What are the exciting opportunities in PCC algorithm work?

- Advancements in data collection technology for assessing in situ PCC
- Hyperspectral satellite remote sensing & UAV data
- Increased application of machine learning and computing power advancements
- Incorporation of additional/ancillary data, both in situ and via combining data from multiple satellite platforms
- Improved models and data collection that in turn provide insights into finer spatial and temporal scale properties of ocean dynamics



Ocean Optics Summer Course, 2011  
Darling Marine Center, UMaine





Thank you!

# A few favorite resources for GitHub, python, and machine learning

Git – the simple guide:

<https://rogerdudler.github.io/git-guide/>

Data Analysis in python for oceanographers:

[https://currents.soest.hawaii.edu/ocn\\_data\\_analysis/index.html](https://currents.soest.hawaii.edu/ocn_data_analysis/index.html)

Recommendation from Patrick:

<https://www.pythonlikeyoumeanit.com/>

Tools for satellite data analysis designed by Patrick:

<https://github.com/patrickcgray/open-geo-tutorial>

Set of four videos that explain neural networks and deep/shallow learning:

[https://www.youtube.com/watch?v=aircAruvnKk&list=PLZHQObOWTQDNU6R1\\_67000Dx\\_ZCJB-3pi](https://www.youtube.com/watch?v=aircAruvnKk&list=PLZHQObOWTQDNU6R1_67000Dx_ZCJB-3pi)

This website lets you play around with number of layers and neurons in a neural network and visualize the effects:

<https://playground.tensorflow.org>

General resource for clear explanations of math terms and concepts:

<https://betterexplained.com/>



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