

Volume III

PART II THEORY OF LIGHT FIELDS

Chapter 4

Canonical Forms of the Equation of Transfer

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